

Measuring Ex-Ante Welfare in Insurance Markets

Nathaniel Hendren

Harvard University

Measuring Welfare in Insurance Markets

- Insurance markets with adverse selection can be inefficient
 - People may be willing to pay their cost of insurance
 - But equilibrium prices reflect average costs (Akerlof 1970)
 - Generates deadweight loss (DWL) from foregone efficient trades
- Recent literature quantifies these inefficiencies
 - Einav, Finkelstein, and Cullen (2010), Hackman, Kolstad, and Kowalski (2015), Handel, Kolstad, and Spinnewijn (2016), Cabral and Cullen (2016), Mahoney and Weyl (Forthcoming)
- Proposes comparing demand and cost curves (DWL) for thinking about optimal policy (e.g. subsidies/mandates)

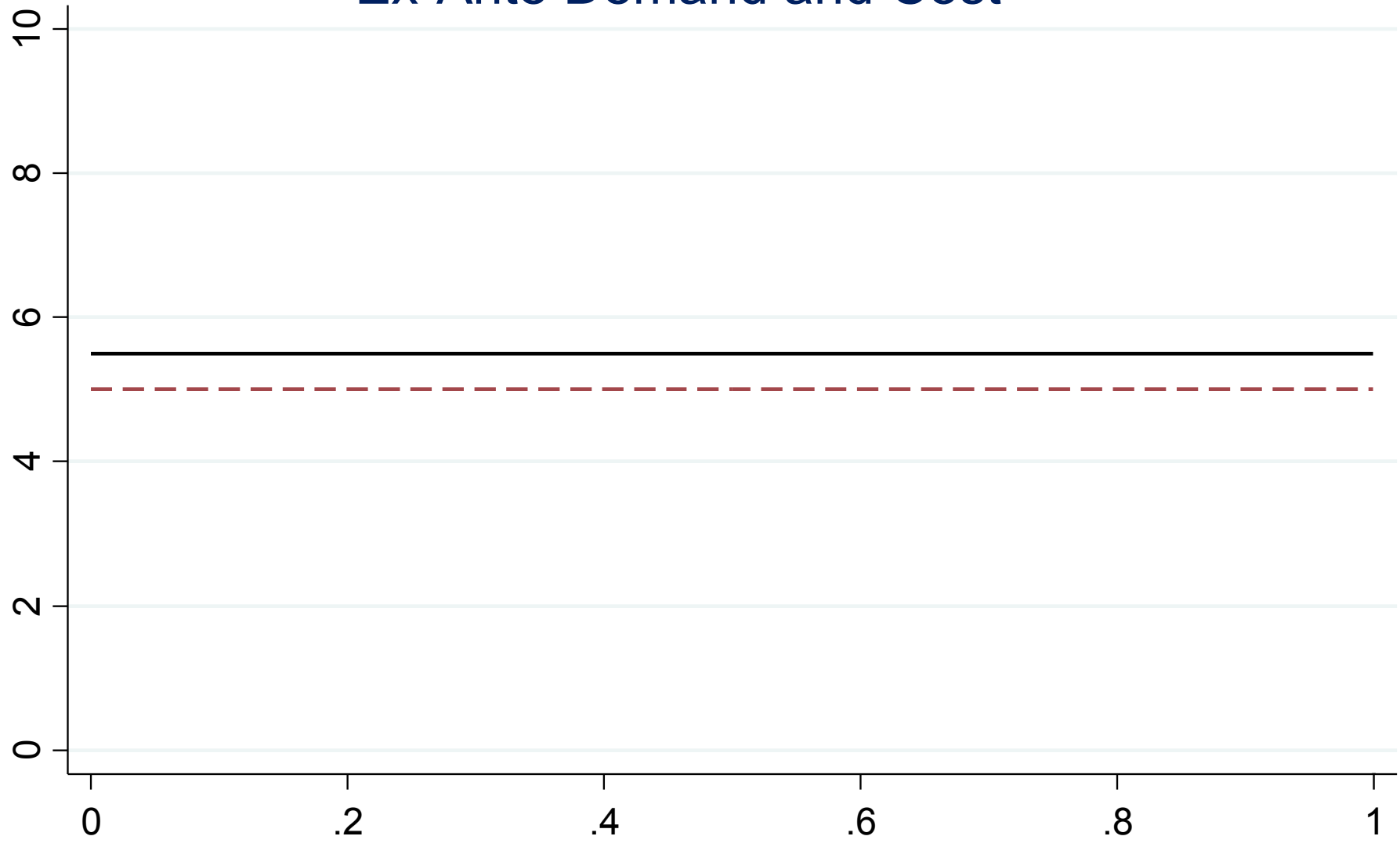
But DWL is Not the Only Measure of Welfare

- Insurance demand depends on knowledge/beliefs of risk
- Individuals often have some knowledge about risk when measuring demand, generating adverse selection
 - LTC, Disability, Life insurance (Hendren, 2013)
 - Dental Insurance (Cabral, forthcoming)
 - Unemployment insurance (Hendren, 2016)
 - Health insurance (Cardon and Hendel, 2001; Handel, 2013; Handel, Hendel, and Whinston, 2015)
- DWL is unstable measure of welfare (Hirshleifer, 1971)
 - Value of foregone trades can be misleading for optimal policy analysis

Motivating Example

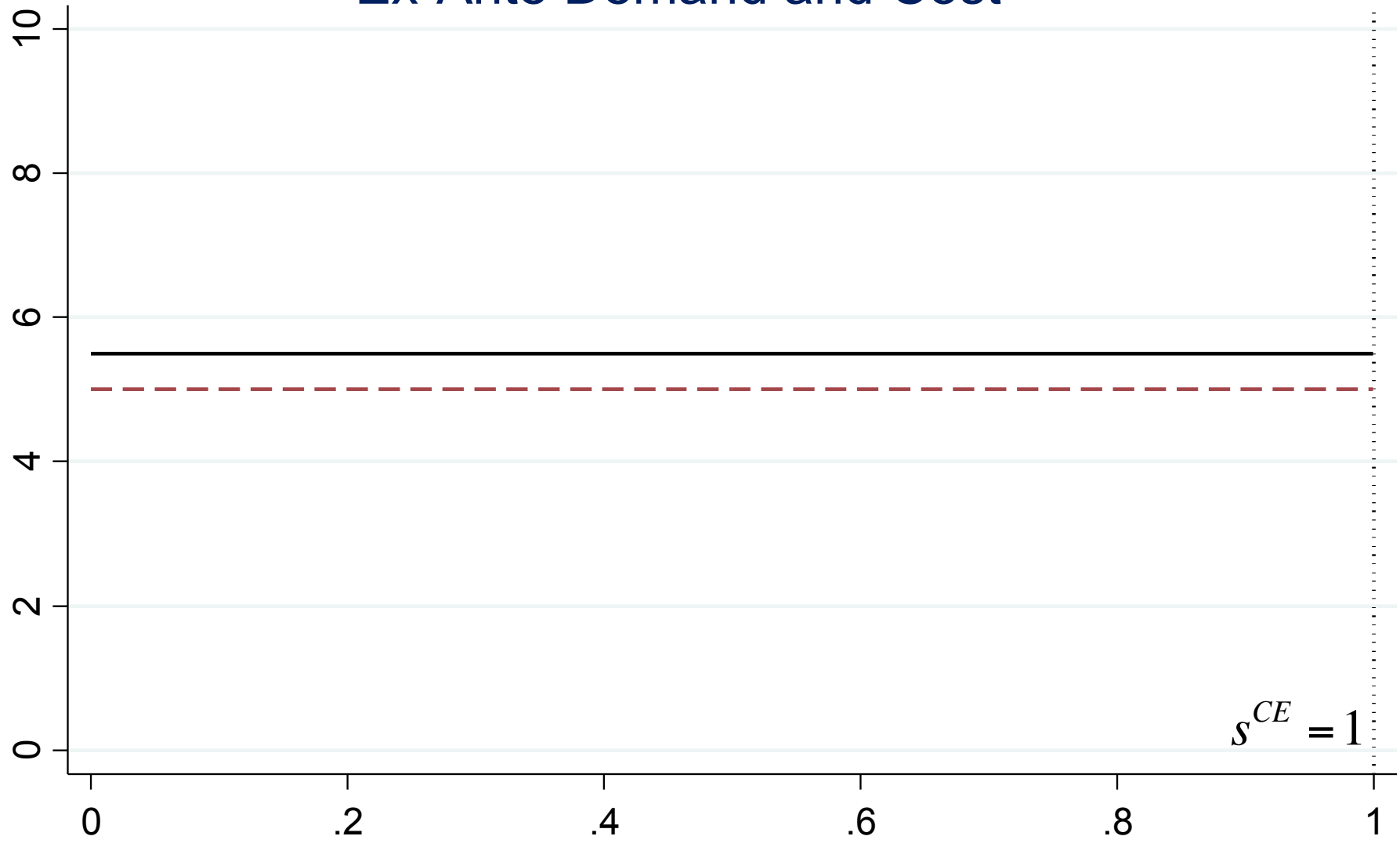
- Begin with simple example to illustrate issue and a solution
- Individuals have \$30
- Face a risk of losing \$ m , uniformly distributed between 0 and 10
- Willing to pay \$0.50 markup for full insurance if CRRA is 3
 - Indifferent between roughly \$24.50 versus uniformly distributed consumption on [20 , 30]
 - Would be “efficient” for everyone to have \$25 with certainty
 - Value of insurance market is \$0.50
- How does this map to demand and cost curves?

Ex-Ante Demand and Cost



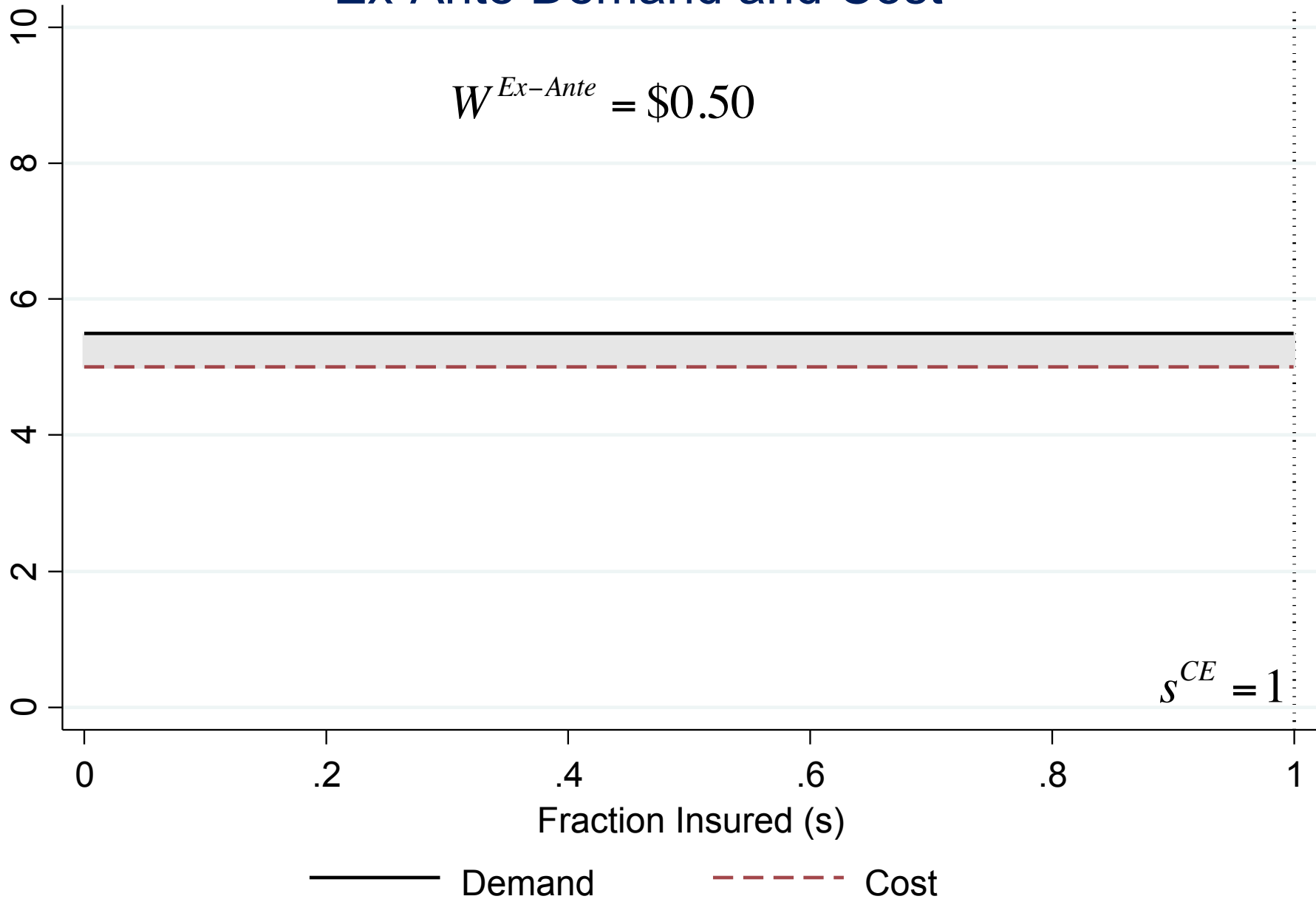
— Demand - - - - - Cost

Ex-Ante Demand and Cost



— Demand - - - Cost

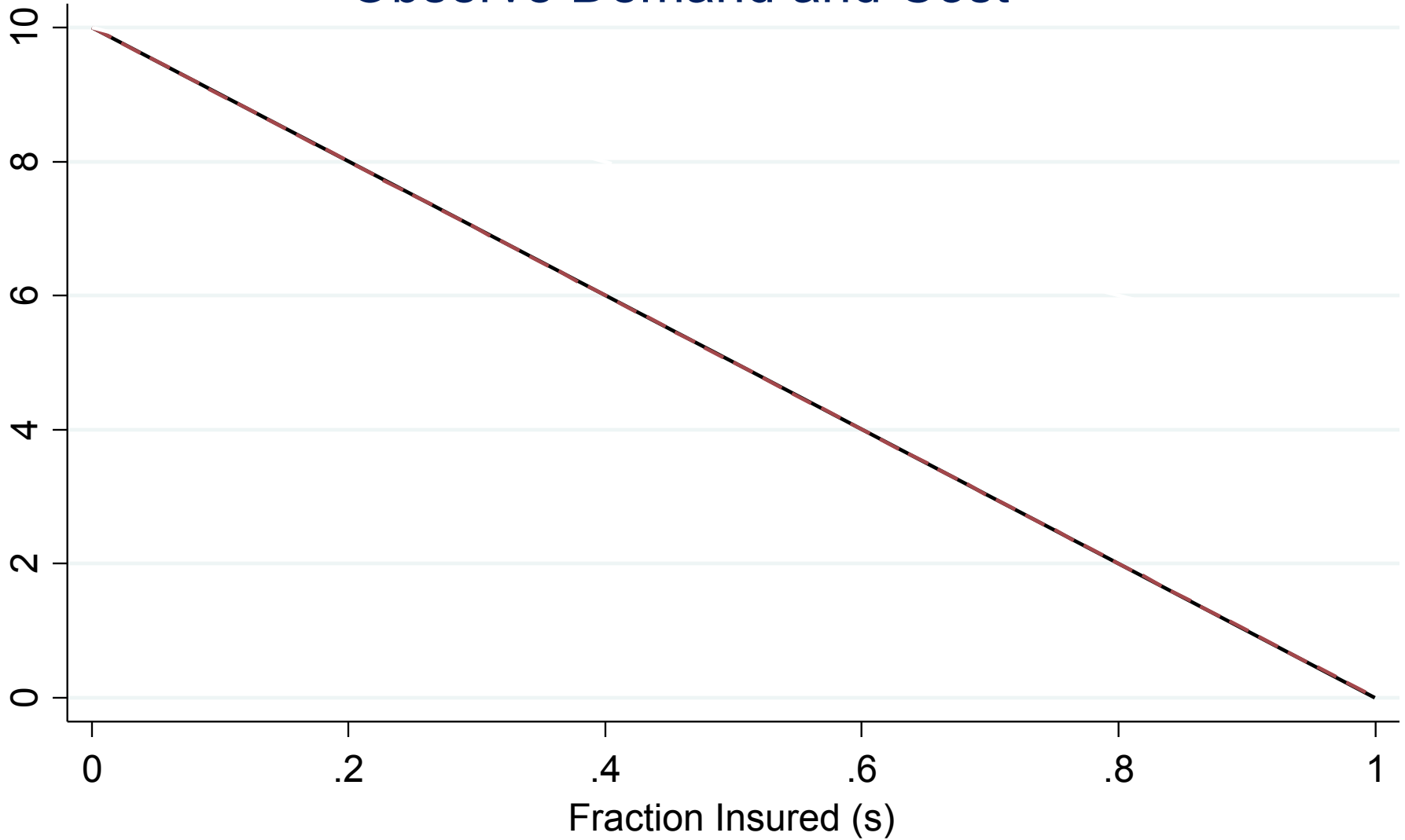
Ex-Ante Demand and Cost



Motivating Example

- What if people have information about their risk when we measure demand?
- Begin with extreme case: suppose individuals learn their loss
 - Willingness to pay equals cost, $D(s)=m(s)$

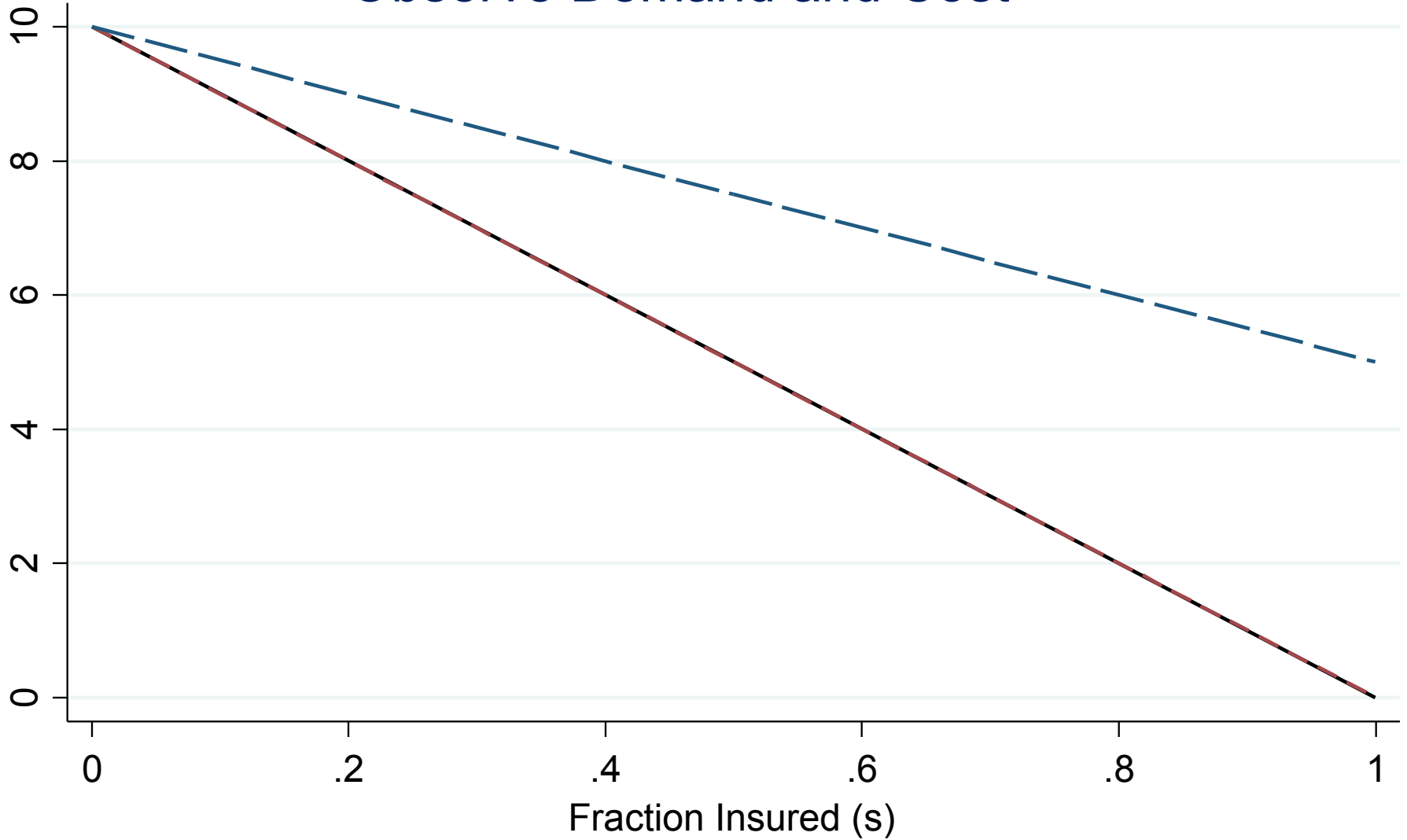
Observe Demand and Cost



— Observed Demand

- - - Marginal Cost

Observe Demand and Cost

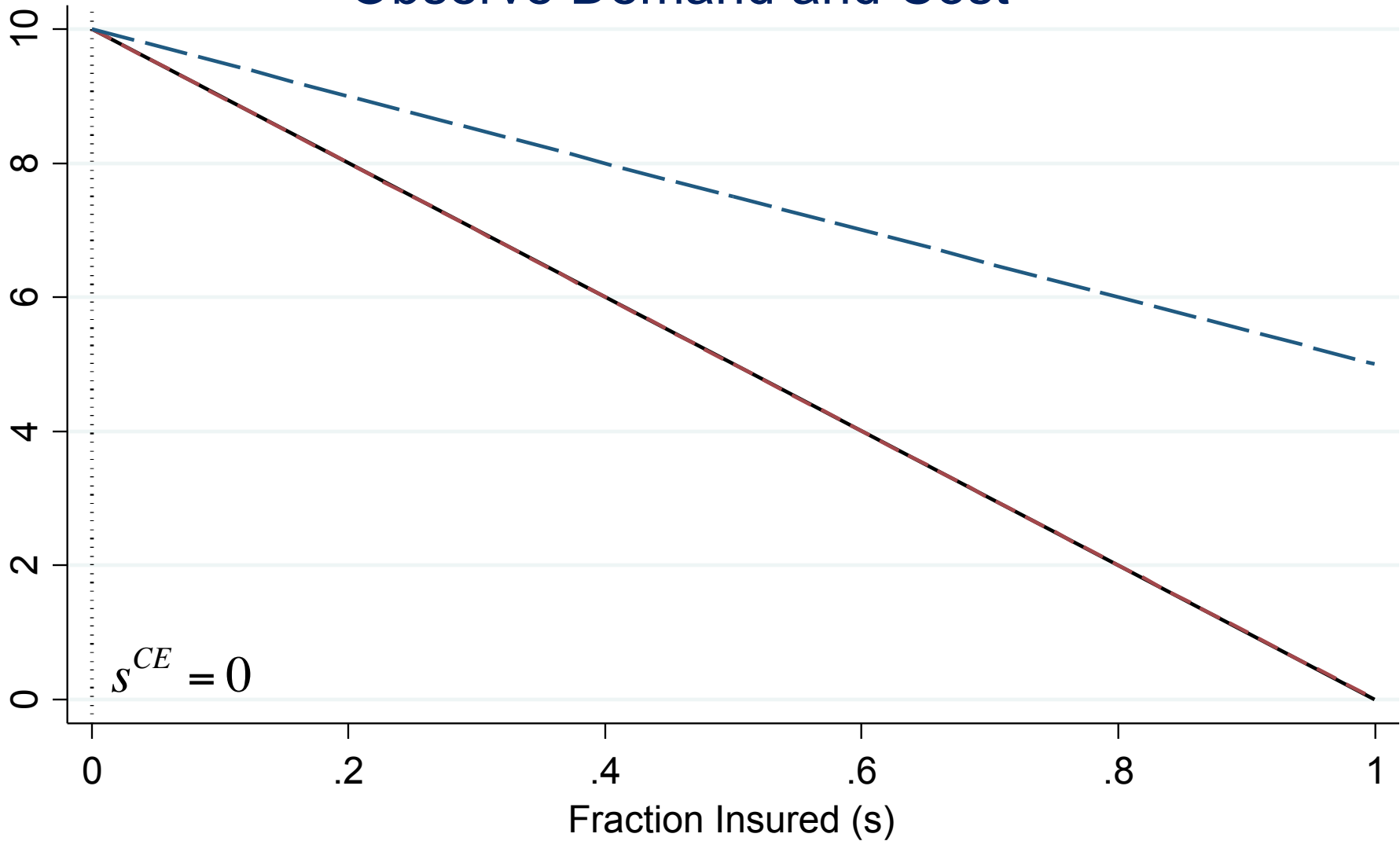


— Observed Demand

- - - Marginal Cost

- - - Average Cost

Observe Demand and Cost

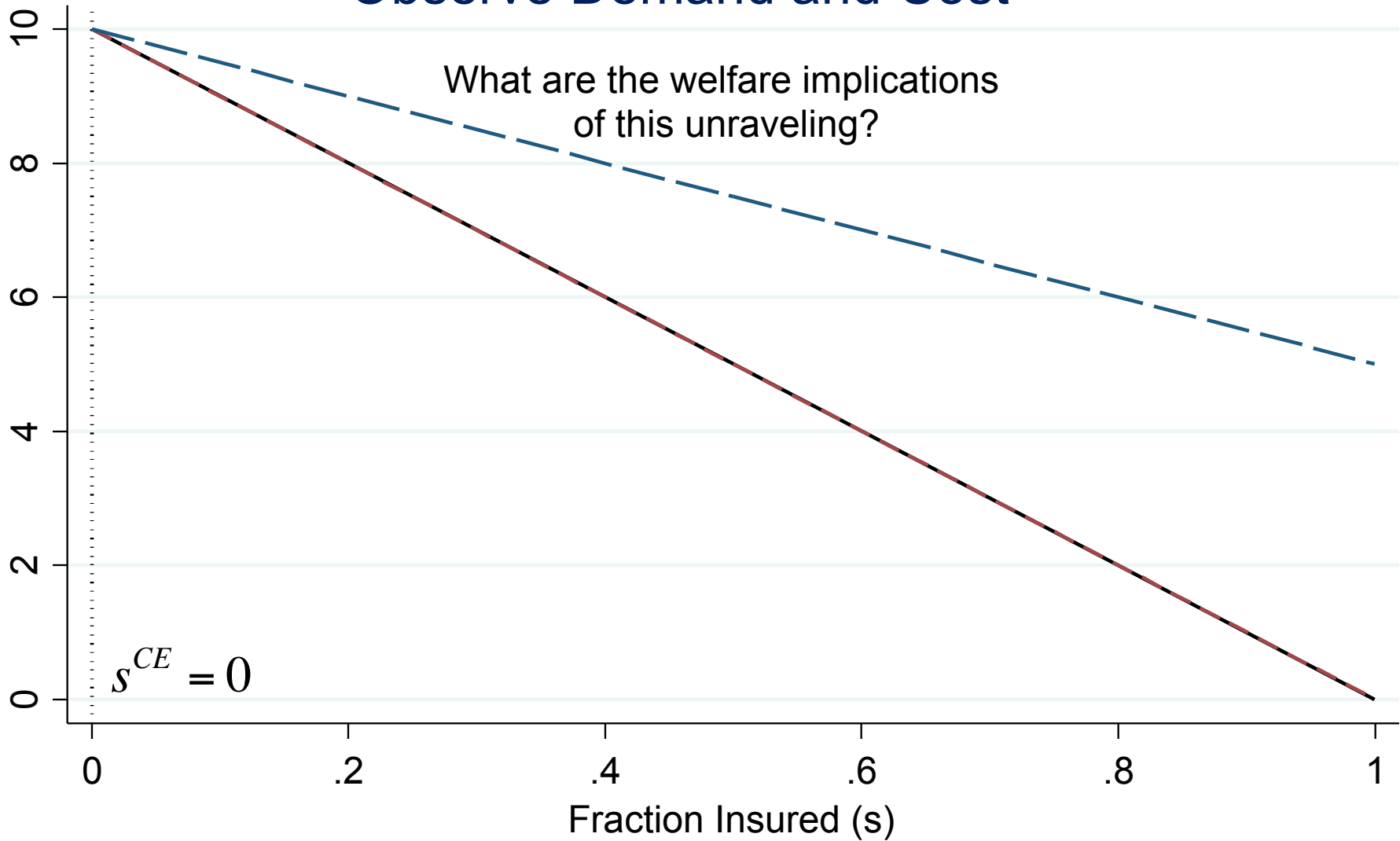


— Observed Demand

- - - Marginal Cost

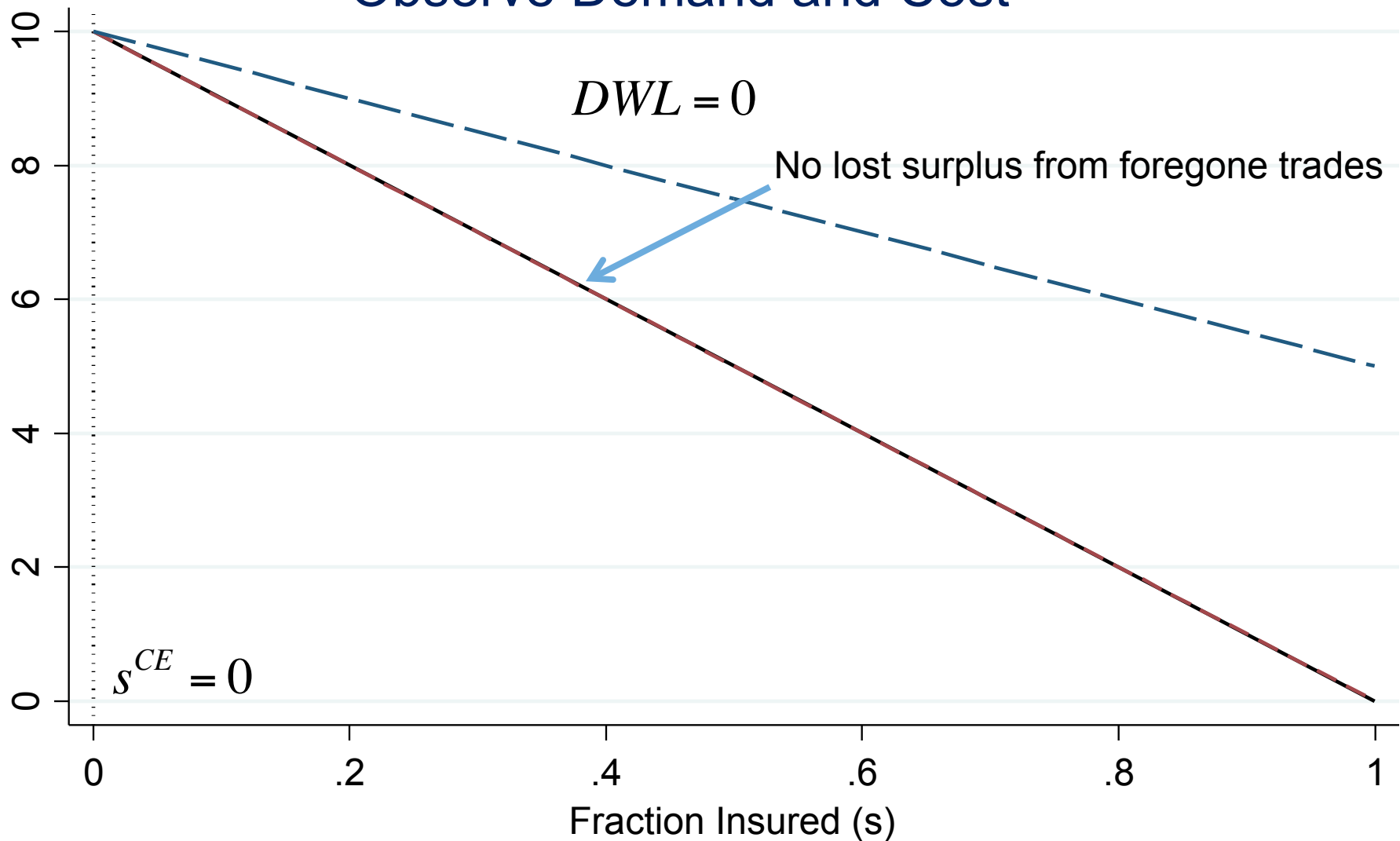
- - - Average Cost

Observe Demand and Cost



- Observed Demand
- - - Marginal Cost
- - - Average Cost

Observe Demand and Cost



- Observed Demand
- - - Marginal Cost
- - - Average Cost

Motivating Example

- Observed demand does not capture the value of insurance against learning about your risk prior to demand measurement
 - Adverse selection implies a divergence between DWL and Ex-Ante Welfare

Motivating Example

- Observed demand does not capture the value of insurance against learning about your risk prior to demand measurement
 - Adverse selection implies a divergence between DWL and Ex-Ante Welfare
- **This paper:** Derive new “ex-ante” demand curve to facilitate welfare analysis from behind the veil of ignorance
 - Combine Einav, Finkelstein, and Cullen (2010) with Baily-Chetty

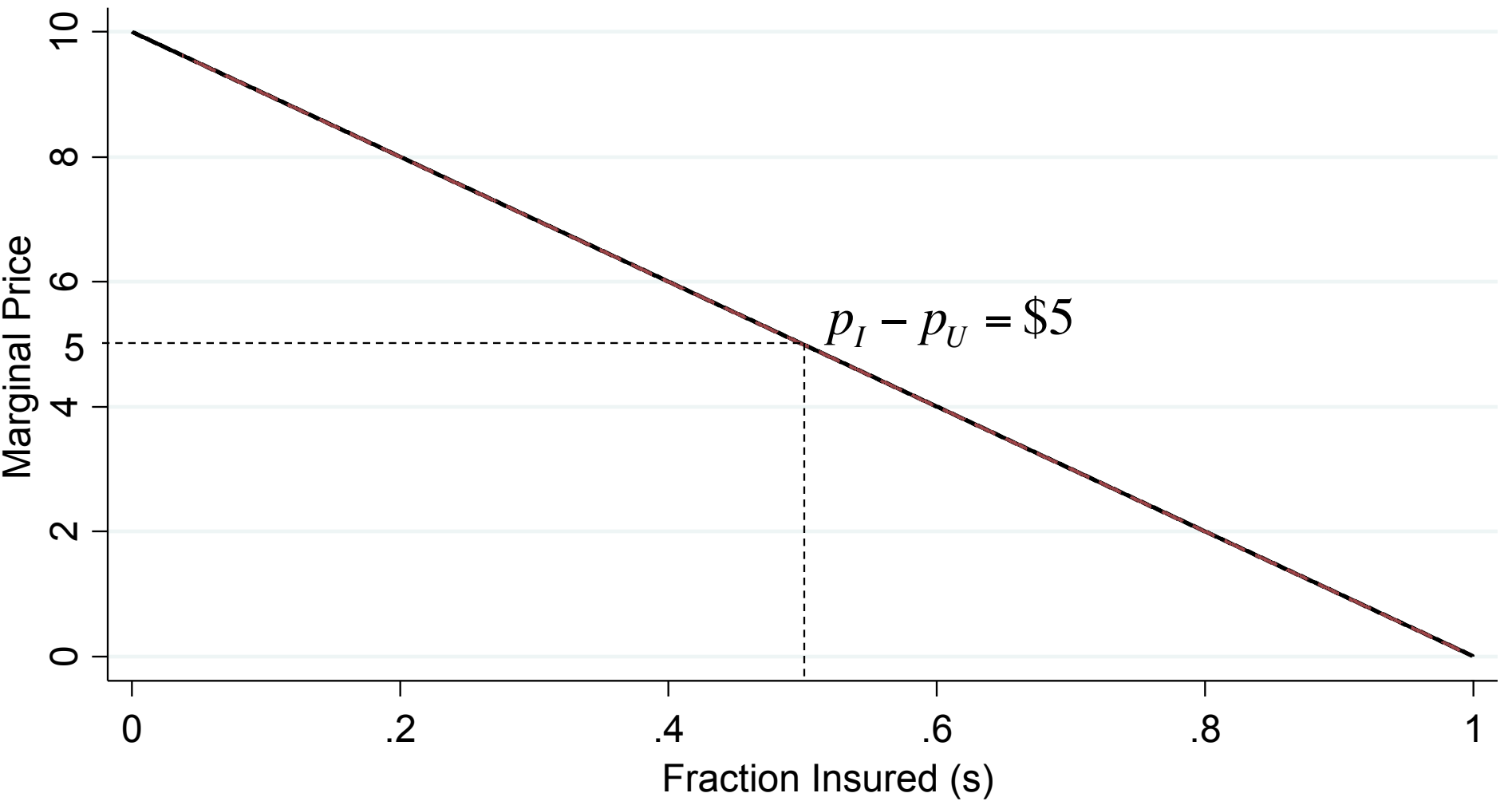
Motivating Example

- Dual philosophical motivation for using ex-ante demand:
 - **Ex-ante welfare** behind the veil of ignorance
 - **Ex-post welfare** using utilitarian aggregation
- Condition on any ex-ante known X if don't want redistribution across X
- Paper is primarily about ensuring that we have a consistent measure of welfare that is stable w.r.t. the amount of information people have when measuring demand

Deriving the Ex-Ante Demand Curve

- Return to example in which $D(s)=m(s)$
- Suppose $s = 50\%$ of the population has insurance
- Obtained by setting prices subject to a resource constraint:
 - Price of insurance, p_I
 - Price/penalty of being uninsured, p_U
 - Set so that $sp_I + (1-s)p_U = sAC(s)$

From Observed Demand to Ex-Ante Demand

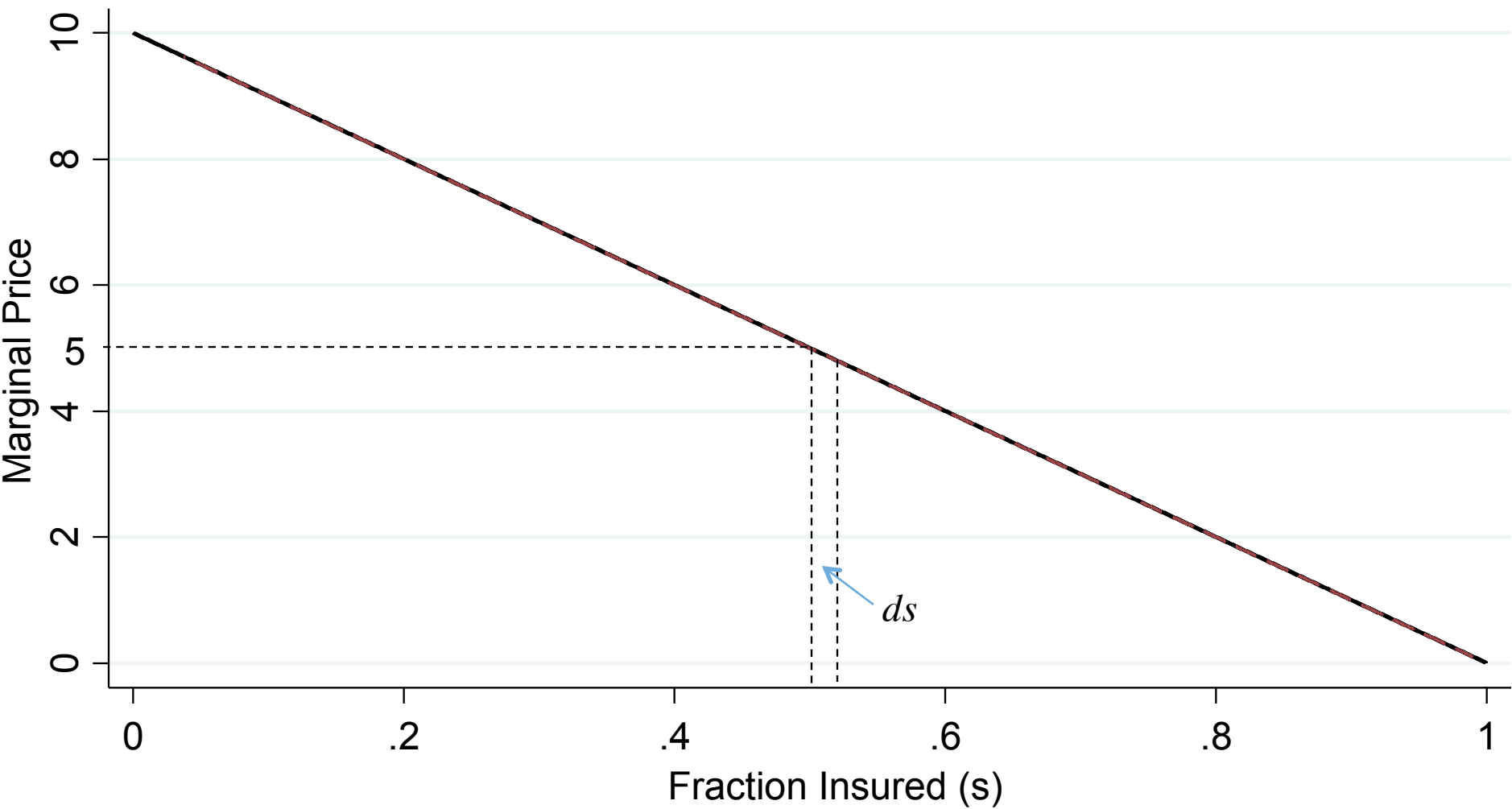


— Demand

- - - Marginal Cost

Price Calculation

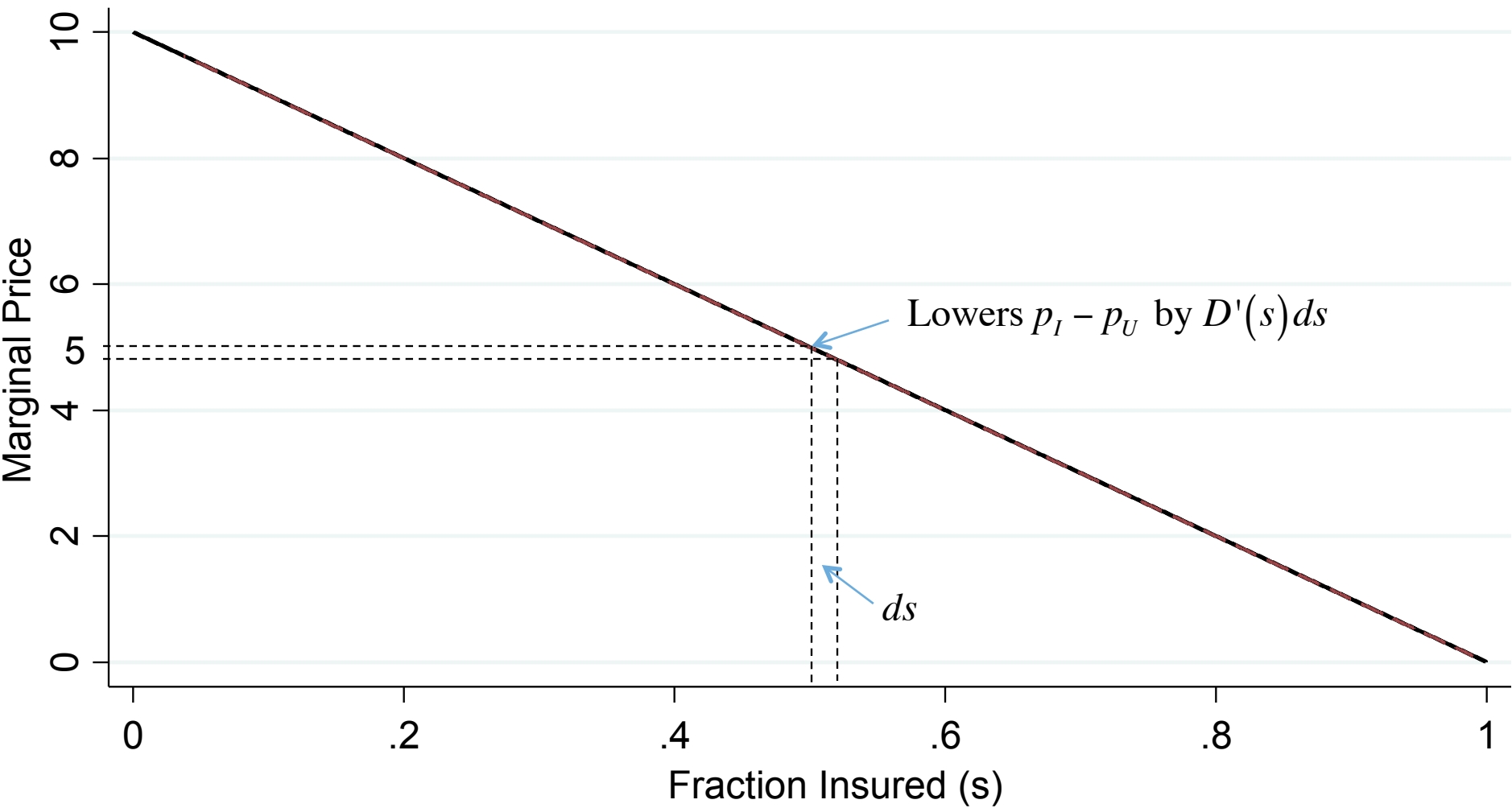
From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

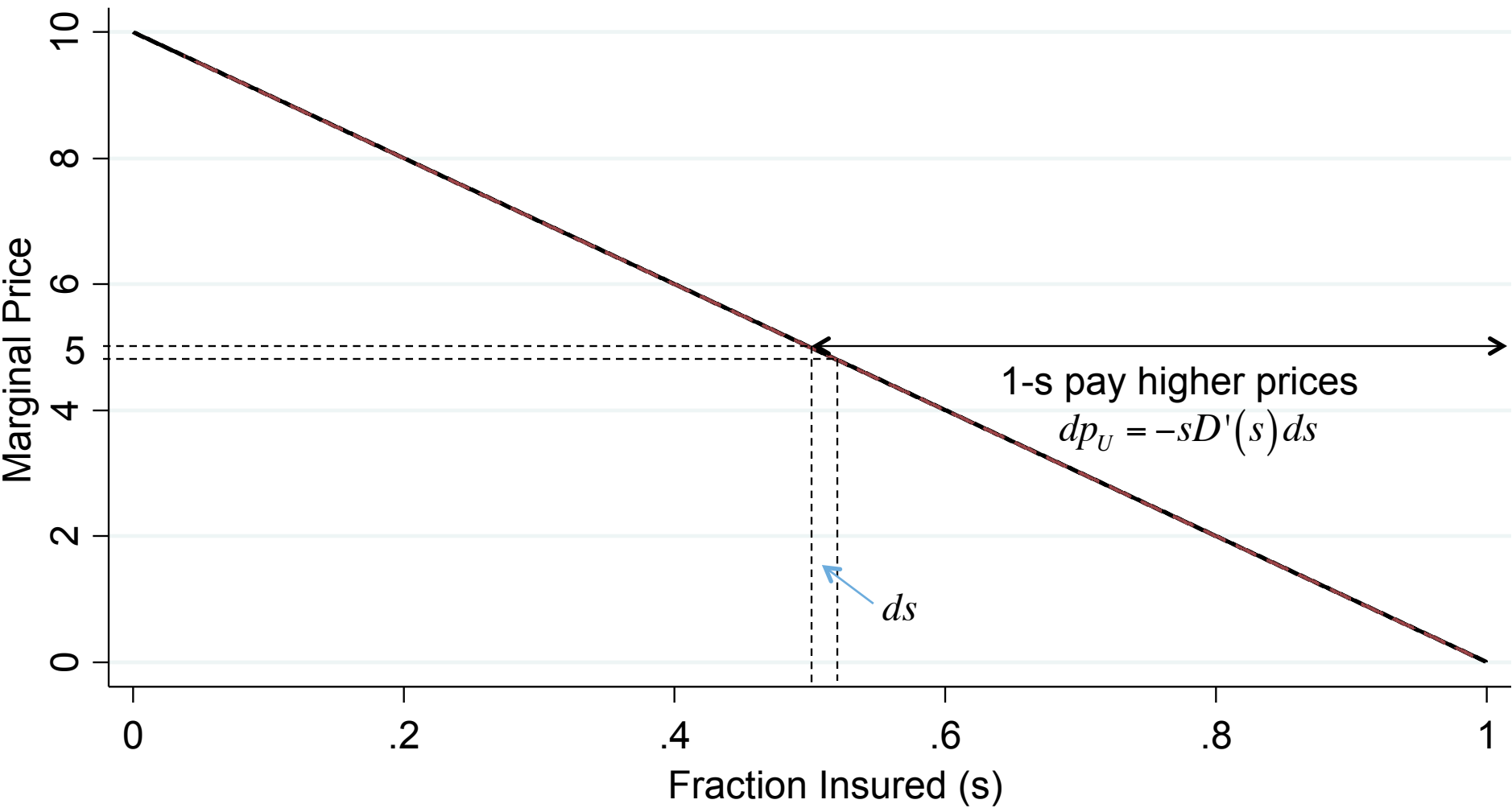
From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

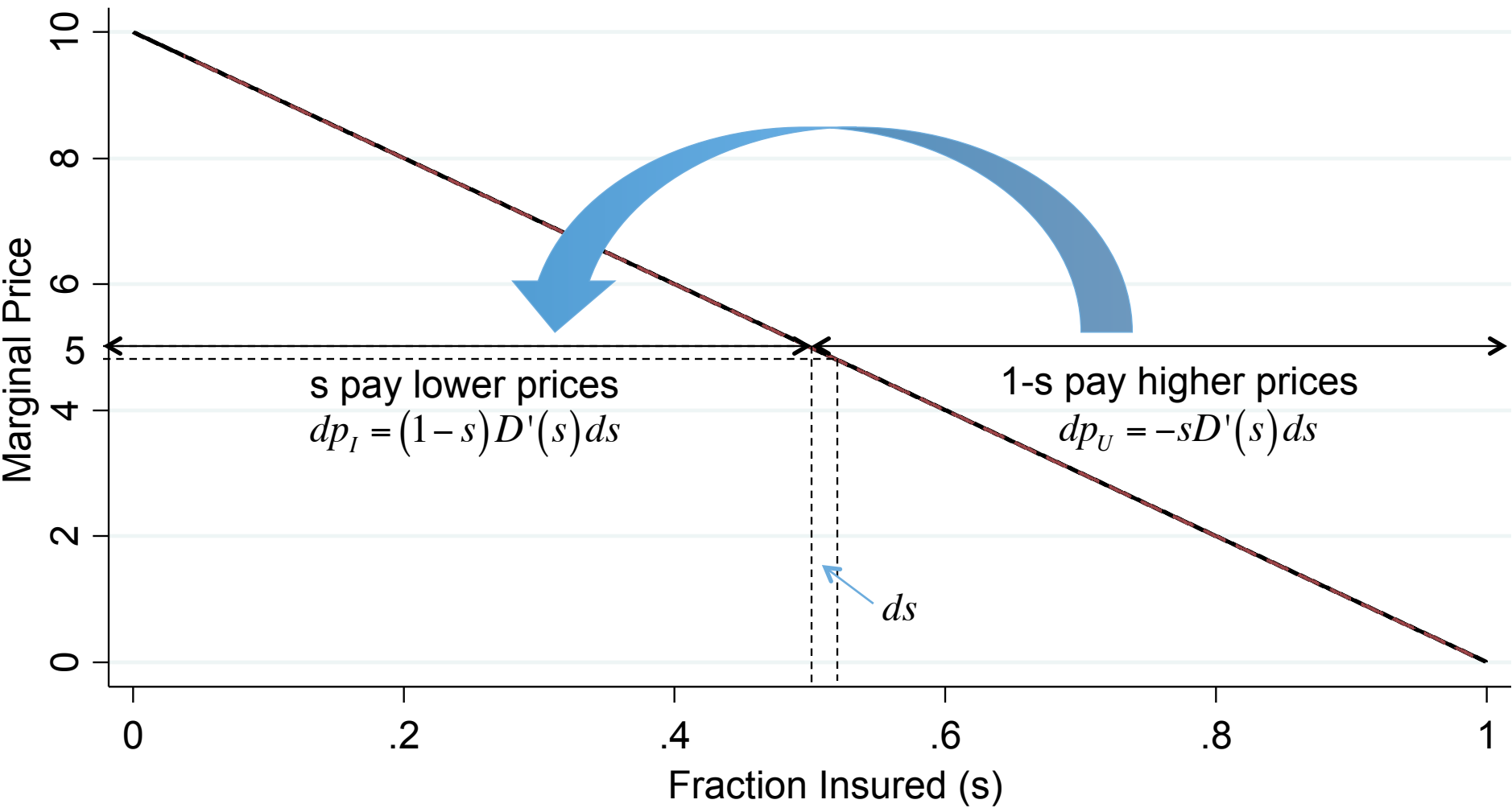
From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

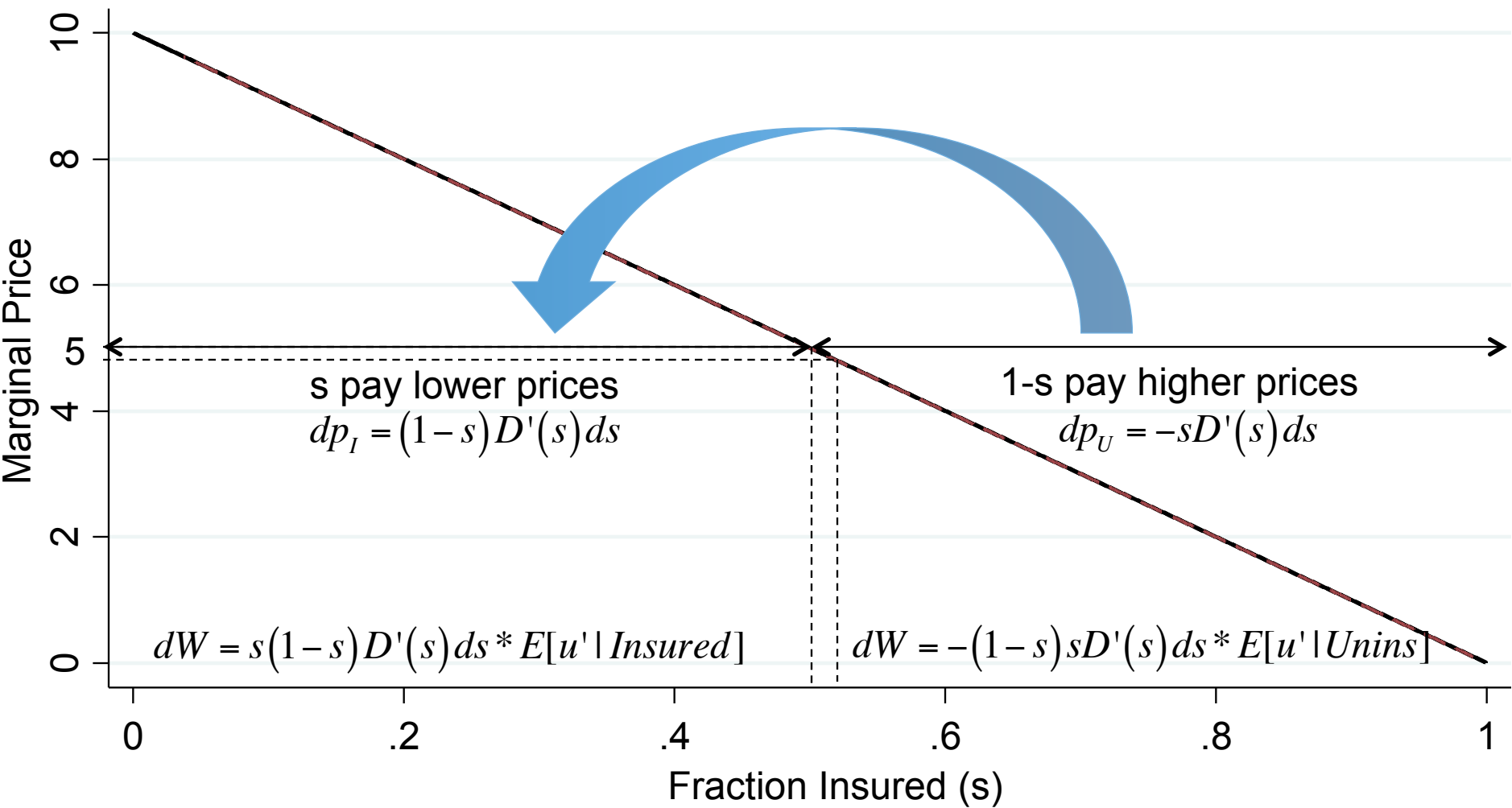
From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

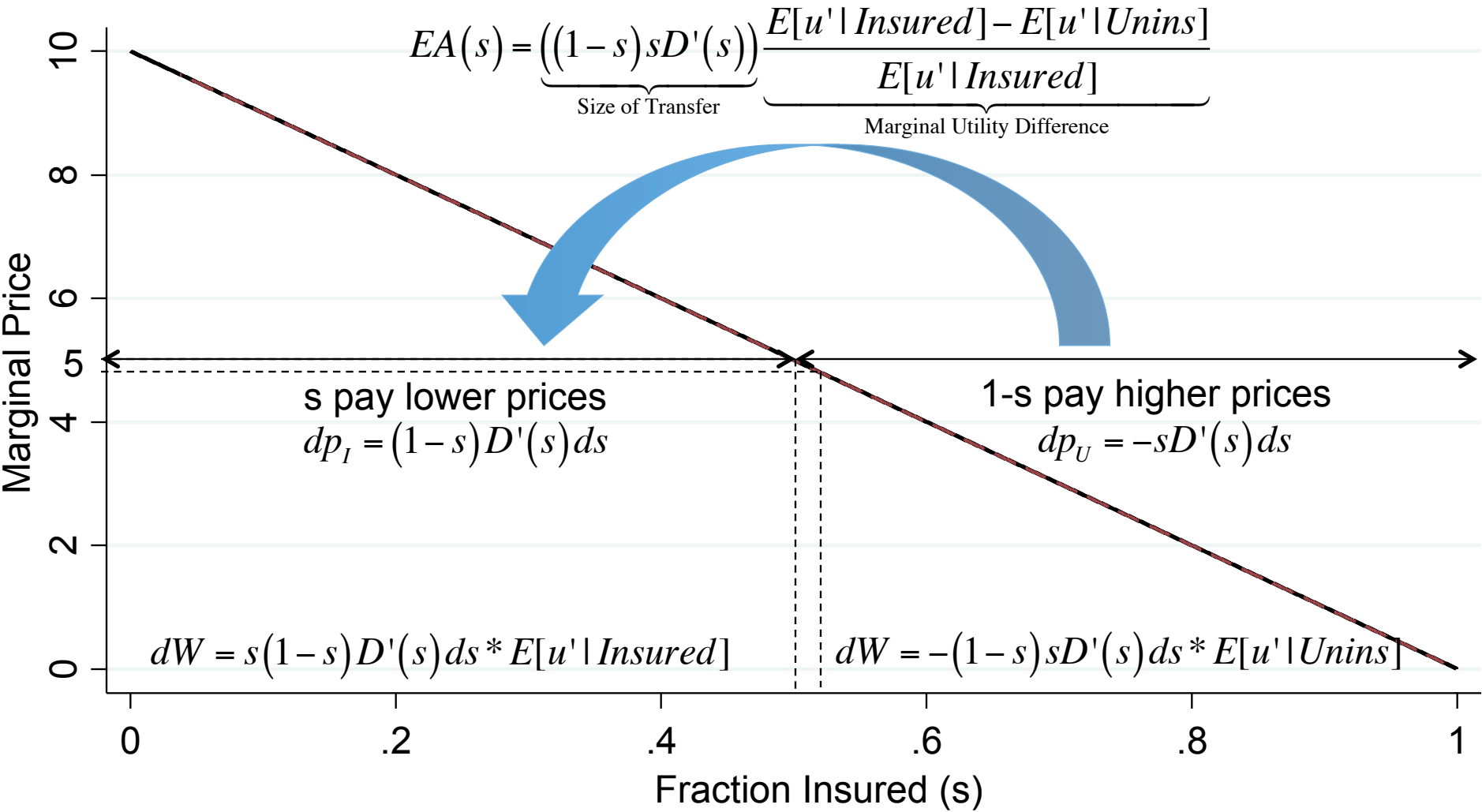
From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

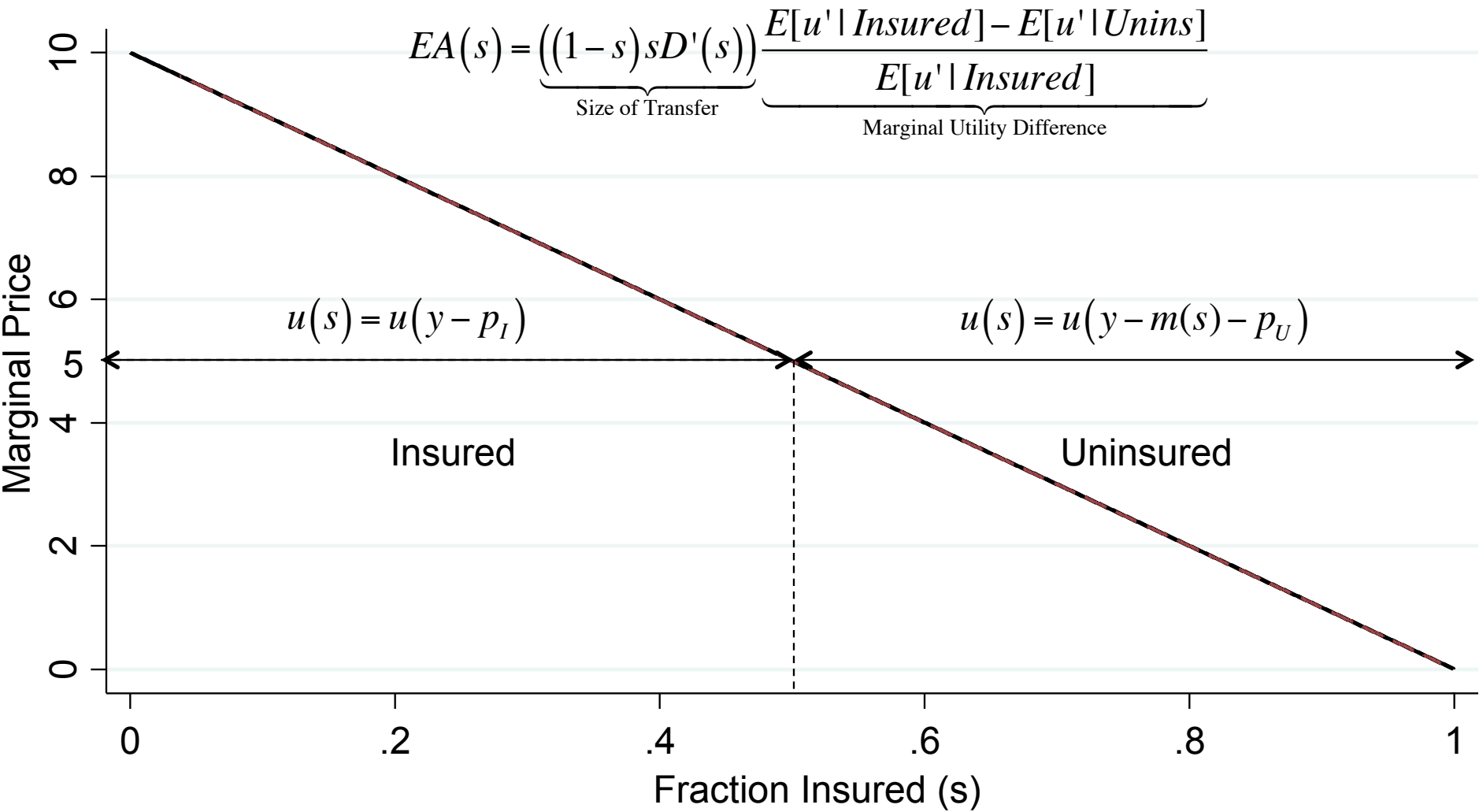
From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

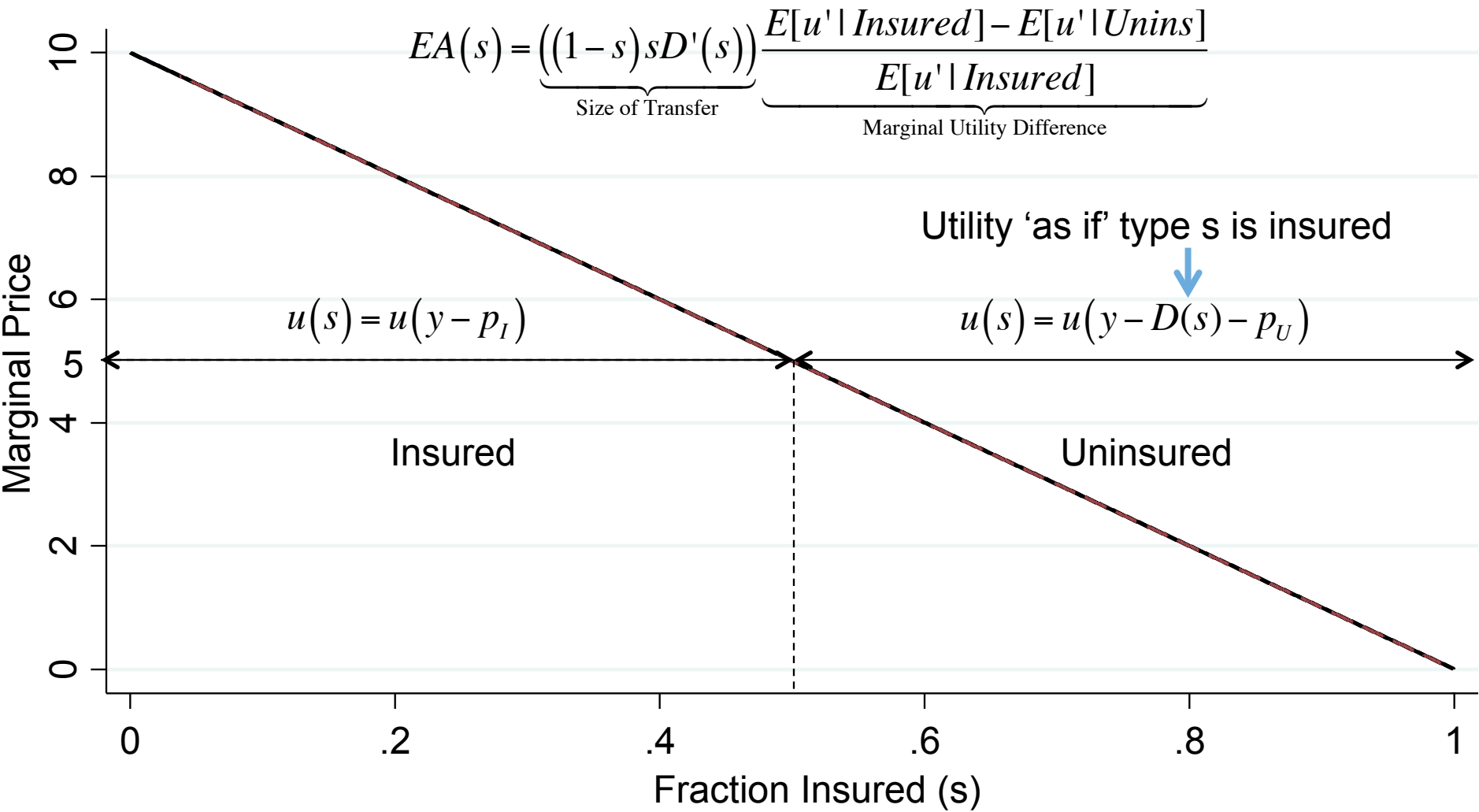
From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand

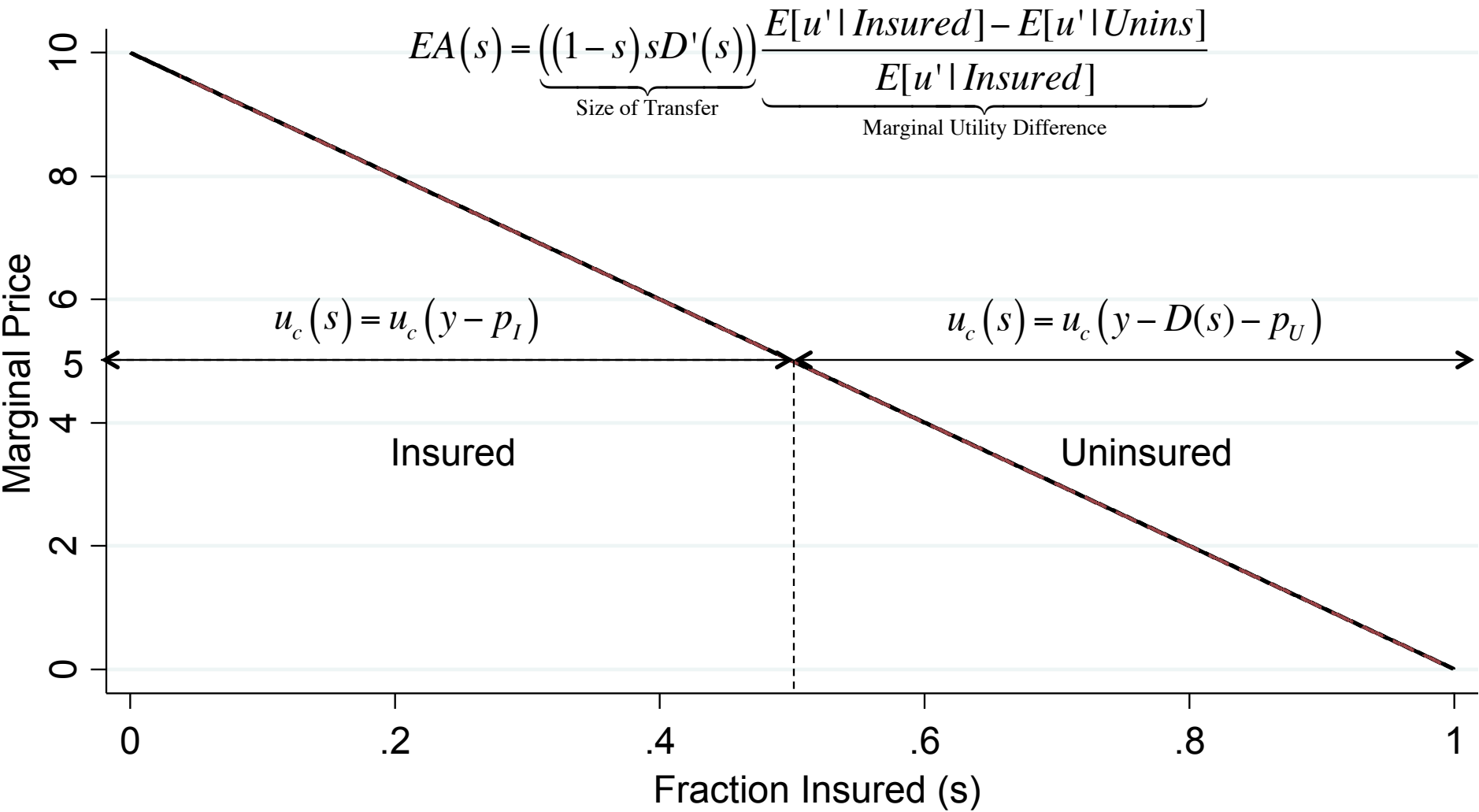


$$EA(s) = \underbrace{\left((1-s)sD'(s) \right)}_{\text{Size of Transfer}} \underbrace{\frac{E[u' | Insured] - E[u' | Unins]}{E[u' | Insured]}}_{\text{Marginal Utility Difference}}$$

— Demand

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand



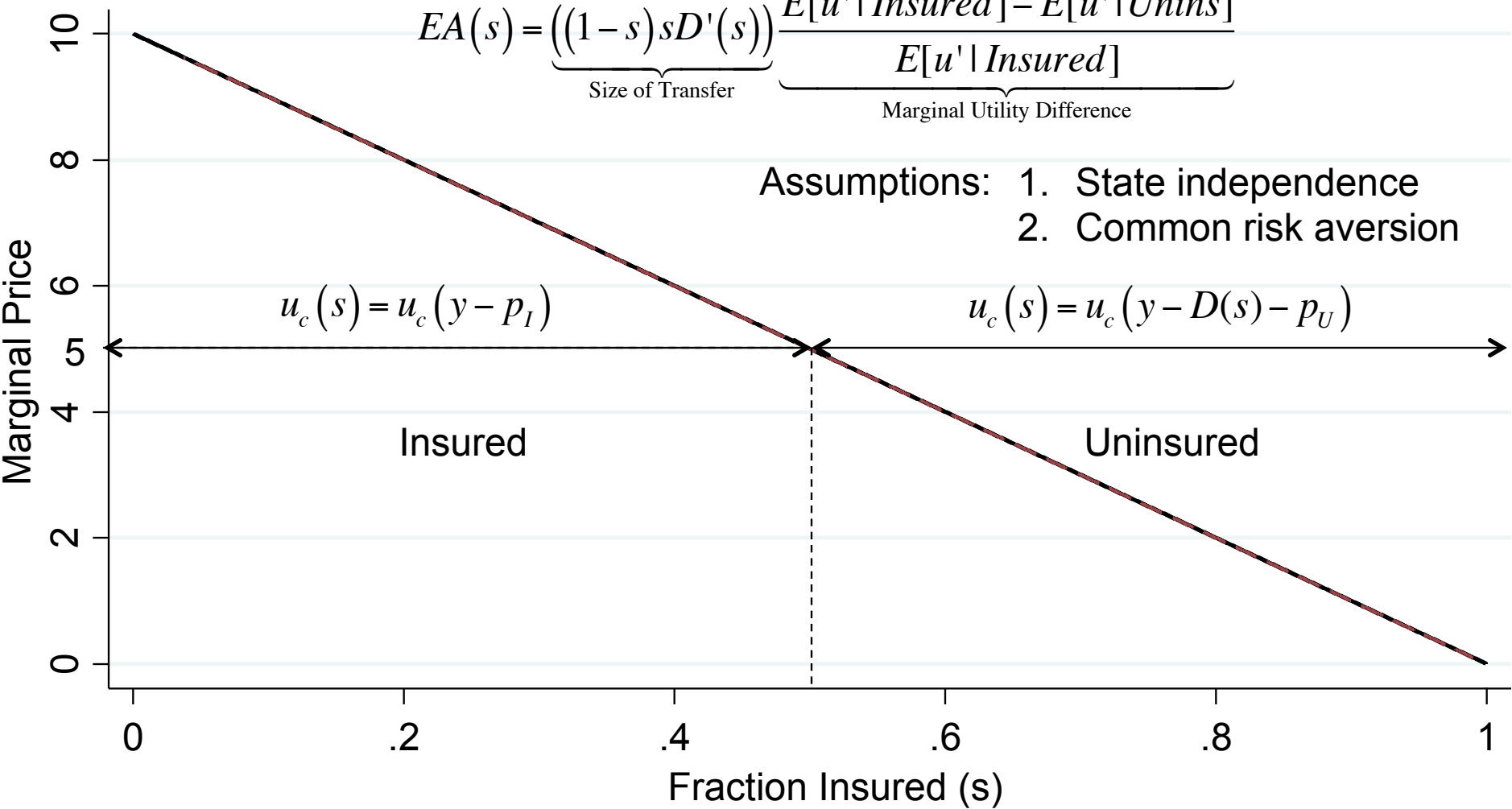
— Demand

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand

$$EA(s) = \underbrace{\left((1-s)sD'(s) \right)}_{\text{Size of Transfer}} \underbrace{\frac{E[u' | Insured] - E[u' | Unins]}{E[u' | Insured]}}_{\text{Marginal Utility Difference}}$$

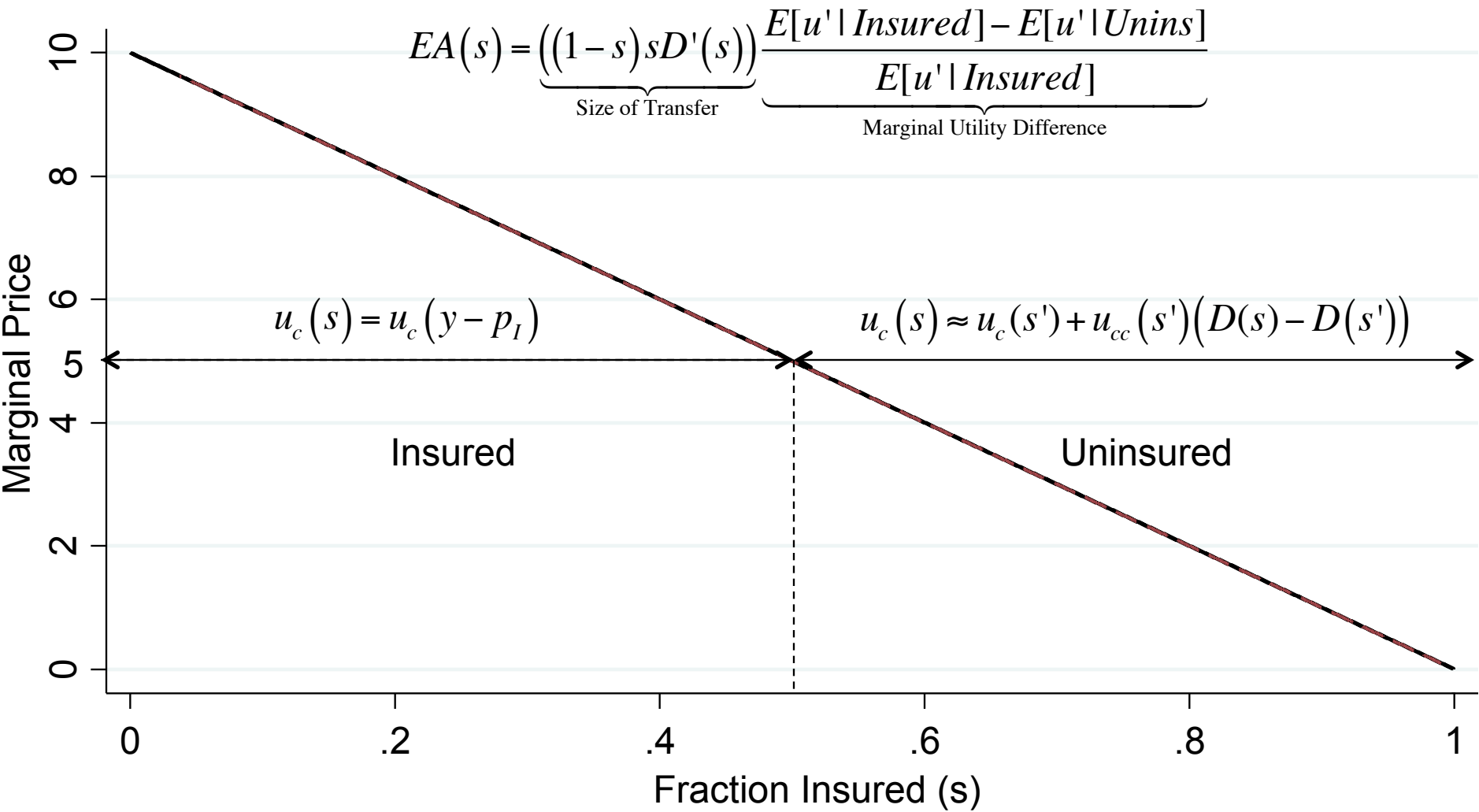
- Assumptions: 1. State independence
2. Common risk aversion



— Demand

- - - Marginal Cost

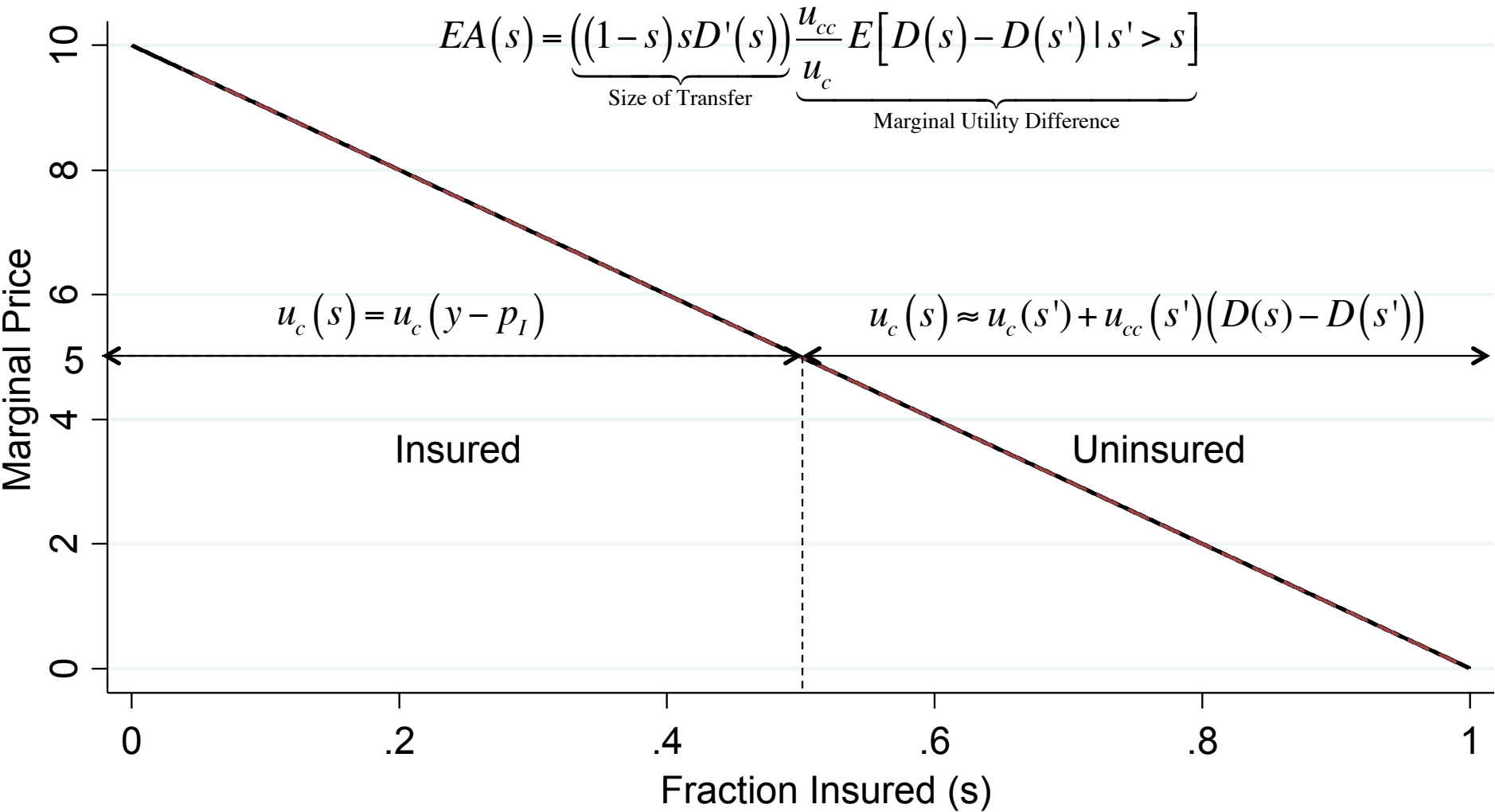
From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand

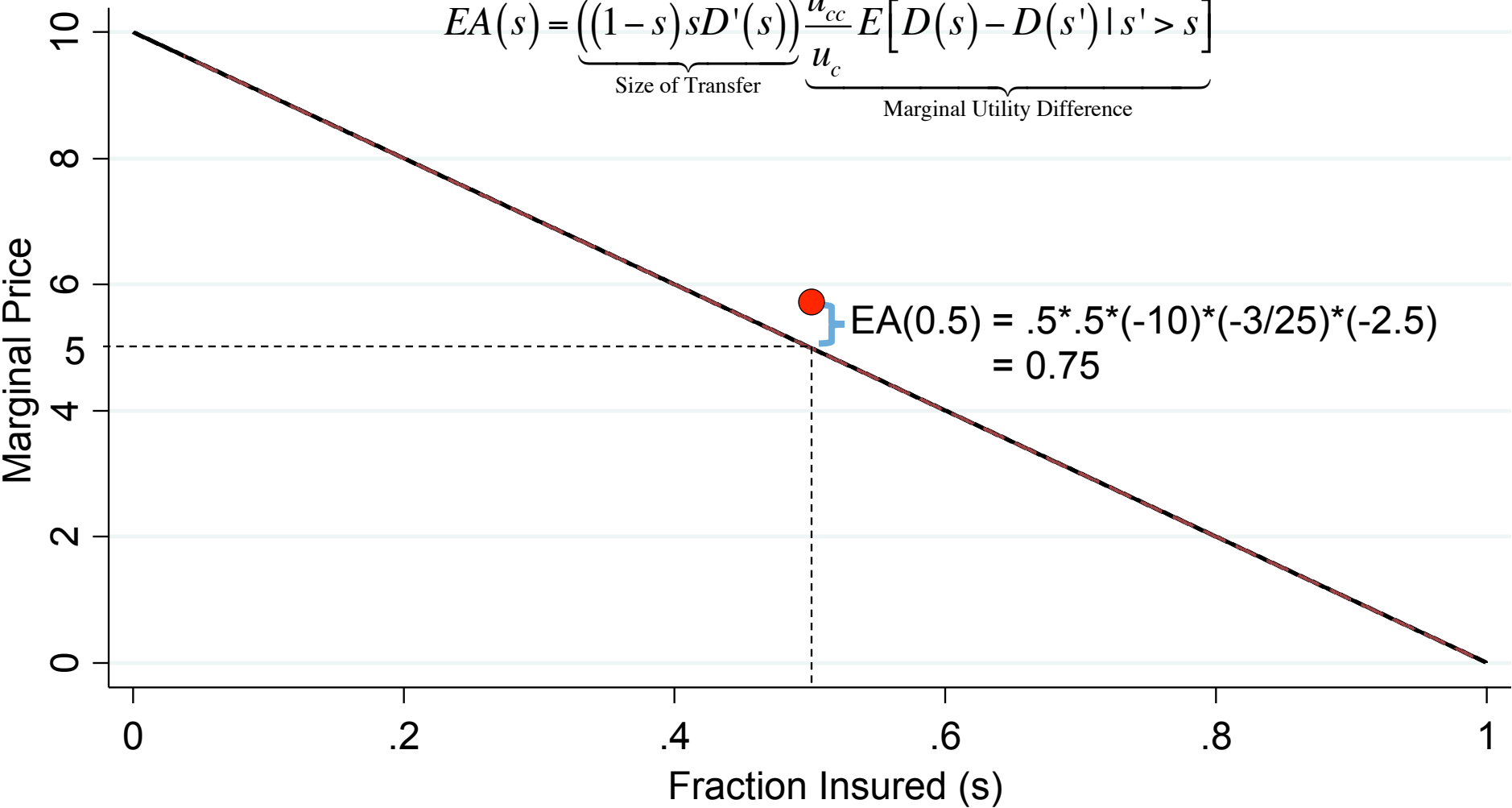


— Demand

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand

$$EA(s) = \underbrace{\left((1-s)sD'(s) \right)}_{\text{Size of Transfer}} \underbrace{\frac{u_{cc}}{u_c} E[D(s) - D(s') | s' > s]}_{\text{Marginal Utility Difference}}$$



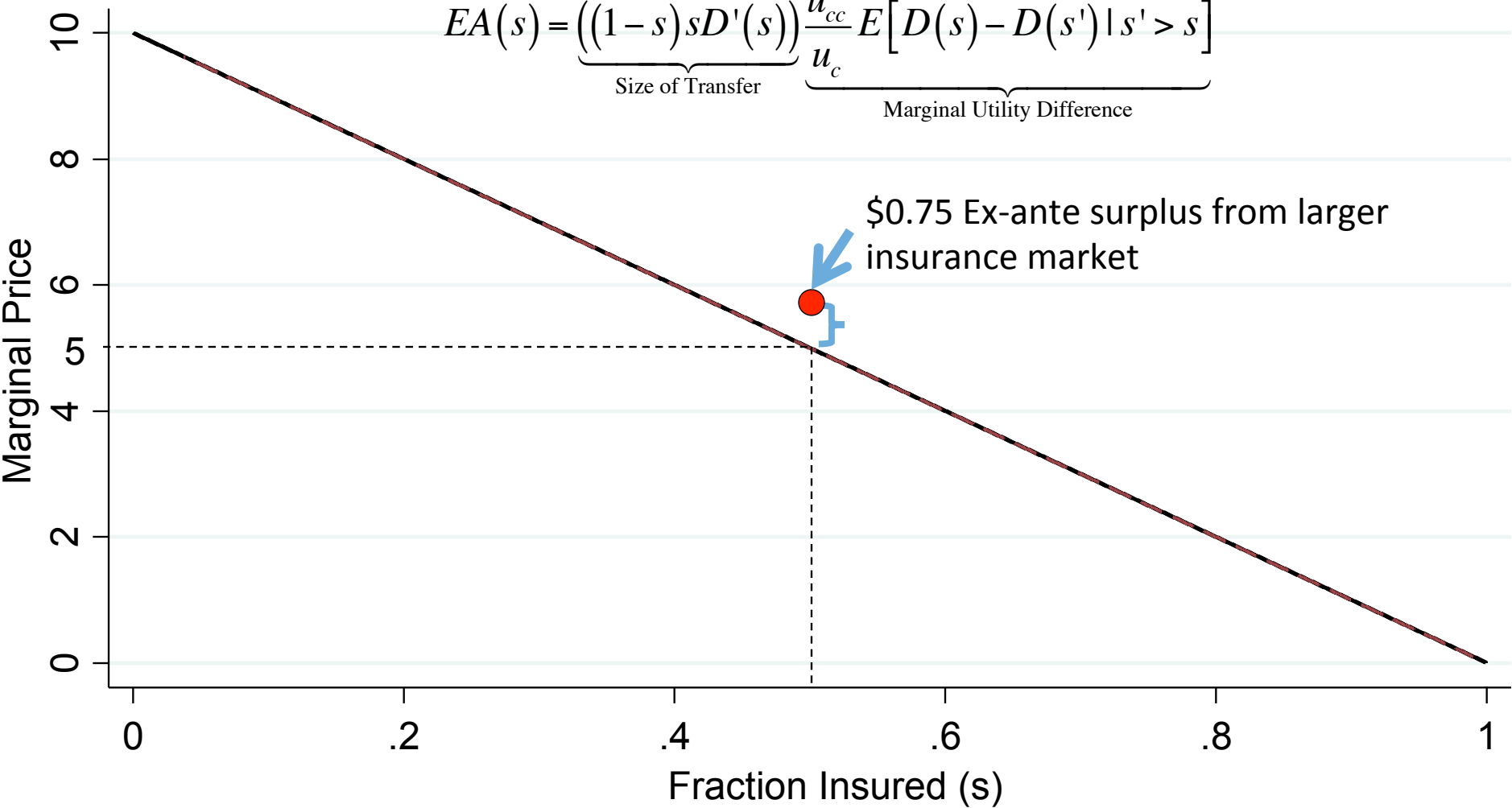
$$EA(0.5) = .5 * .5 * (-10) * (-3/25) * (-2.5) = 0.75$$

— Demand

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand

$$EA(s) = \underbrace{\left((1-s)sD'(s) \right)}_{\text{Size of Transfer}} \underbrace{\frac{u_{cc}}{u_c} E[D(s) - D(s') | s' > s]}_{\text{Marginal Utility Difference}}$$

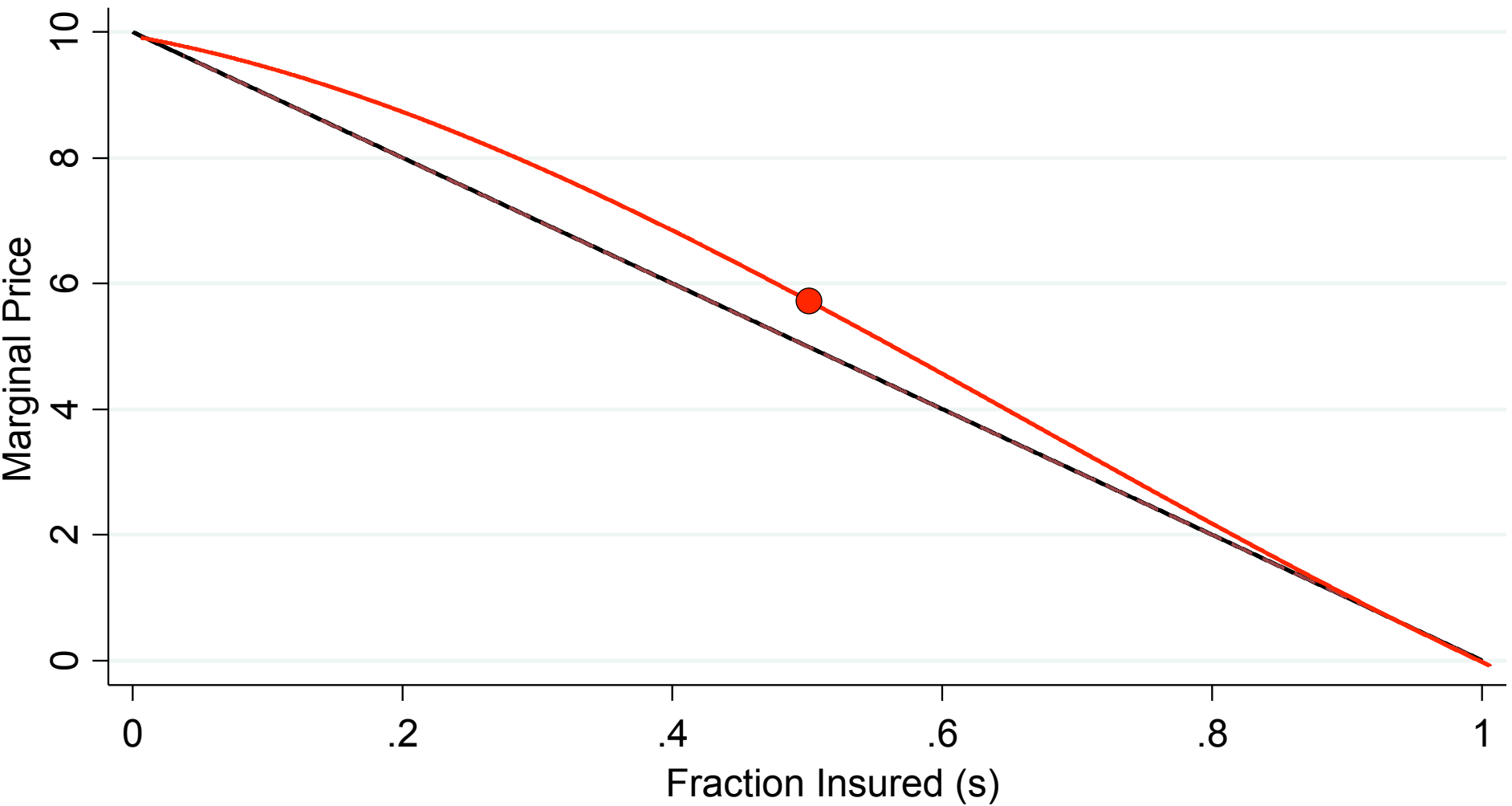


\$0.75 Ex-ante surplus from larger insurance market

— Demand

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand

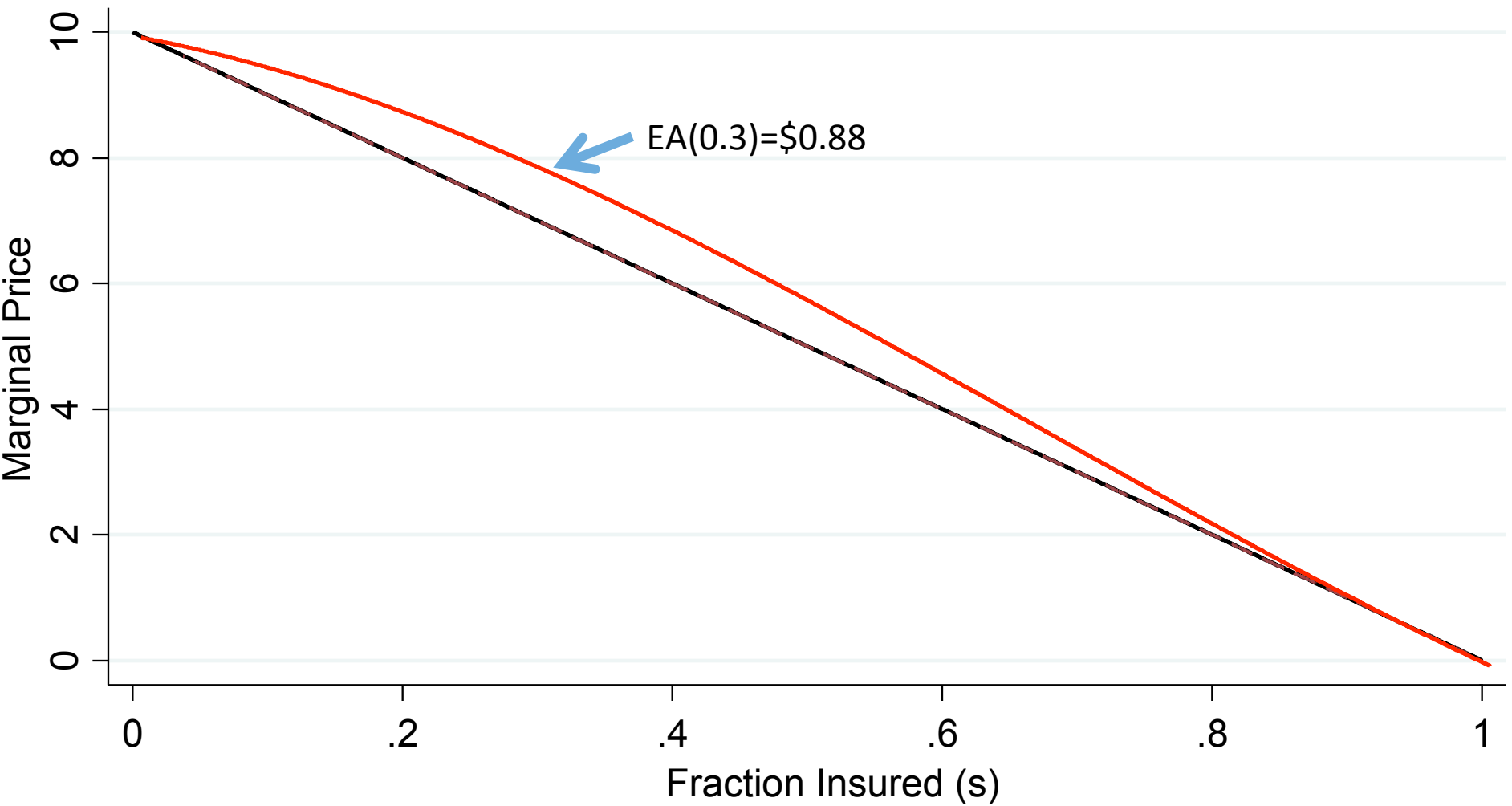


— Demand

— 'Ex-ante' Demand, $D(s)+EA(s)$

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand

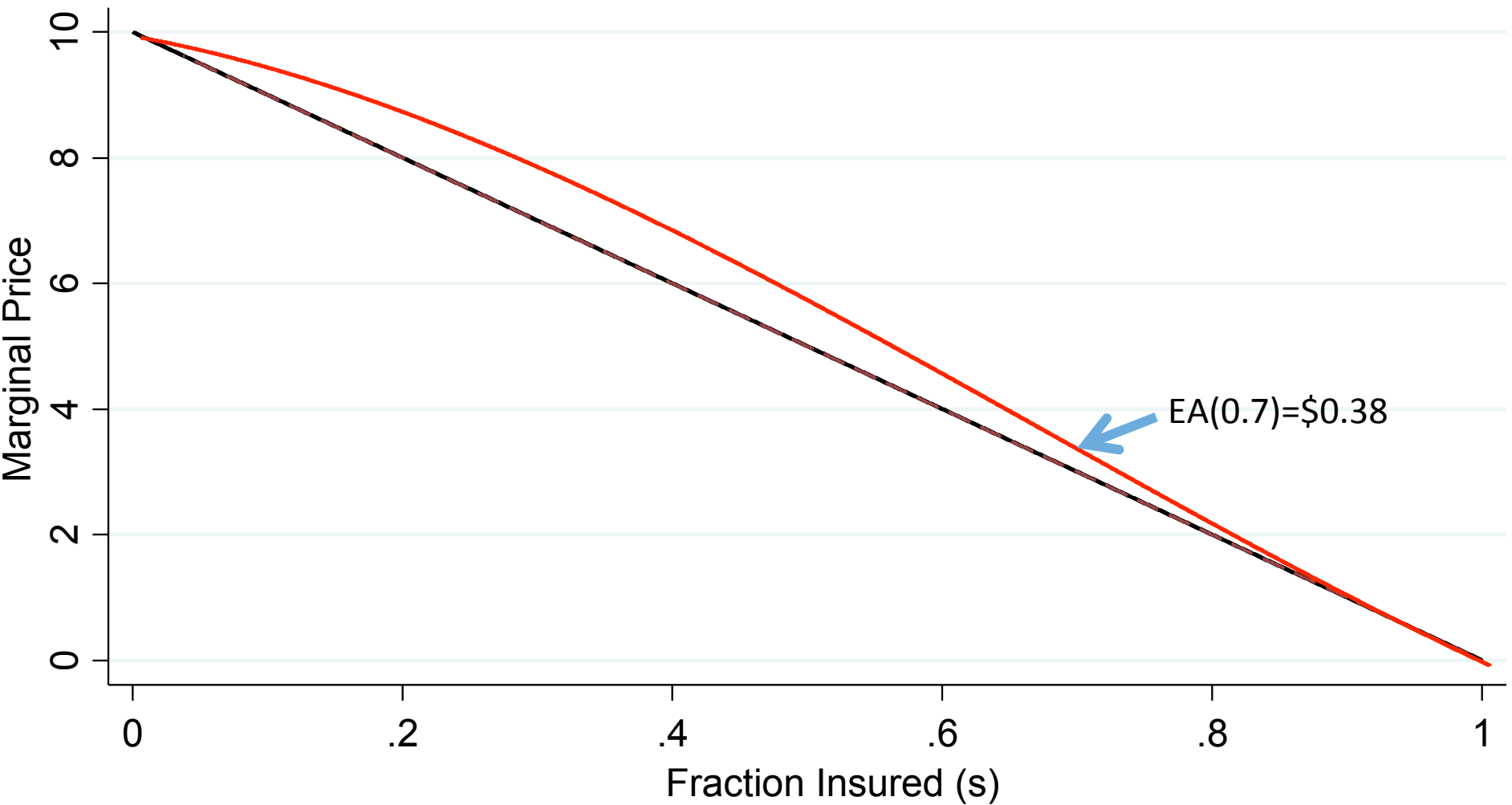


— Demand

- - - Marginal Cost

— 'Ex-ante' Demand, $D(s)+EA(s)$

From Observed Demand to Ex-Ante Demand

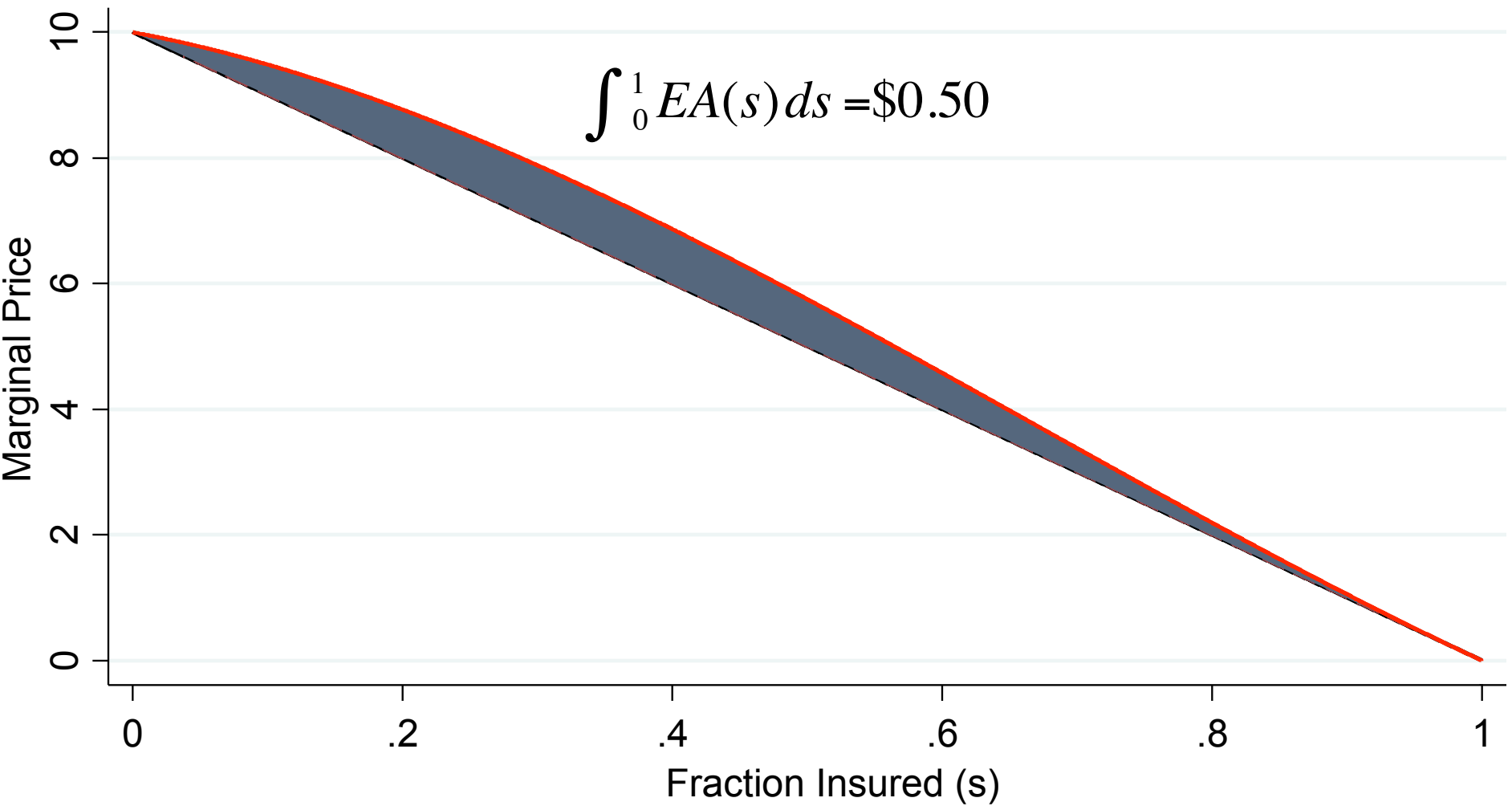


— Demand

- - - Marginal Cost

— 'Ex-ante' Demand, $D(s)+EA(s)$

From Observed Demand to Ex-Ante Demand

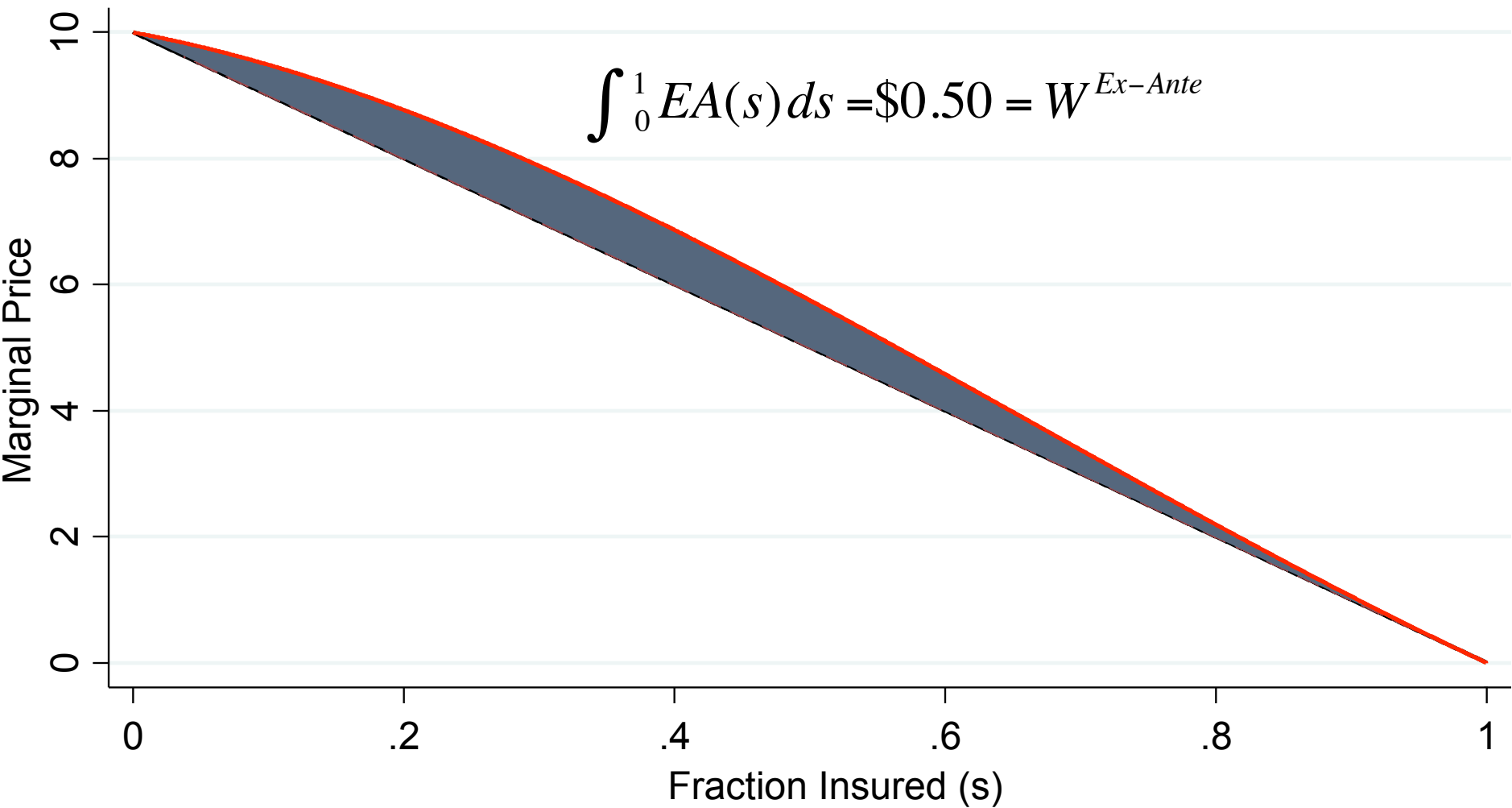


— Demand

— 'Ex-ante' Demand, $D(s)+EA(s)$

- - - Marginal Cost

From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

— 'Ex-ante' Demand, D(s)+EA(s)

DWL versus Ex-Ante WTP

- Ex-ante demand curve facilitates ex-ante/utilitarian welfare analysis
 - Even though demand is measured after information is revealed
- Ex-ante (ex-post utilitarian) surplus can lead to different conclusions about the value of insurance
 - Ex-ante efficient to have full insurance
 - No value to insurance market after info is revealed
 - (Strictly positive DWL if there was moral hazard)

Outline

- Simple Example
- General Model
- Illustration with Optimal Health Insurance
- Optimal open enrollment periods

Outline

- Simple Example
- General Model
- Illustration with Optimal Health Insurance
- Optimal open enrollment periods

General Model

- Goal: Nest demand and cost curves into general utility setup
- Use underlying utility function structure to derive sufficient statistics to measure ex-ante/utilitarian value of insurance
- Use language of health insurance
 - Paper illustrates how to nest into other settings (e.g. UI)

General Model

- Individuals choose consumption, c , and medical spending, m
 - Face (health) shock, θ
 - Income, y (potentially dependent on θ)
 - Utility $u(c, m; \theta)$
- Insurance product allows payment of $x(m)$ instead of m
 - Prices p_I and p_U of being insured and uninsured s.t. resource constraint
 - Learn signal about θ at time of measuring demand
 - Let s denote fraction purchasing insurance
 - Fraction insured solves: $D(s) = p_I - p_U$
- Average Cost: $AC(s) = E[m(s'; \theta) - x(m(s'; \theta)) | s' \geq s = D^{-1}(p_I - p_U)]$
- Marginal Cost: $MC(s) = \frac{d}{ds} [sAC(s)] = AC(s) + sAC'(s)$

General Model

- Ex-ante/Utilitarian welfare when fraction s has insurance

$$W(s) = E[u(c(s; \theta), m(s; \theta); \theta)]$$

General Model

- Ex-ante/Utilitarian welfare when fraction s has insurance

$$W(s) = E[u(c(s; \theta), m(s; \theta); \theta)]$$

- Ex-ante WTP for larger insurance market:

$$\frac{W'(s)}{E[u' | Insured]} = \underbrace{D(s) - MC(s)}_{\text{Ex-Post Surplus}} + EA(s)$$

where

$$EA(s) = \underbrace{(1-s) \left(MDWL(s) - s \frac{\partial D}{\partial s} \right)}_{\text{Size of Transfer}} \underbrace{\frac{E[u'(s) | Insured] - E[u'(s) | Uninsured]}{E[u'(s) | Insured]}}_{\text{Marginal Utility Difference}}$$

- Adjust size of transfer for $MDWL = MC(s) - D(s)$

Implementation

- Use common assumptions to approximate difference in marginal utilities between insured and uninsured
 - State independence: u_c only depends on c
 - Income doesn't vary with s
 - Common risk aversion (Andrews and Miller, 2013)

- Implies:

$$EA(s) = (1-s) \underbrace{\left(MDWL(s) - s \frac{\partial D}{\partial s} \right)}_{\text{Size of Transfer}} \underbrace{\left(\frac{-u_{cc}}{u_c} \right) E[D(s) - D(s') | s' > s]}_{\text{Marginal Utility Difference}}$$

- Ex-ante component increasing with the square of demand/cost
 - $D(s) \rightarrow aD(s)$ implies $EA(s) \rightarrow a^2 EA(s)$

Risk Aversion

- Measuring ex-ante demand requires risk aversion
- Can be assumed externally
 - CRRA = 3
 - CARA = 5×10^{-4}
- Or can be estimated internally

$$\frac{-u_{cc}}{u_c} \approx 2 \frac{\text{Markup}}{\text{Variance Reduction}} \approx 2 \frac{D(s) - MC(s)}{\text{var}(m^U) - \text{var}(x^I)}$$

- WTP for insurance against remaining risk reveals can proxy for WTP for insurance against realized risk

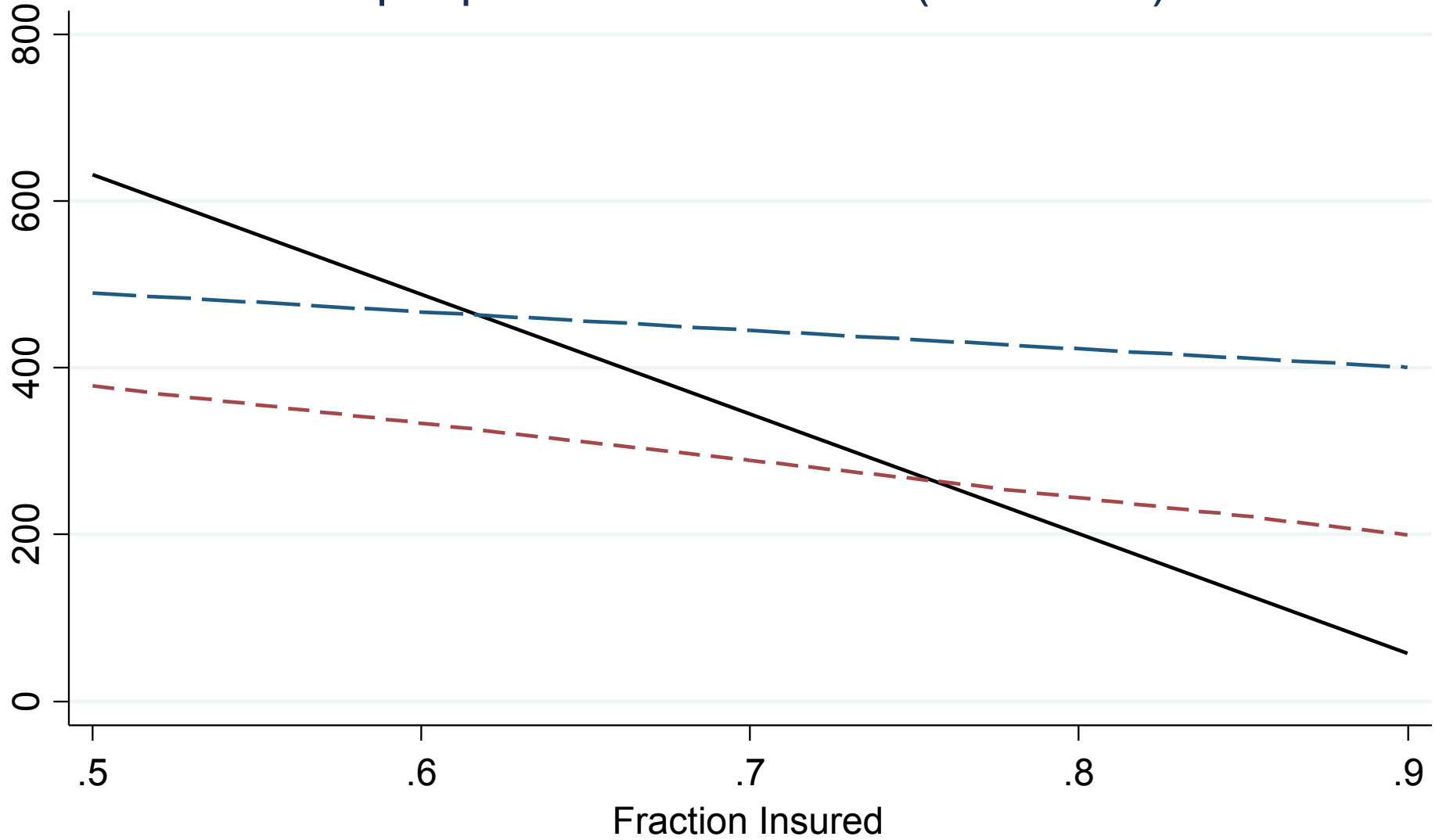
Outline

- Simple Example
- General Model
- Illustration with Optimal Health Insurance
- Optimal open enrollment periods

Illustration with Three Health Insurance Examples

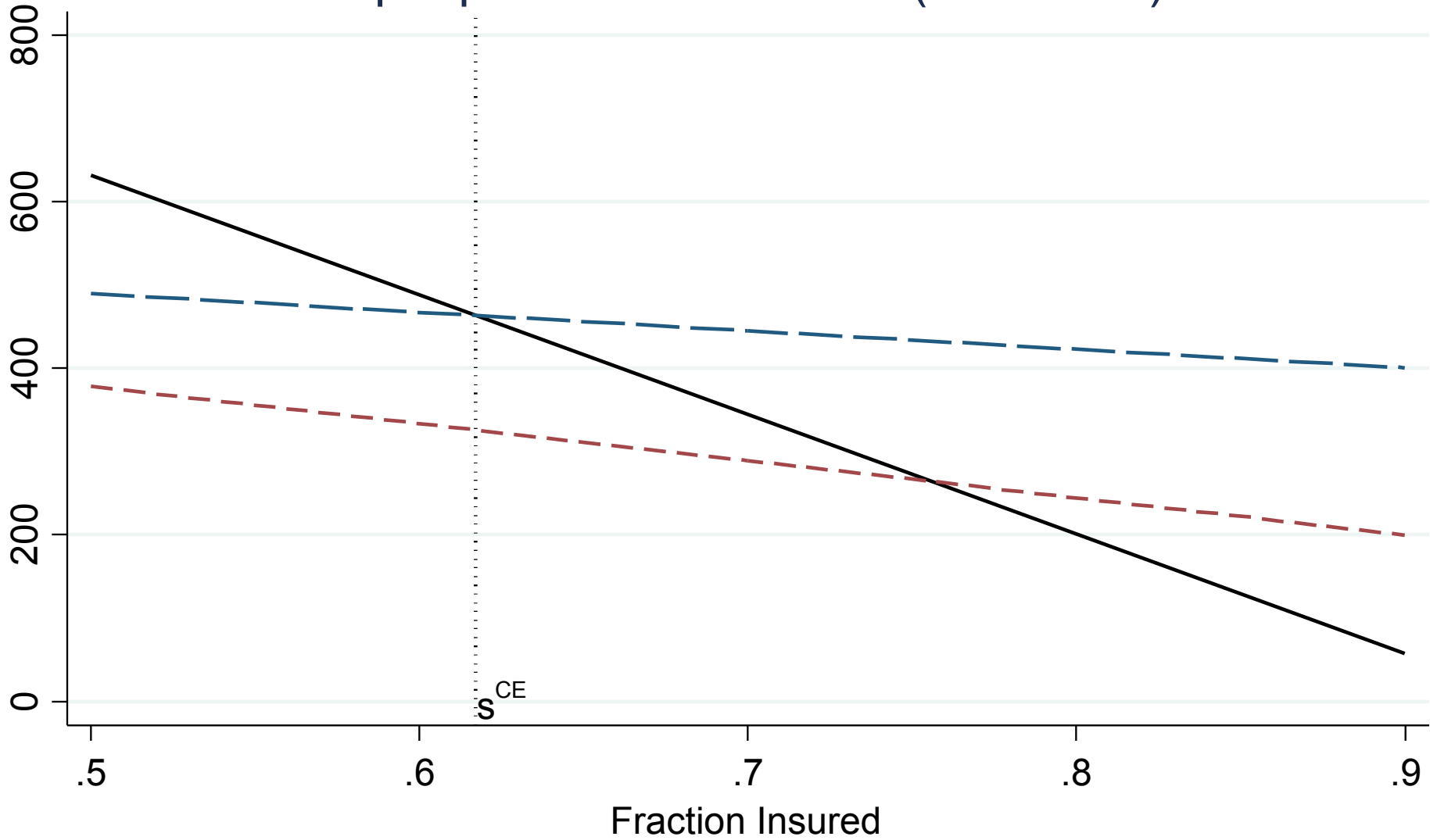
1. Top-up market for more generous PPO coverage in Alcoa
 - Demand and Cost Curves from Einav, Finkelstein, and Cullen (2010)
 - Average annual cost: \$500
 2. “Medium risk”
 - 4x Demand and Cost curves from Einav, Finkelstein, and Cullen (2010)
 - Average annual cost: \$2,000
 3. “Large Risk”: Conservative approx. to insured vs. uninsured
 - 8x Demand and Cost curves from Einav, Finkelstein, and Cullen (2010)
 - Average annual cost: \$4,000
 - Smaller than \$5,922 (full vs. no insurance) or \$5,270 in MA (Hackman, Kolstad, Kowalski, 2015)
- Briefly: hypothetical market for UI from Hendren (2016)

Top-Up Health Insurance (EFC2010)



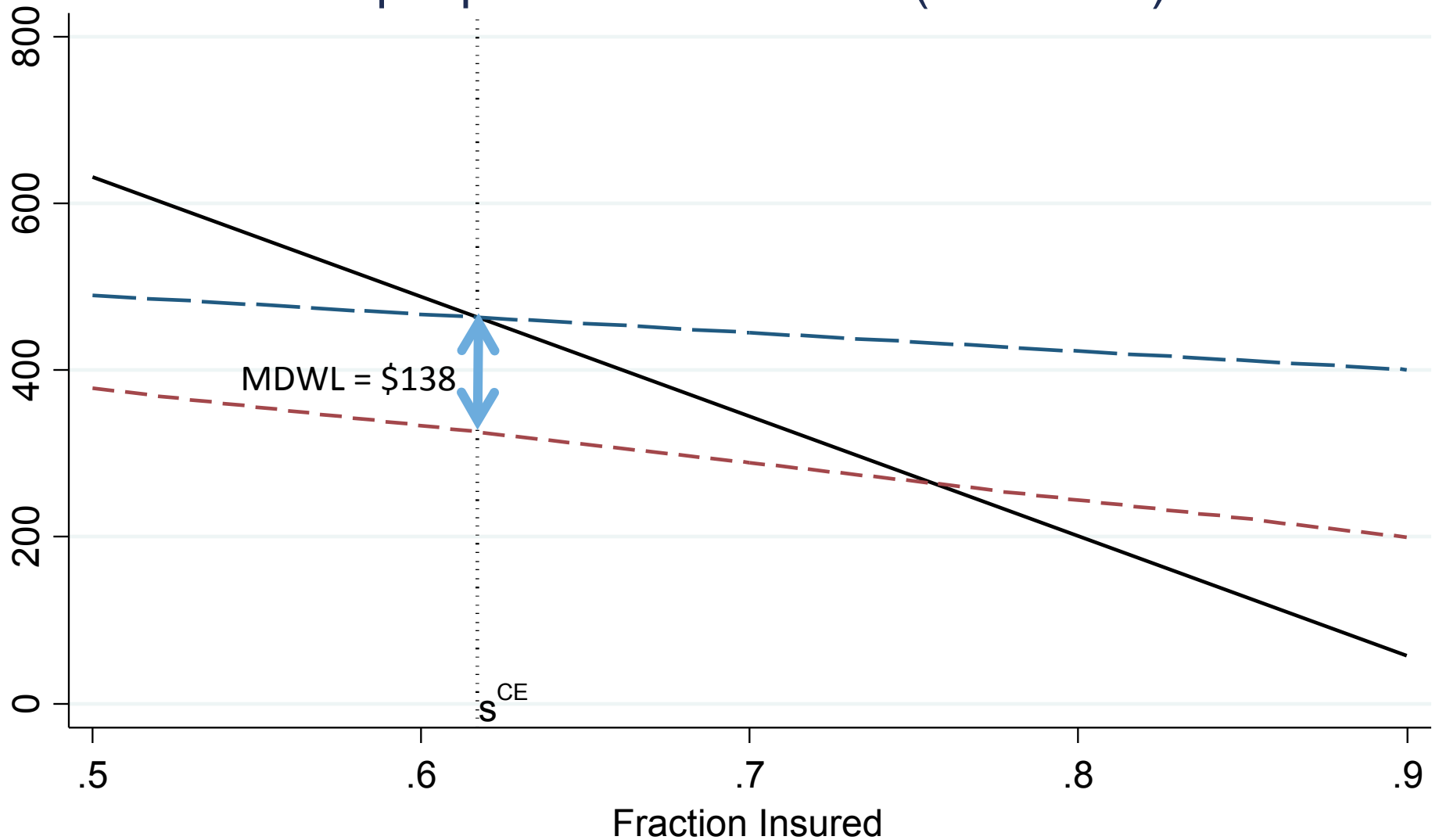
— Demand
- - - Average Cost
- - - Marginal Cost

Top-Up Health Insurance (EFC2010)



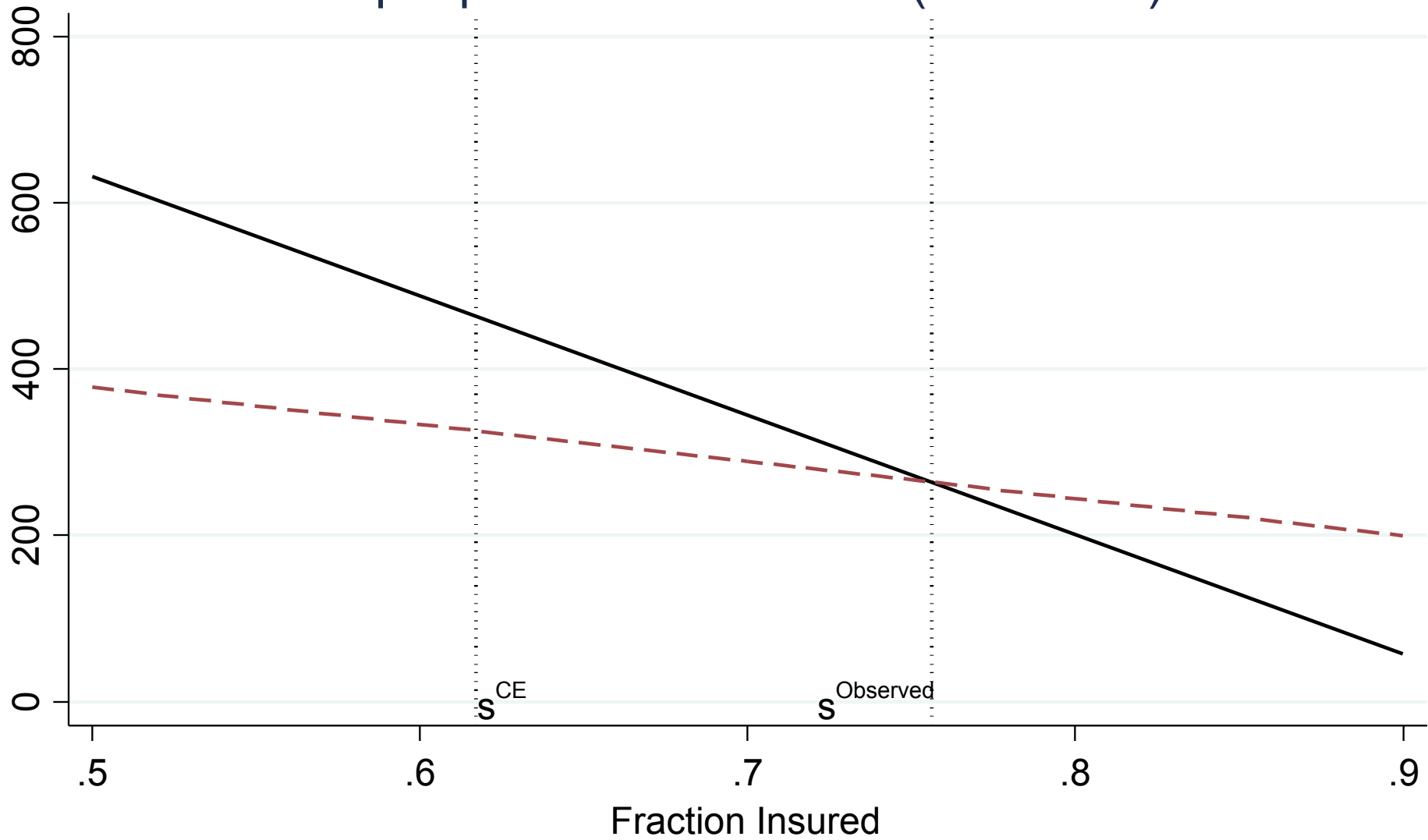
— Demand - - - Marginal Cost
- - - Average Cost

Top-Up Health Insurance (EFC2010)



— Demand - - - Marginal Cost
- - - Average Cost

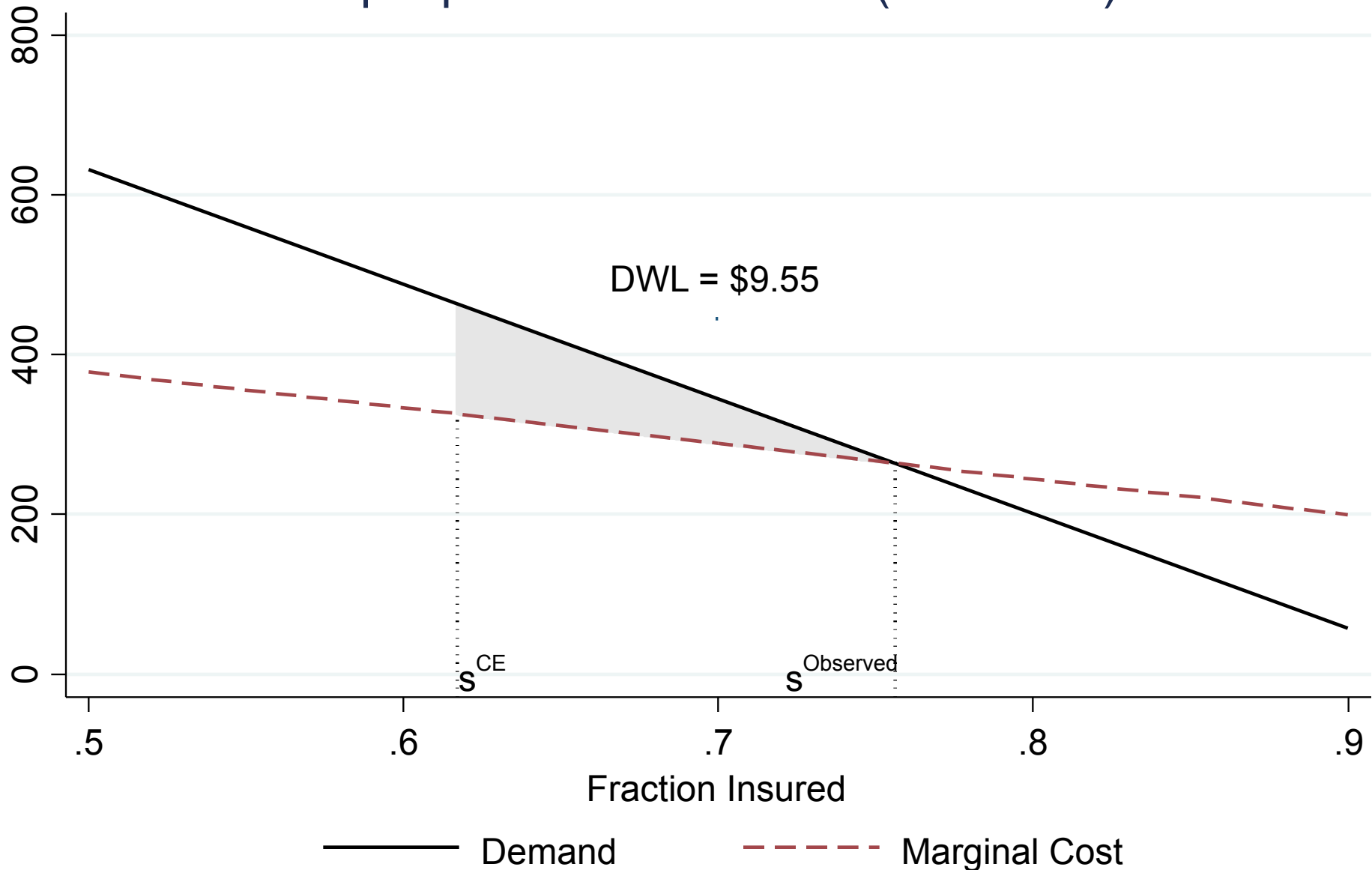
Top-Up Health Insurance (EFC2010)



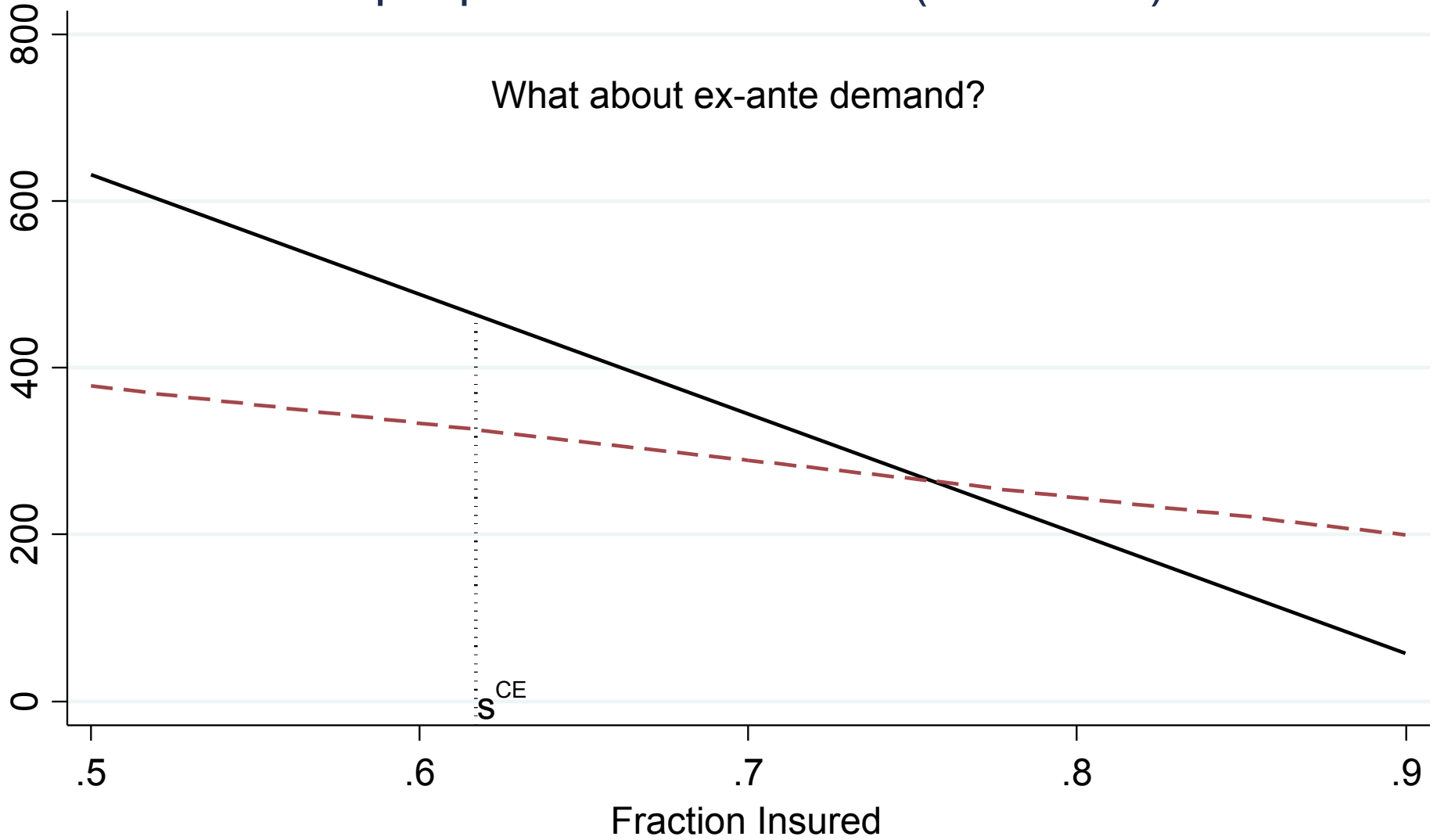
— Demand

- - - Marginal Cost

Top-Up Health Insurance (EFC2010)



Top-Up Health Insurance (EFC2010)

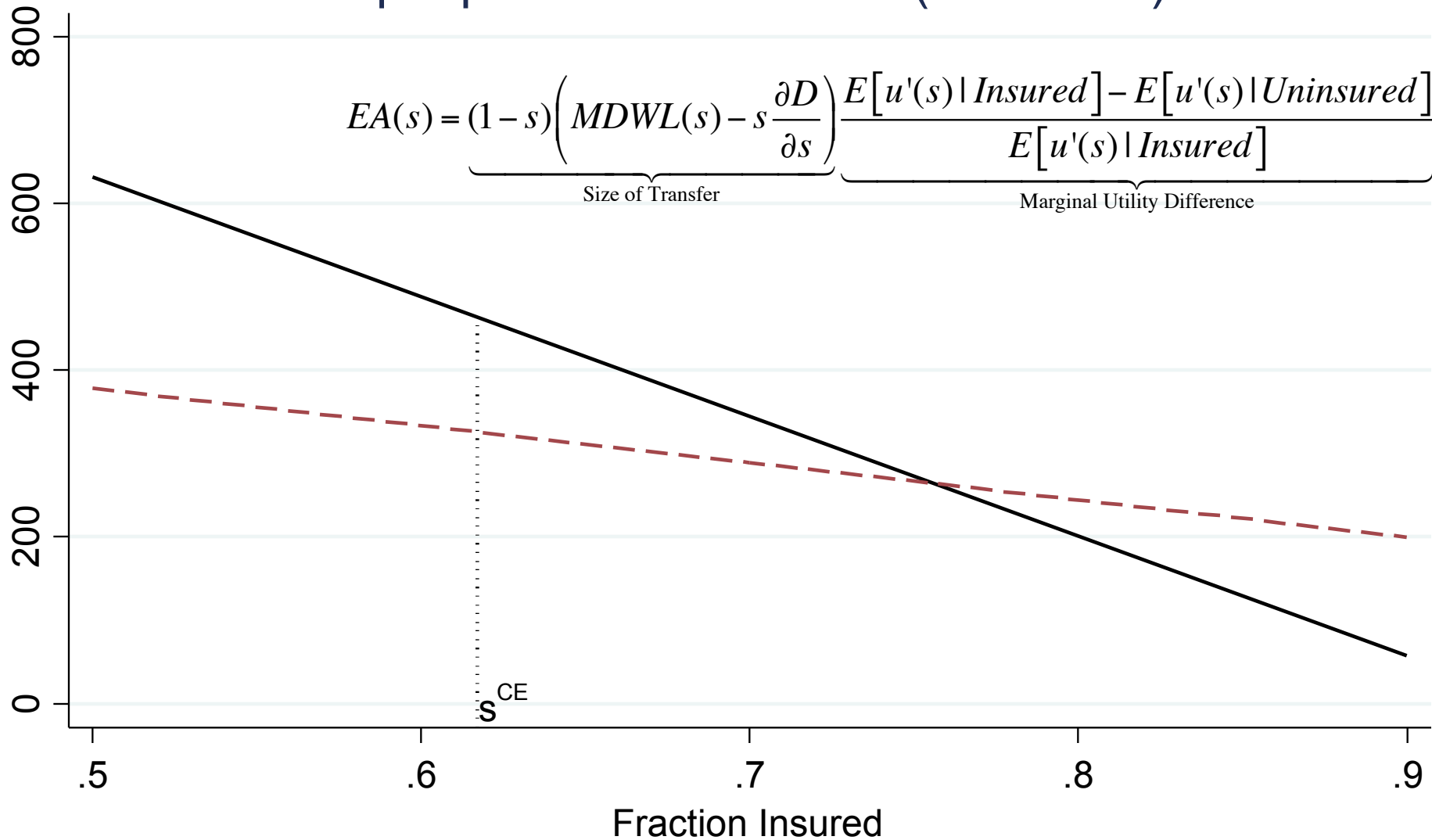


— Demand

- - - Marginal Cost

Top-Up Health Insurance (EFC2010)

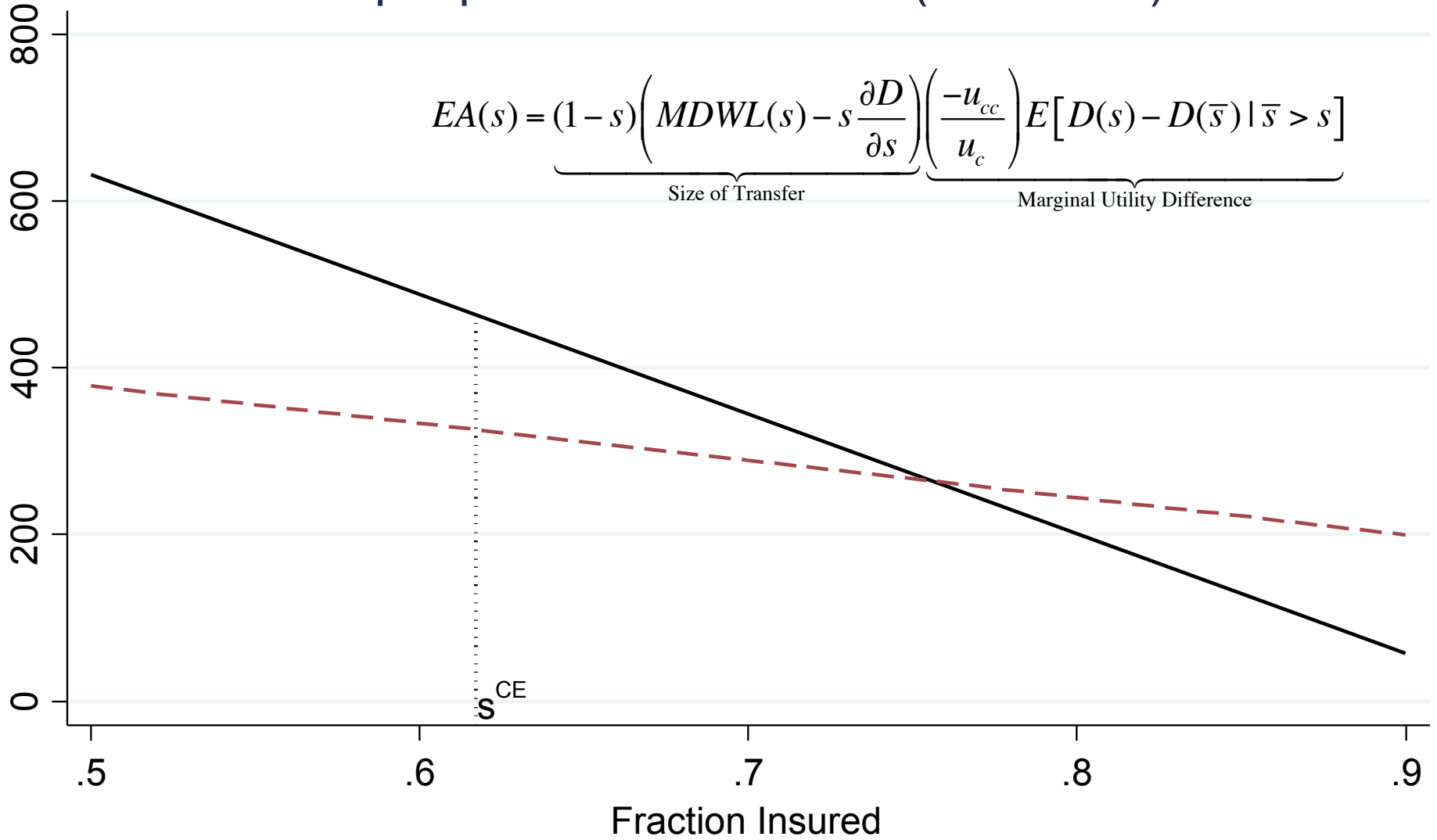
$$EA(s) = \underbrace{(1-s) \left(MDWL(s) - s \frac{\partial D}{\partial s} \right)}_{\text{Size of Transfer}} \underbrace{\frac{E[u'(s) | Insured] - E[u'(s) | Uninsured]}{E[u'(s) | Insured]}}_{\text{Marginal Utility Difference}}$$



— Demand

- - - Marginal Cost

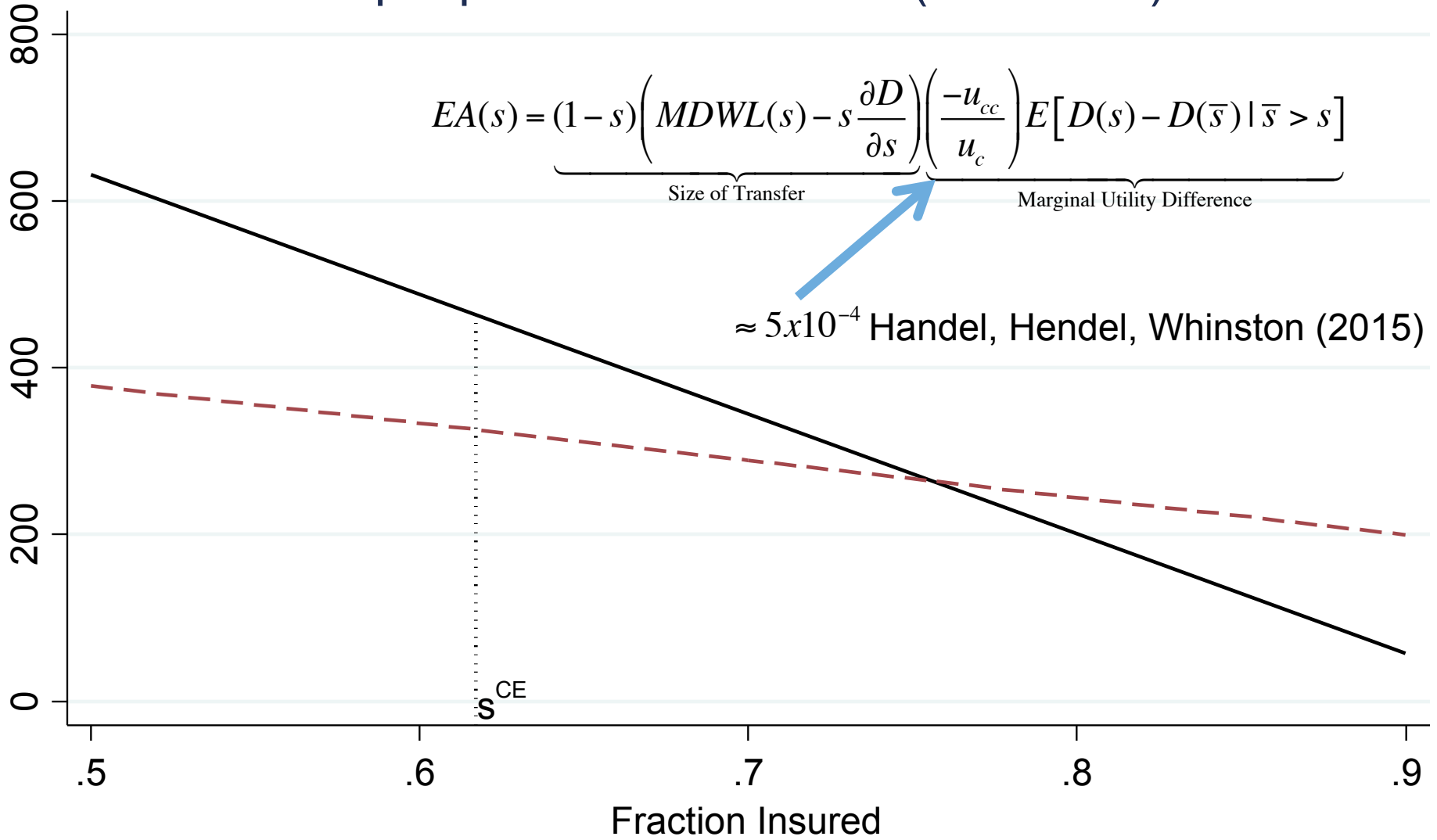
Top-Up Health Insurance (EFC2010)



$$EA(s) = \underbrace{(1-s) \left(MDWL(s) - s \frac{\partial D}{\partial s} \right)}_{\text{Size of Transfer}} \underbrace{\left(\frac{-u_{cc}}{u_c} \right) E[D(s) - D(\bar{s}) | \bar{s} > s]}_{\text{Marginal Utility Difference}}$$

— Demand - - - Marginal Cost

Top-Up Health Insurance (EFC2010)



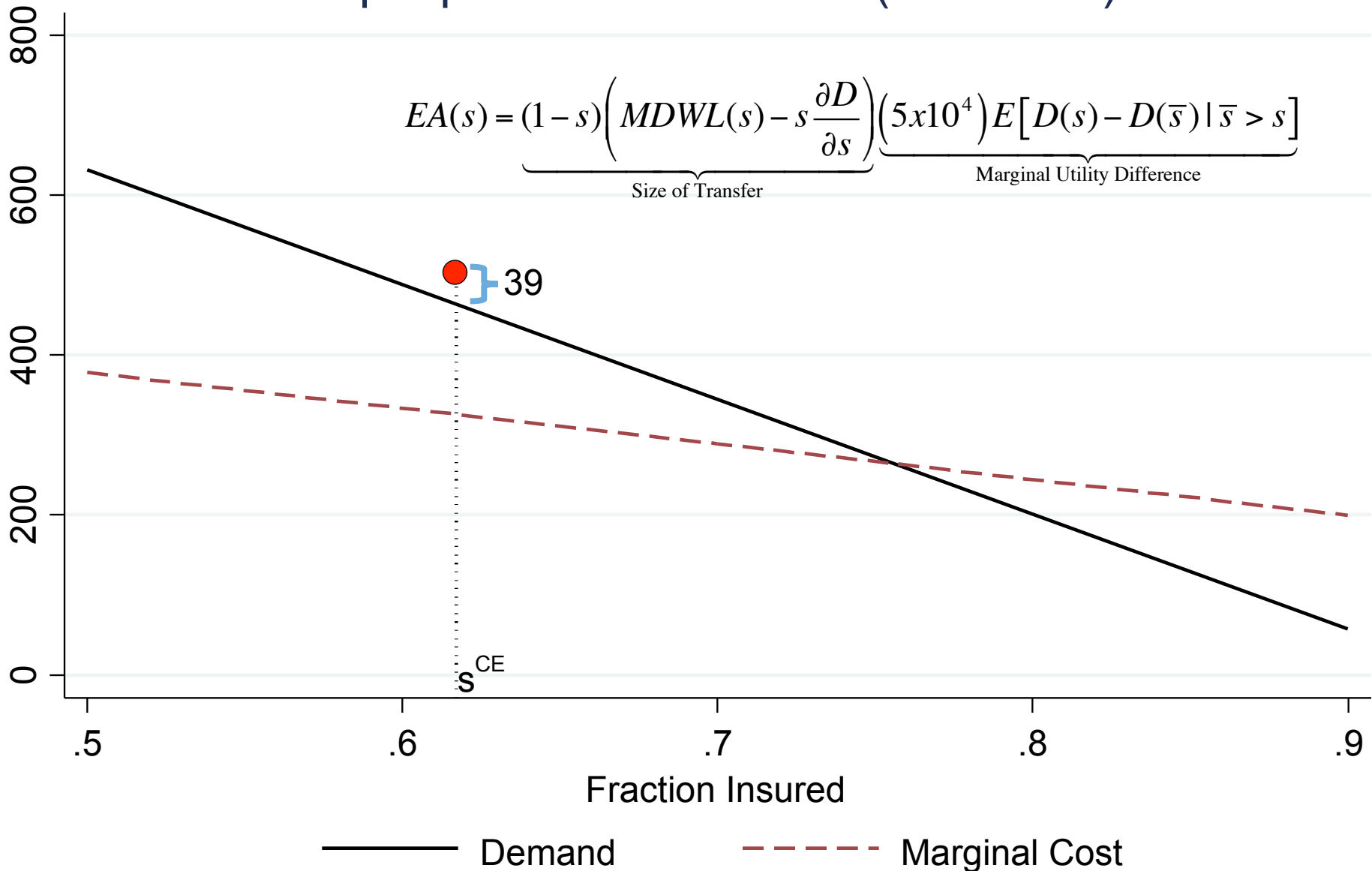
$$EA(s) = (1-s) \underbrace{\left(MDWL(s) - s \frac{\partial D}{\partial s} \right)}_{\text{Size of Transfer}} \underbrace{\left(\frac{-u_{cc}}{u_c} \right) E[D(s) - D(\bar{s}) | \bar{s} > s]}_{\text{Marginal Utility Difference}}$$

$\approx 5 \times 10^{-4}$ Handel, Hendel, Whinston (2015)

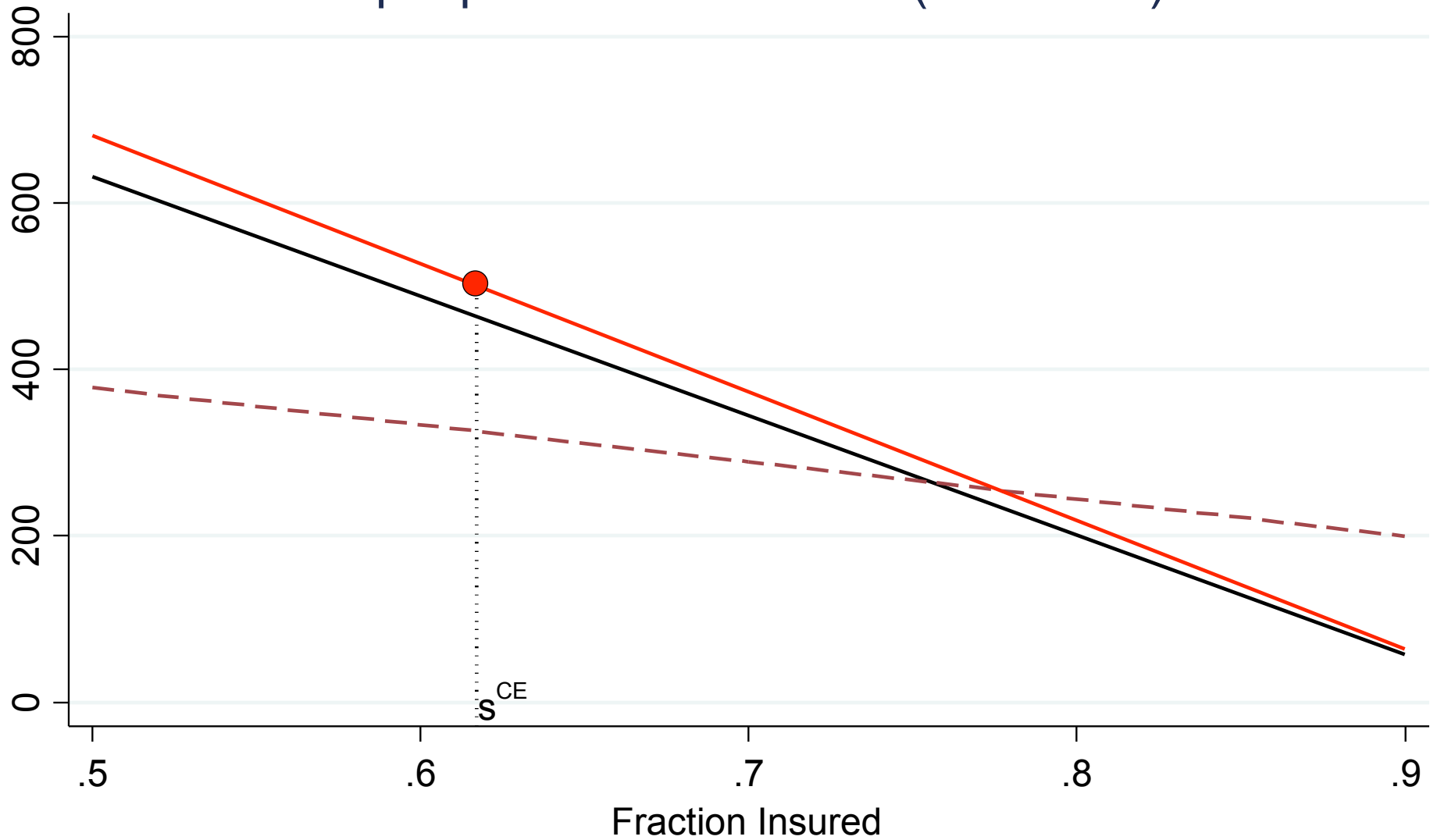
— Demand

- - - Marginal Cost

Top-Up Health Insurance (EFC2010)

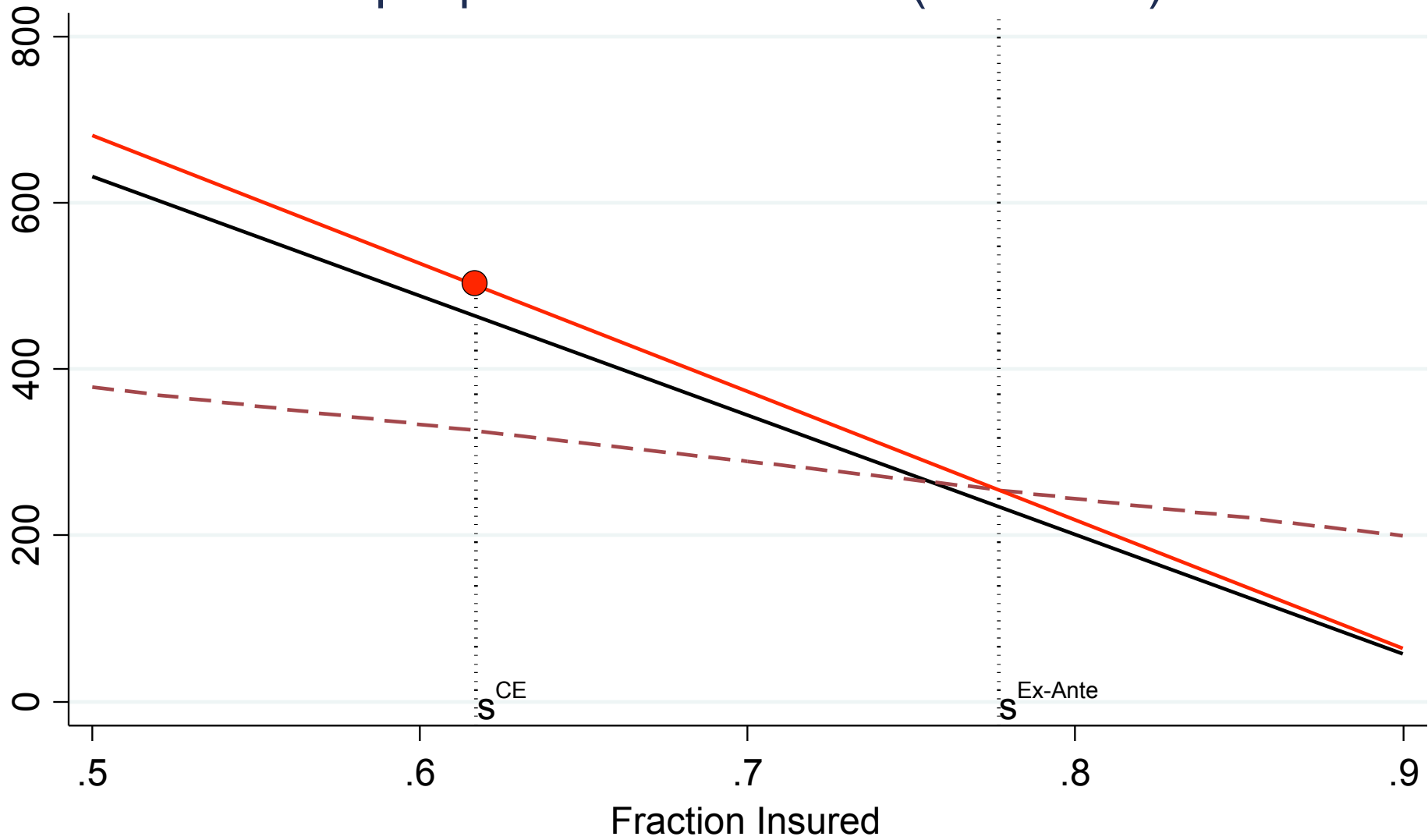


Top-Up Health Insurance (EFC2010)



— Demand - - - Marginal Cost
— 'Ex-ante' Demand

Top-Up Health Insurance (EFC2010)



— Demand - - - Marginal Cost
— 'Ex-ante' Demand

Ex-Ante Optimal Insurance Markets Generate DWL

- Ex-ante optimal size of the insurance market solves:

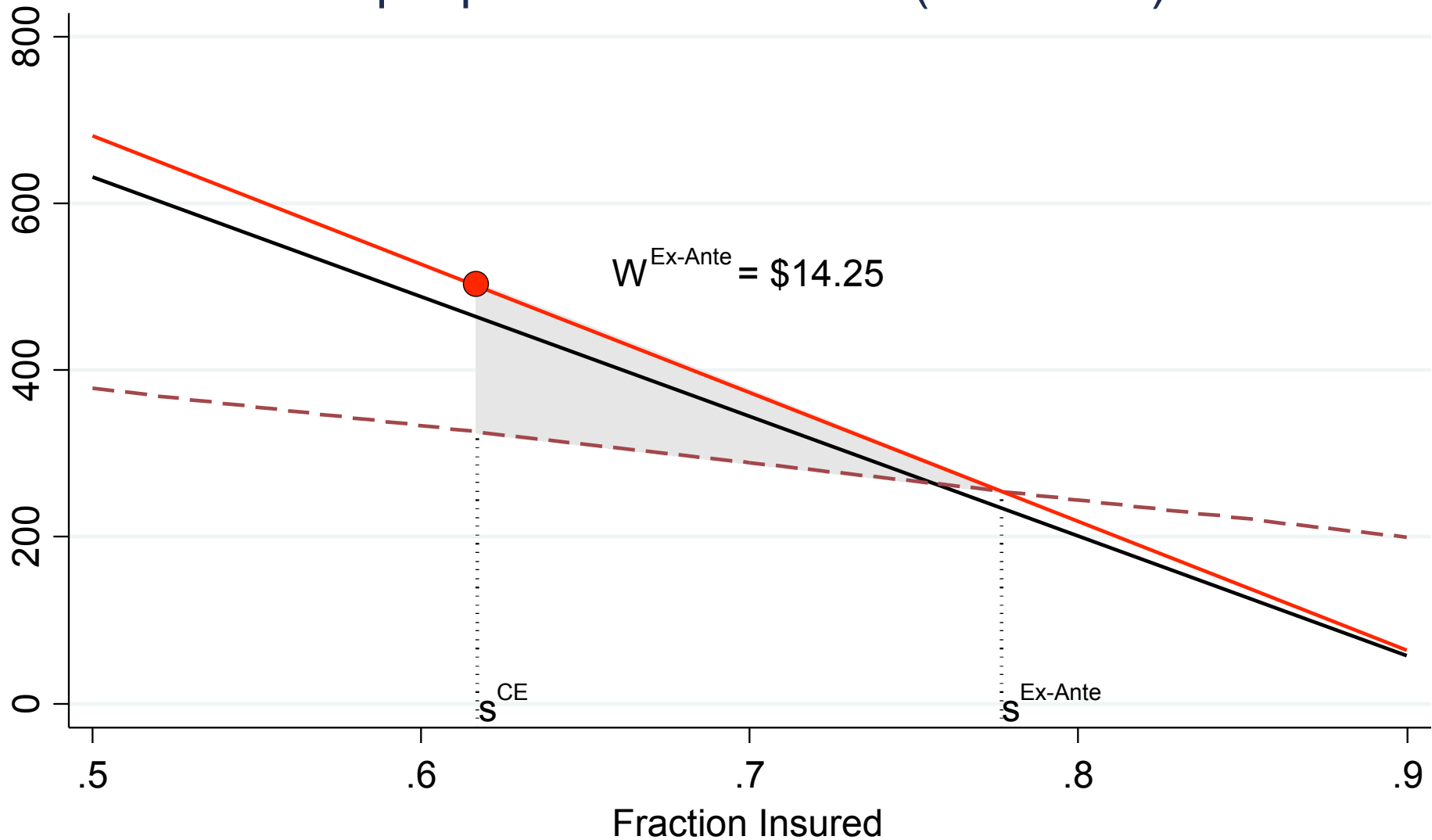
$$\frac{W'(s^{Ex-Ante})}{E[u' | Insured]} = \underbrace{D(s^{Ex-Ante}) - MC(s^{Ex-Ante})}_{\text{Ex-Post Surplus}} + EA(s^{Ex-Ante}) = 0$$

- Yields a “Baily-Chetty” condition:

$$EA(s^{Ex-Ante}) = MDWL(s^{Ex-Ante})$$

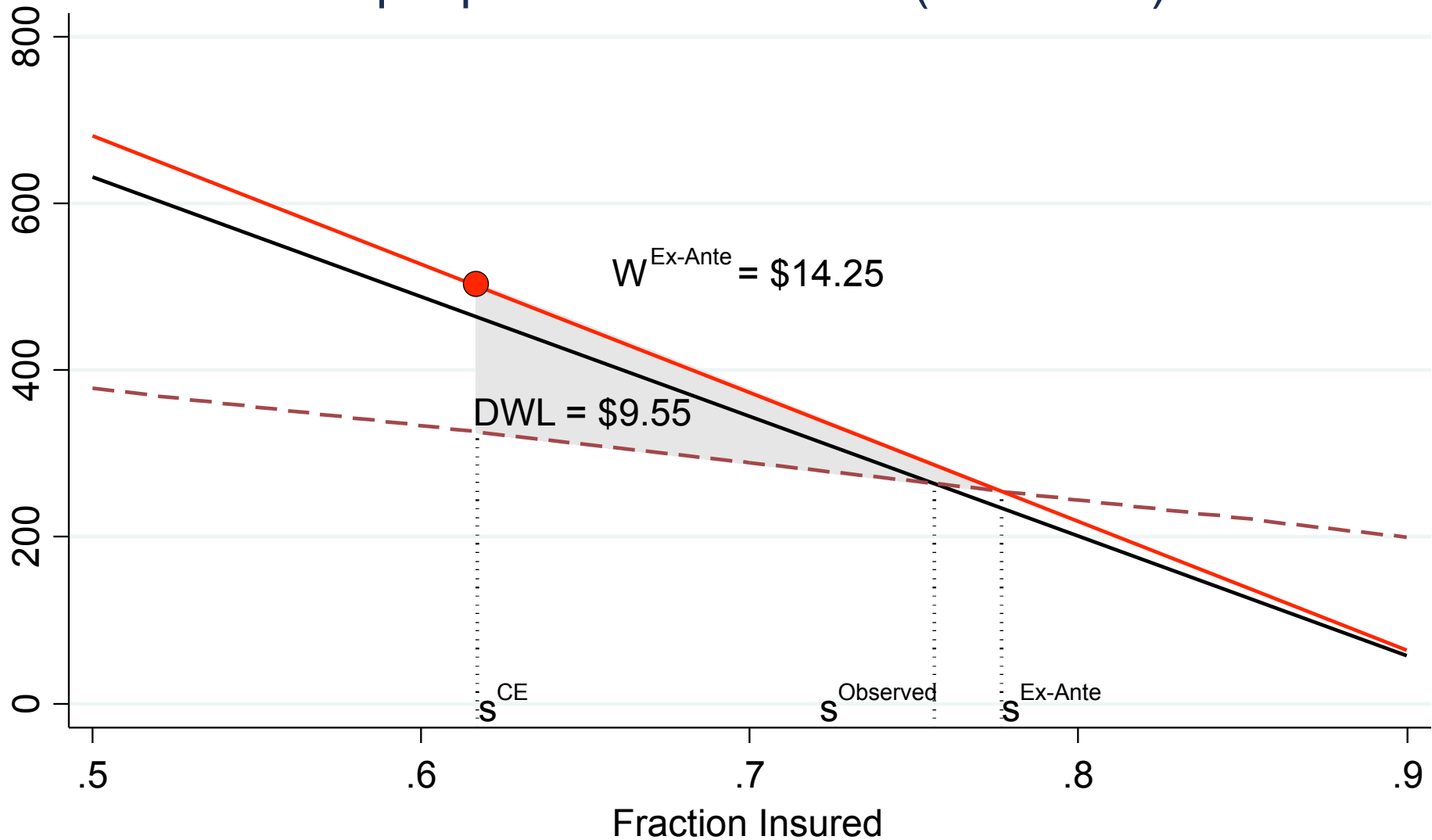
- **Corollary:** The ex-ante optimal allocation generally involves (ex-post) deadweight loss
 - Easy to show that $MDWL(s)=0$ implies $EA(s)>0$ whenever marginal utilities are higher for the insured than uninsured
 - MDWL is a cost we’re willing to accept for ex-ante insurance

Top-Up Health Insurance (EFC2010)



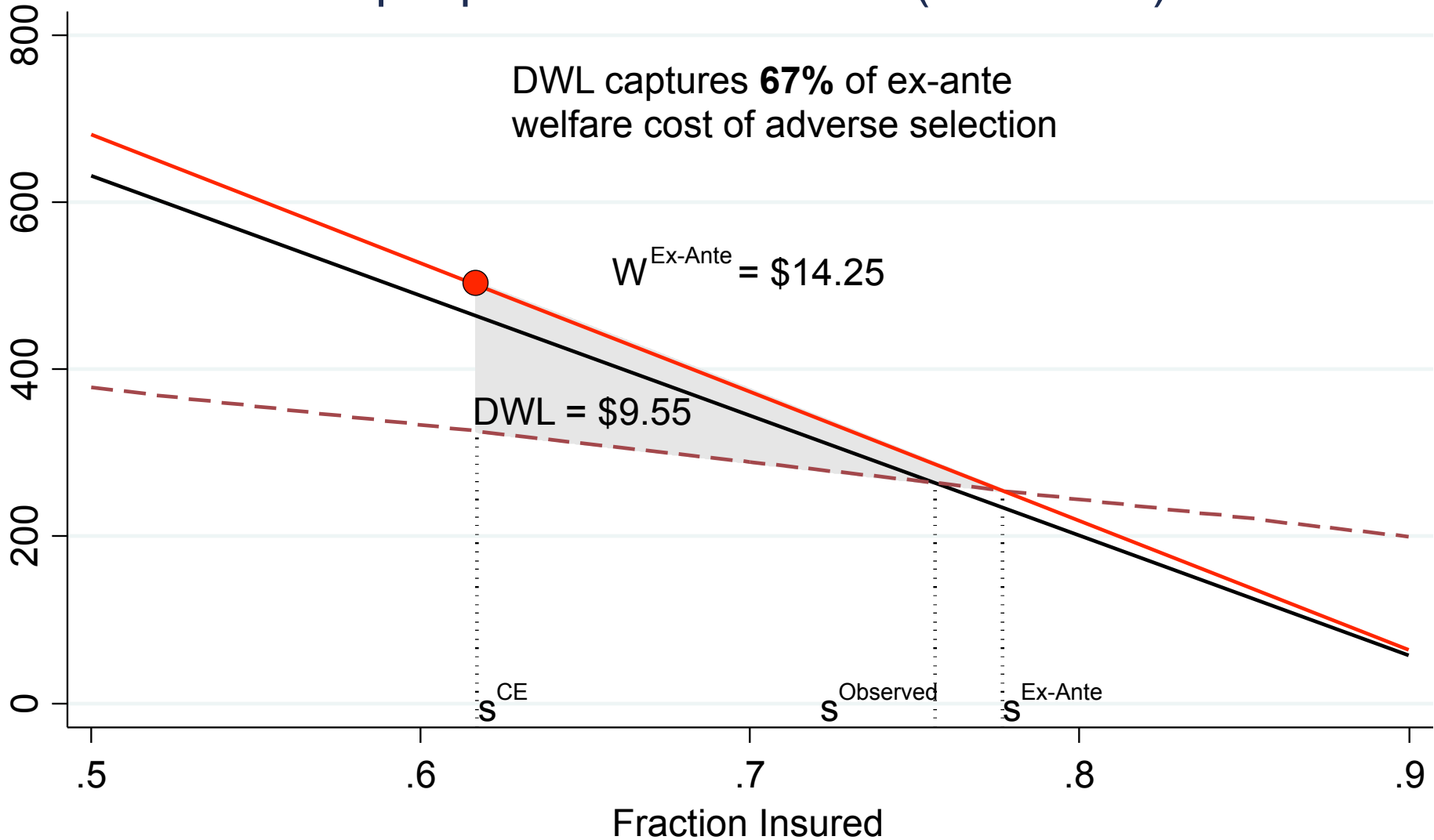
— Demand - - - Marginal Cost
— 'Ex-ante' Demand

Top-Up Health Insurance (EFC2010)



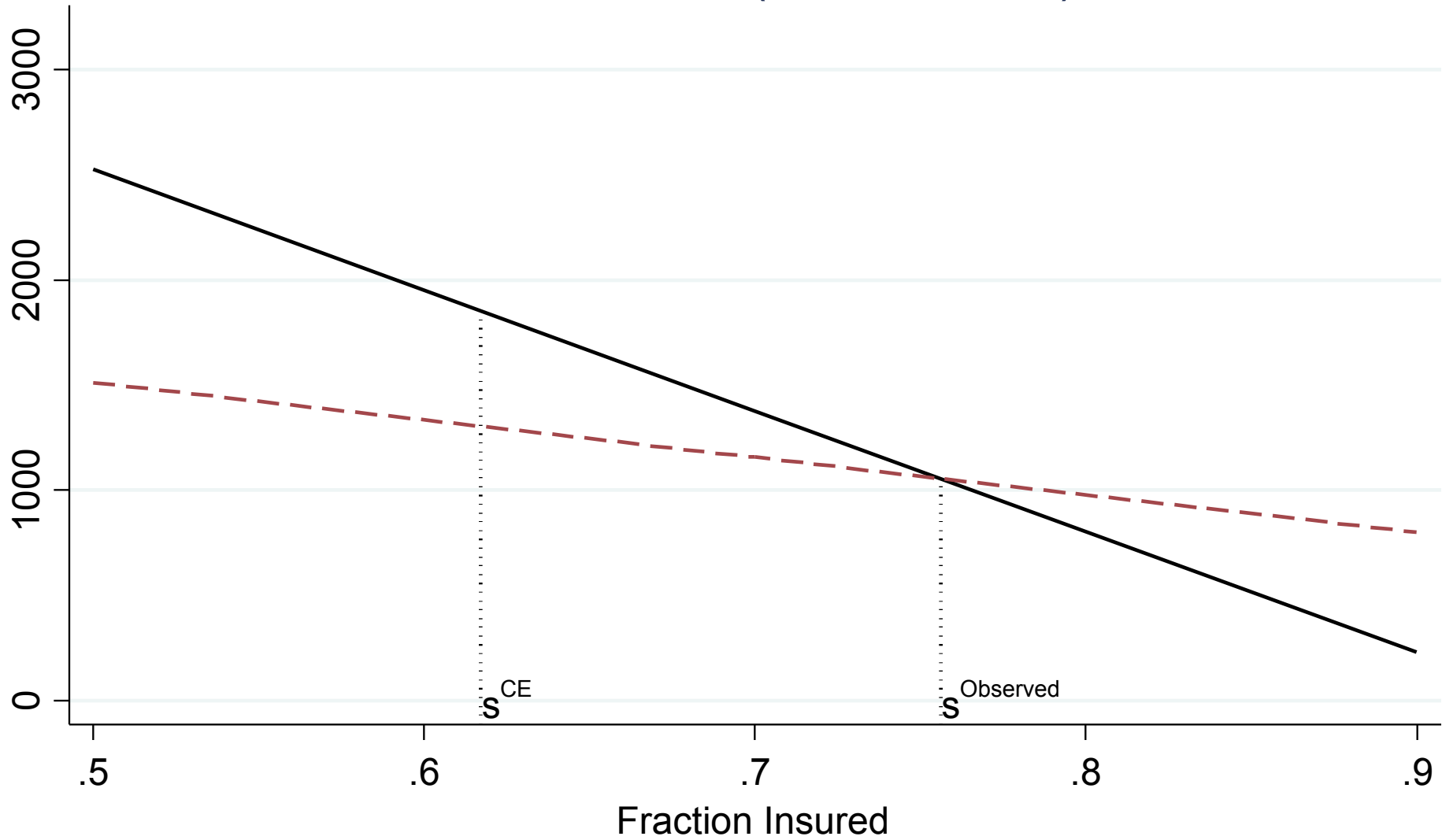
— Demand - - - Marginal Cost
— 'Ex-ante' Demand

Top-Up Health Insurance (EFC2010)



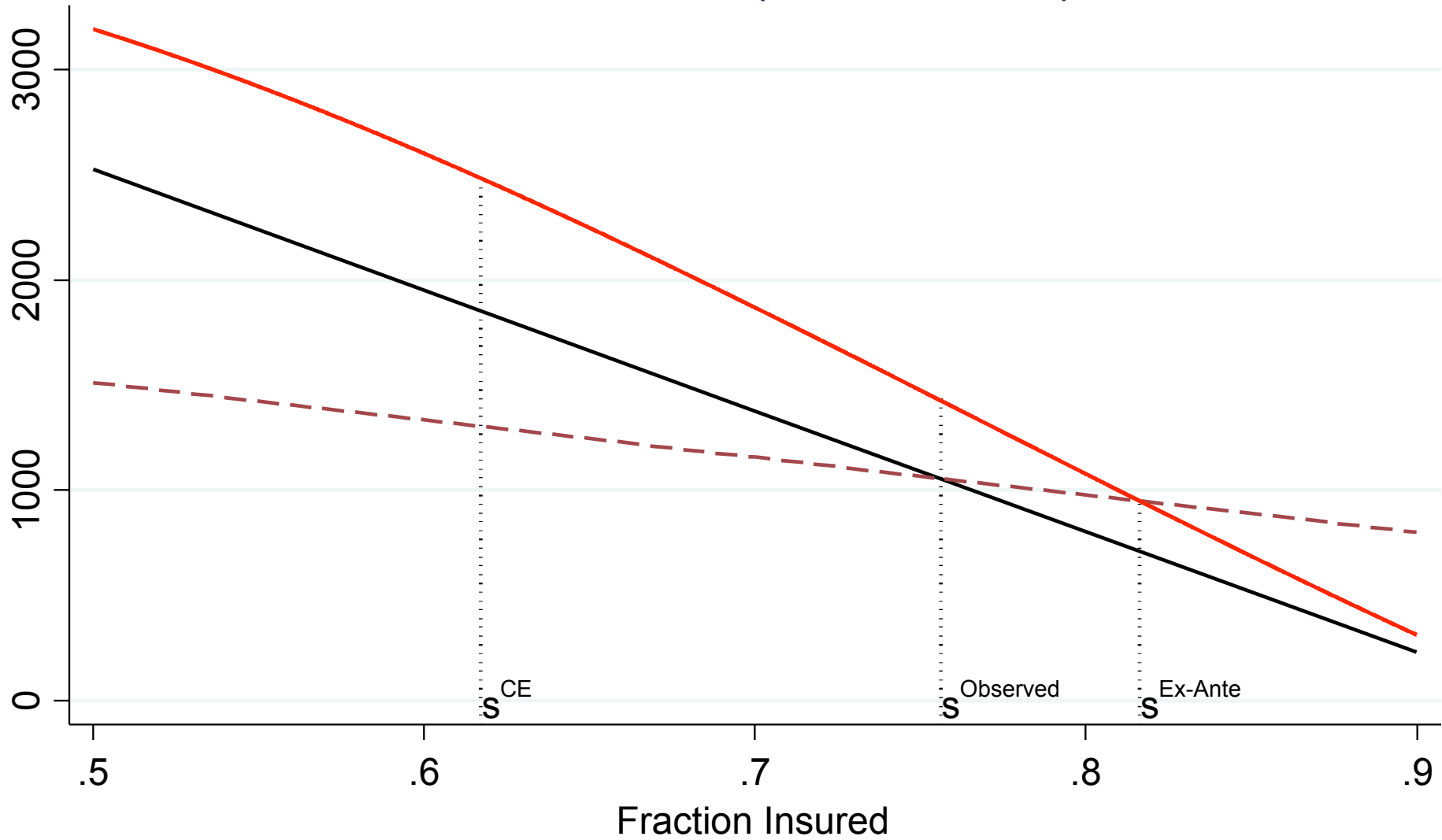
— Demand - - - Marginal Cost
— 'Ex-ante' Demand

Medium Risk (4x EFC2010)



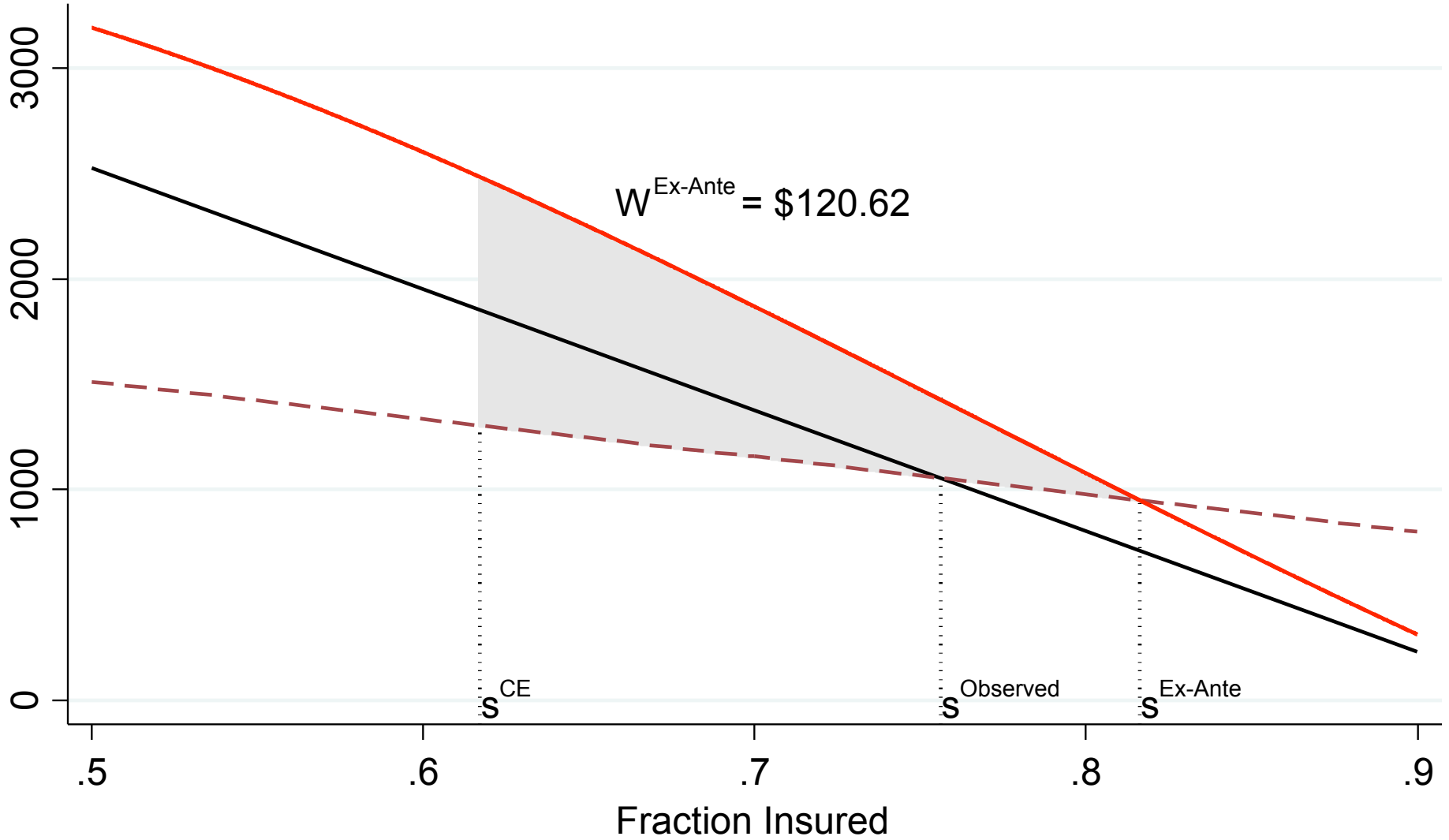
— Demand - - - Marginal Cost
— 'Ex-ante' Demand

Medium Risk (4x EFC2010)



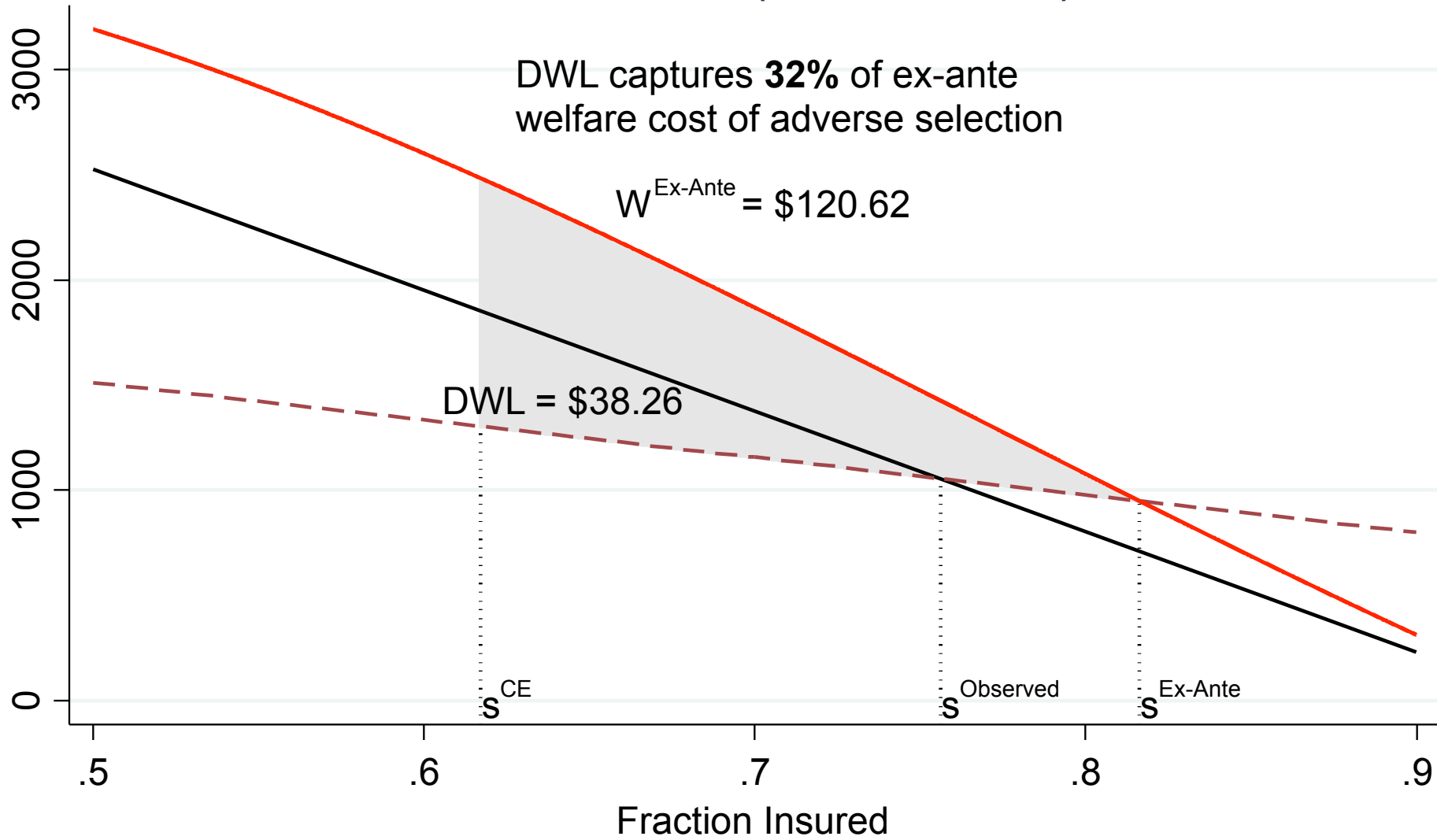
— Demand - - - Marginal Cost
— 'Ex-ante' Demand

Medium Risk (4x EFC2010)



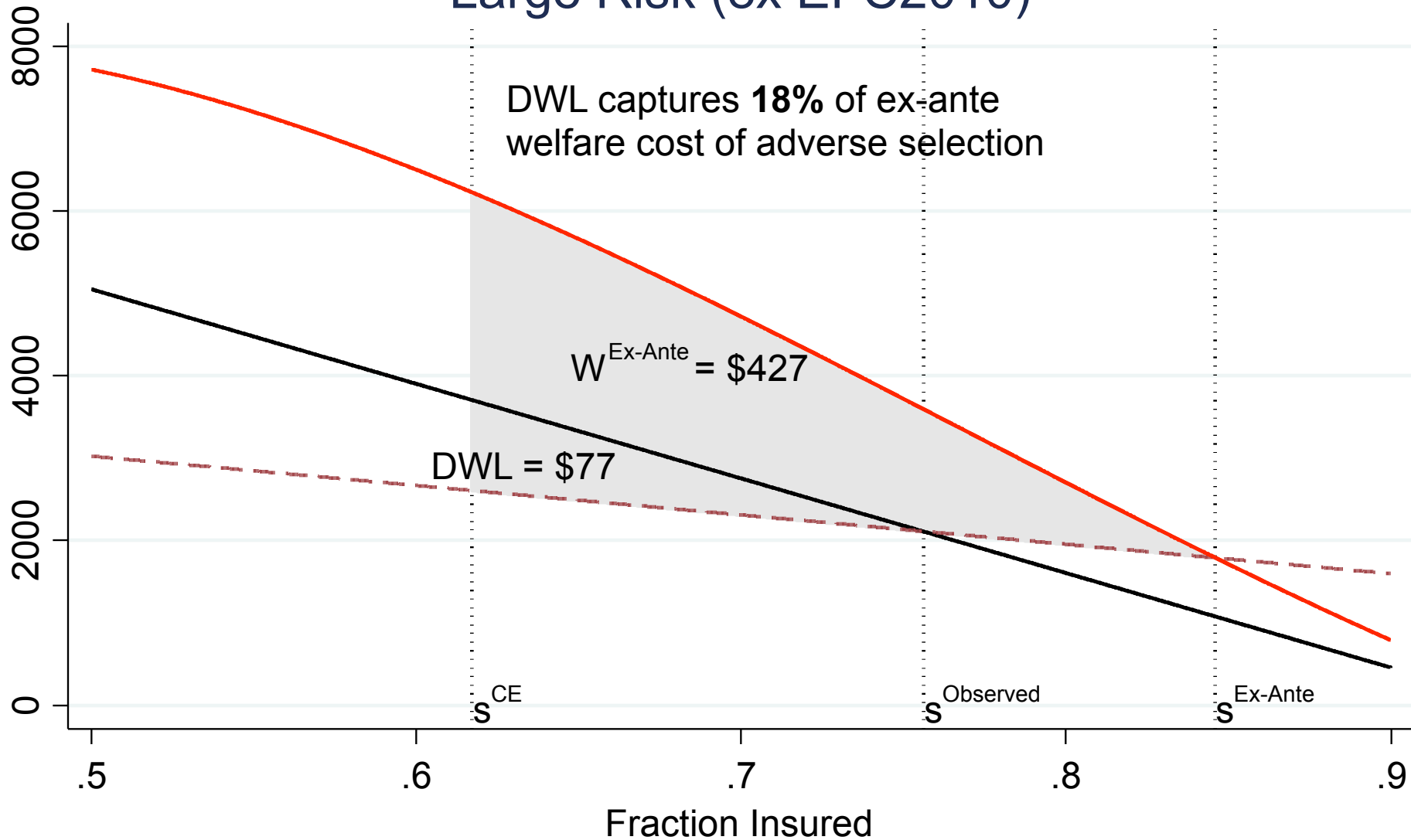
— Demand - - - Marginal Cost
— 'Ex-ante' Demand

Medium Risk (4x EFC2010)



- Demand
- 'Ex-ante' Demand
- - - Marginal Cost

Large Risk (8x EFC2010)



- Demand
- Ex-Ante Demand
- - - Marginal Cost

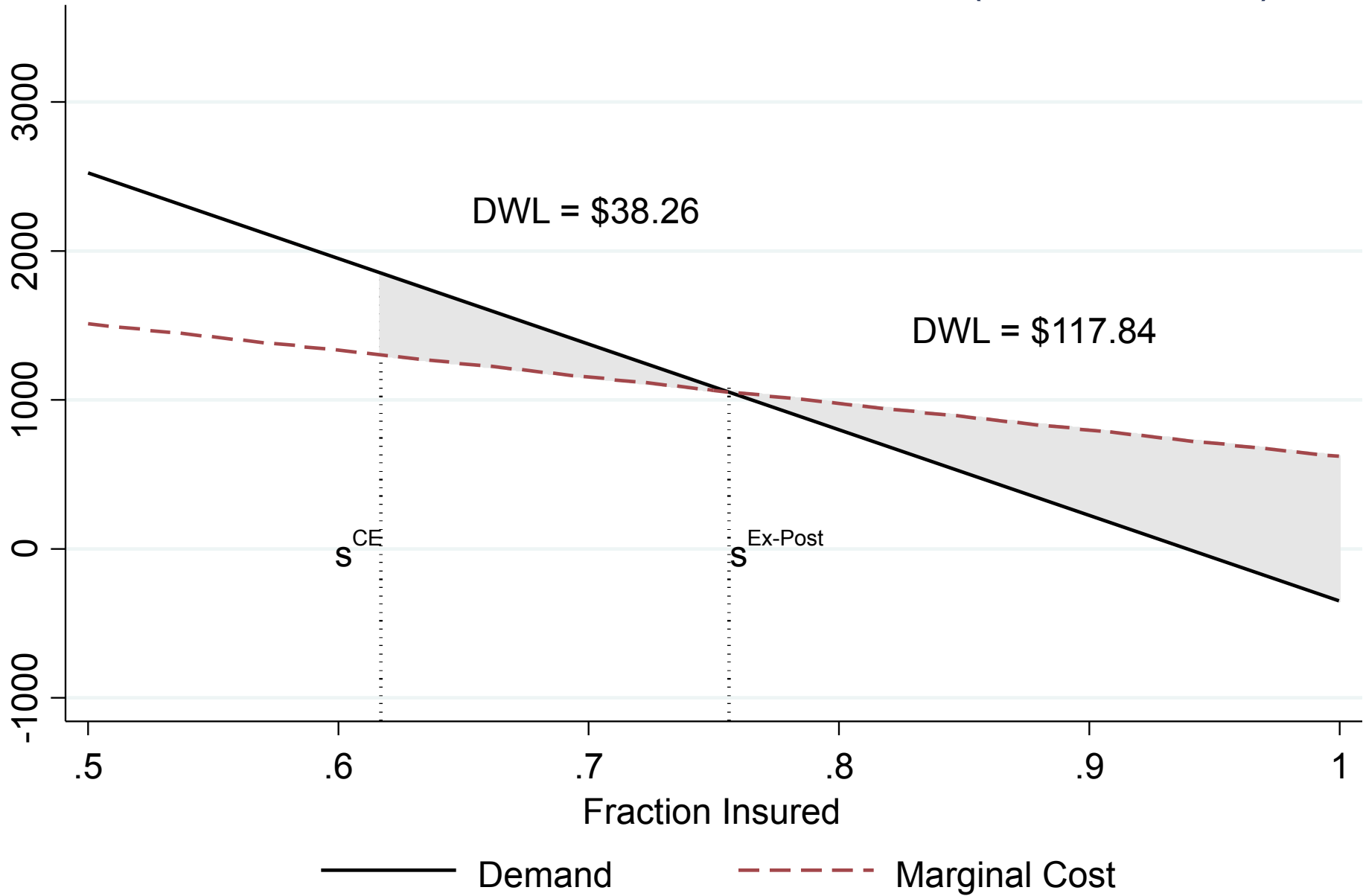
Ex-ante Insurance Value Increasing in Premium

- Divergence between Observed and Ex-ante value of insurance is increasing in the size/importance of the risk
 - DWL captures 67% of the ex-ante welfare cost of adverse selection for baseline specification in Einav, Finkelstein, and Cullen (2010)
 - Only 18% if risks are 8x as large
- More important for risks where the premiums are a significant share of people's incomes
 - Health, life, disability, unemployment insurance
 - Less important for iPhone insurance...

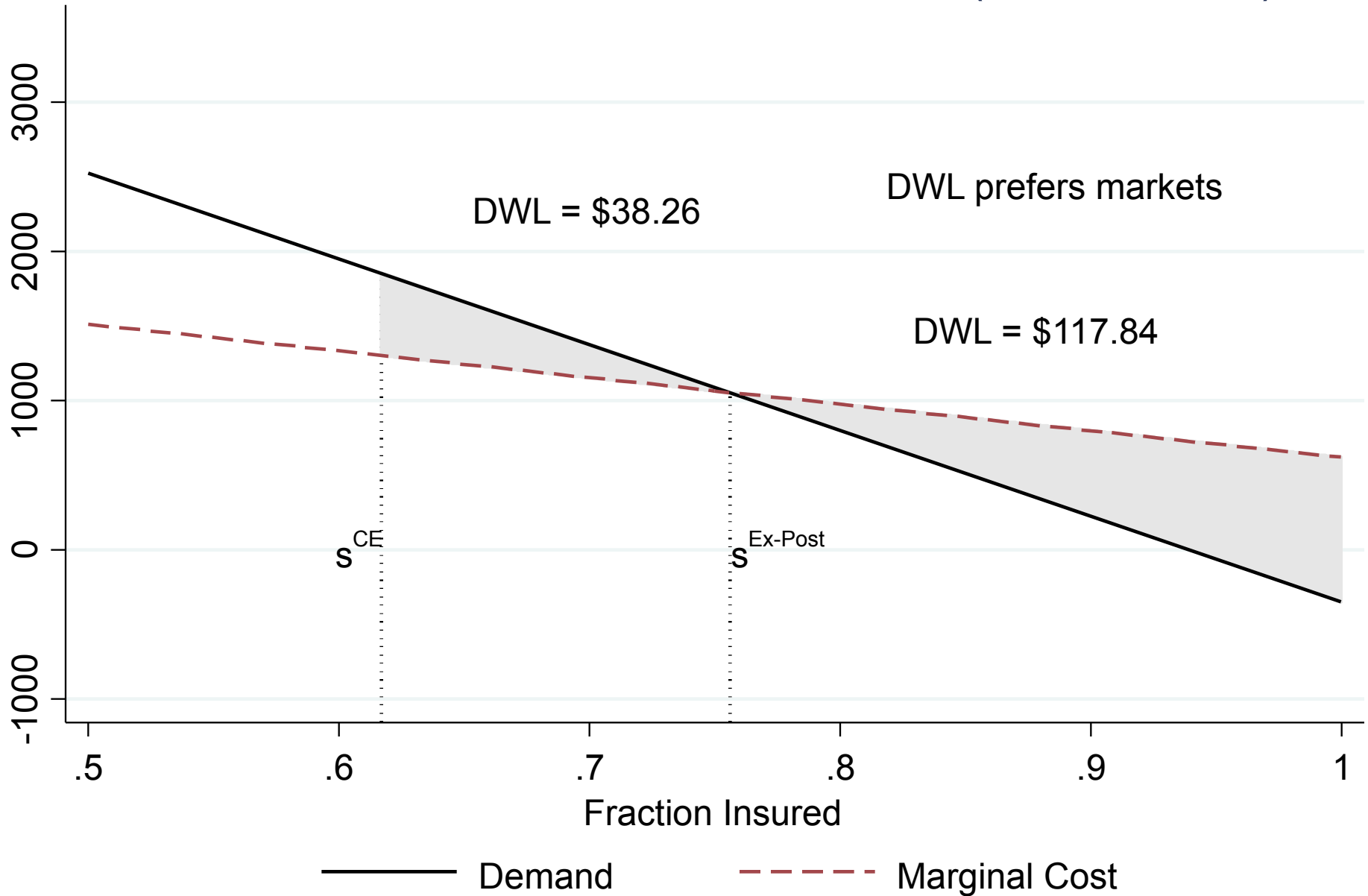
Competitive Markets vs. Mandates

- Are competitive markets better or worse than govt mandates?
 - Competitive markets suffer adverse selection
 - Mandates may require some to buy insurance that don't want it

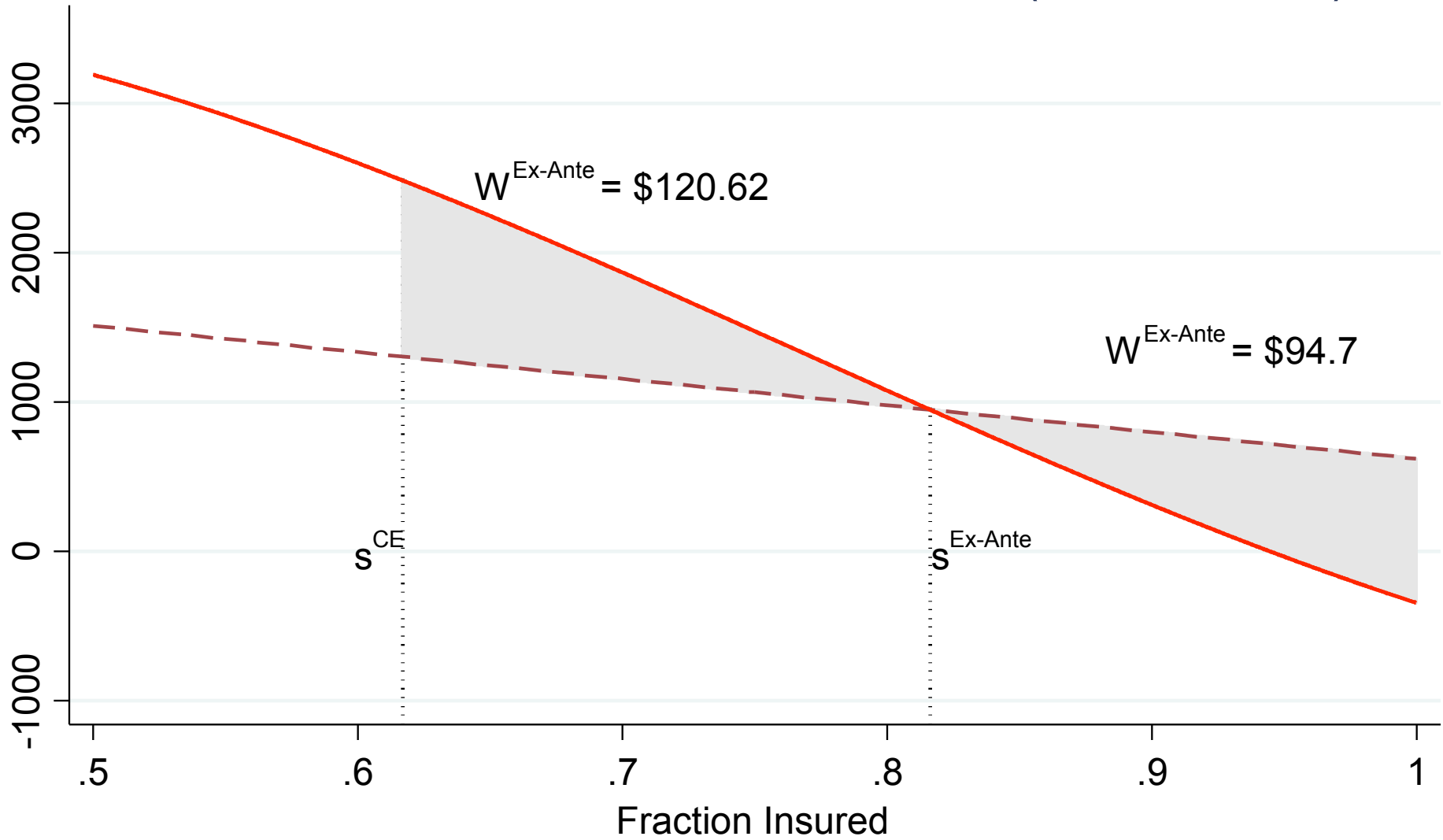
Markets vs. Mandates: Medium Risk (4x EFC2010)



Markets vs. Mandates: Medium Risk (4x EFC2010)

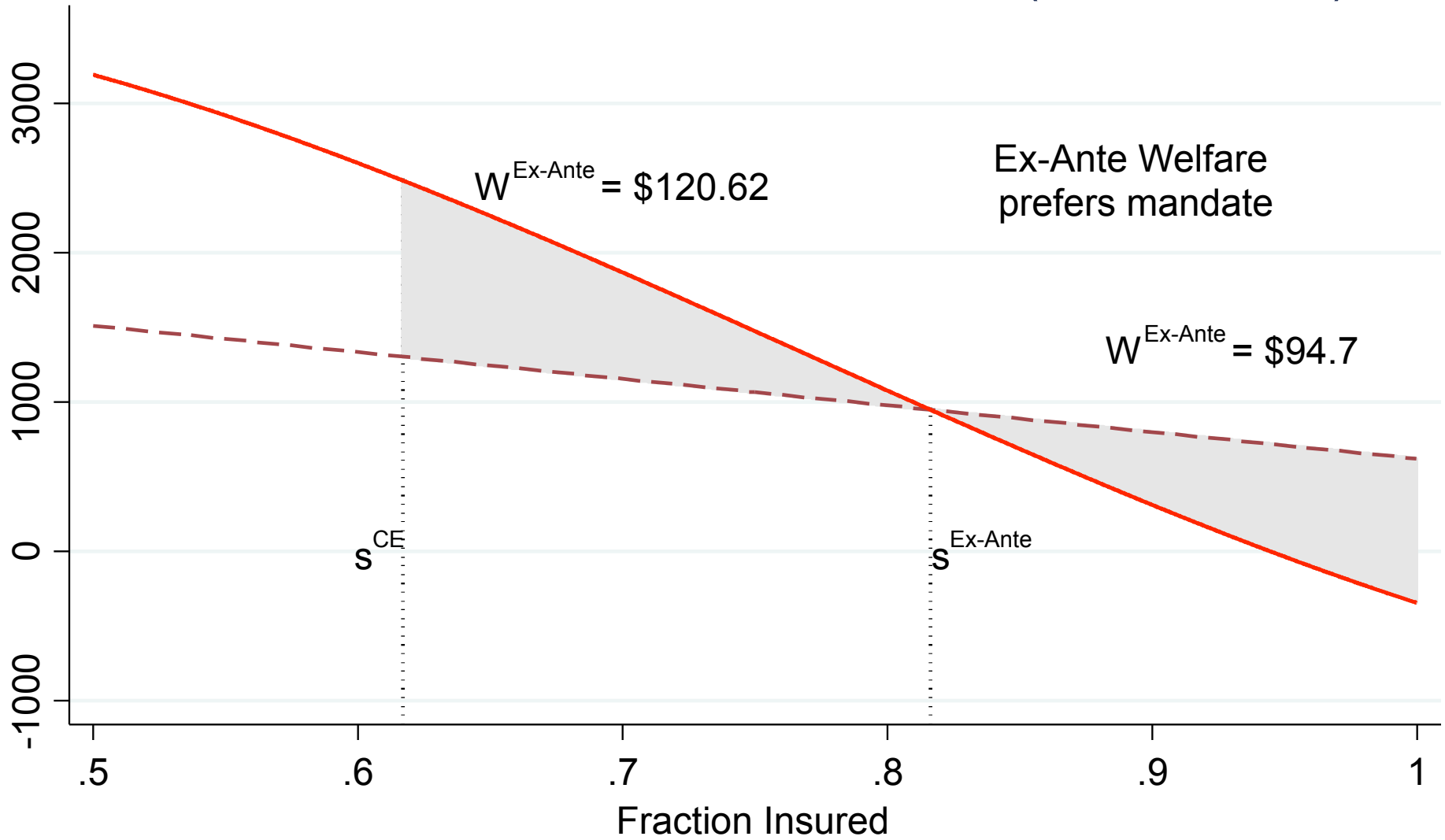


Markets vs. Mandates: Medium Risk (4x EFC2010)



- Demand
- 'Ex-ante' Demand
- - - Marginal Cost

Markets vs. Mandates: Medium Risk (4x EFC2010)



- Demand
- 'Ex-ante' Demand
- - - Marginal Cost

DWL vs. Ex-Ante Welfare Lead to Different Conclusions

- For the medium and large risk specifications, ex-ante and ex-post (DWL) welfare measures generate different conclusions
- DWL perspective prefers markets
- Ex-ante/utilitarian perspective prefers mandates

Outline

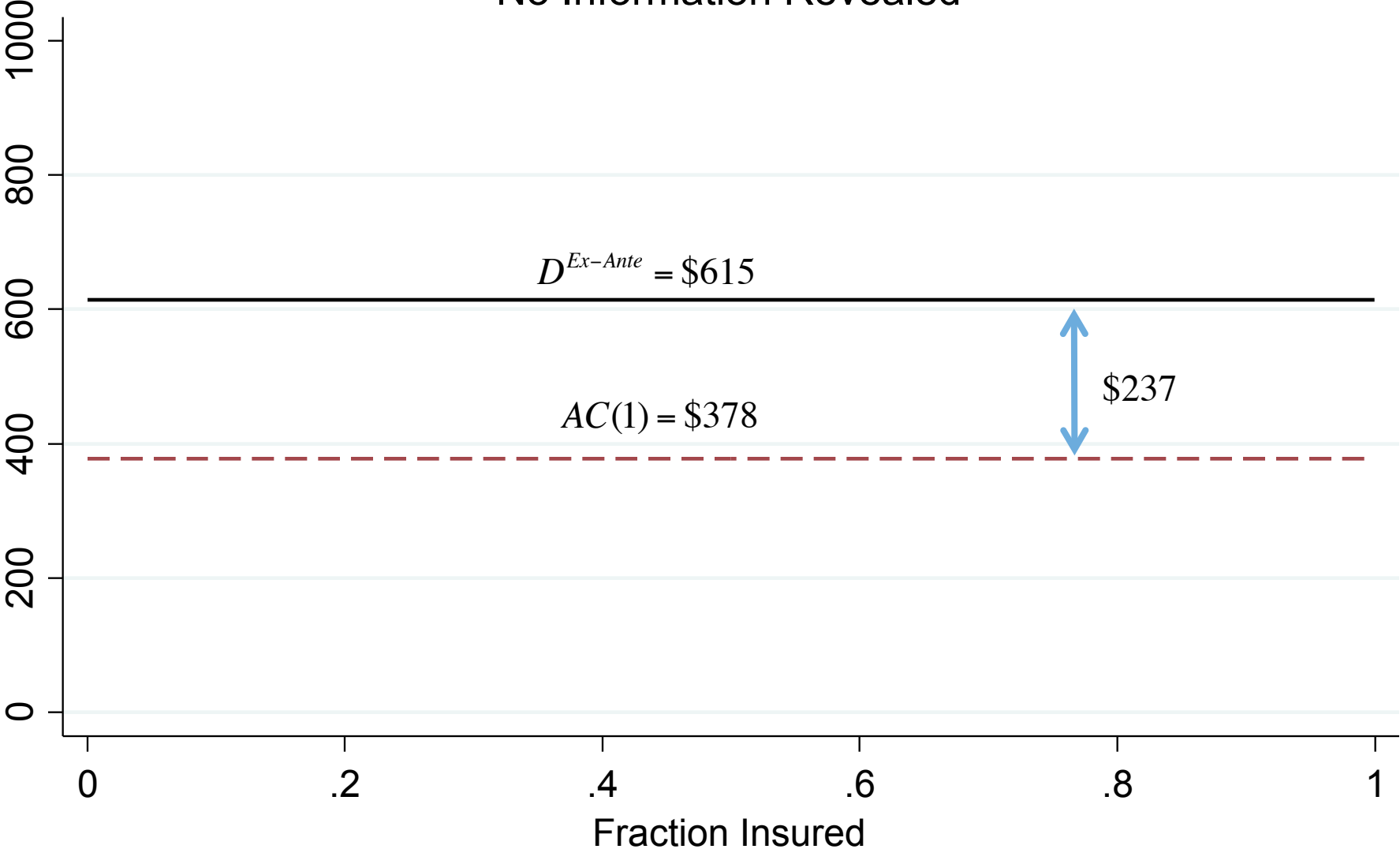
- Simple Example
- General Model
- Illustration with Optimal Health Insurance
- Optimal open enrollment periods

Optimal Open Enrollment Periods

- When should markets exist?
 - E.g. should open enrollment for 2017 ACA coverage be in:
 - September 2016? January 2017? Birth?
- Each of these timing of open enrollment generates different demand/cost curves
 - As information is revealed, demand curve tends to:
 - Rotate
 - Fall in levels
- Can use ex-ante demand curve to characterize optimal open enrollment period
 - Paper provides stylized calibration of this process to the EFC2010 setting

Optimal Open Enrollment Period

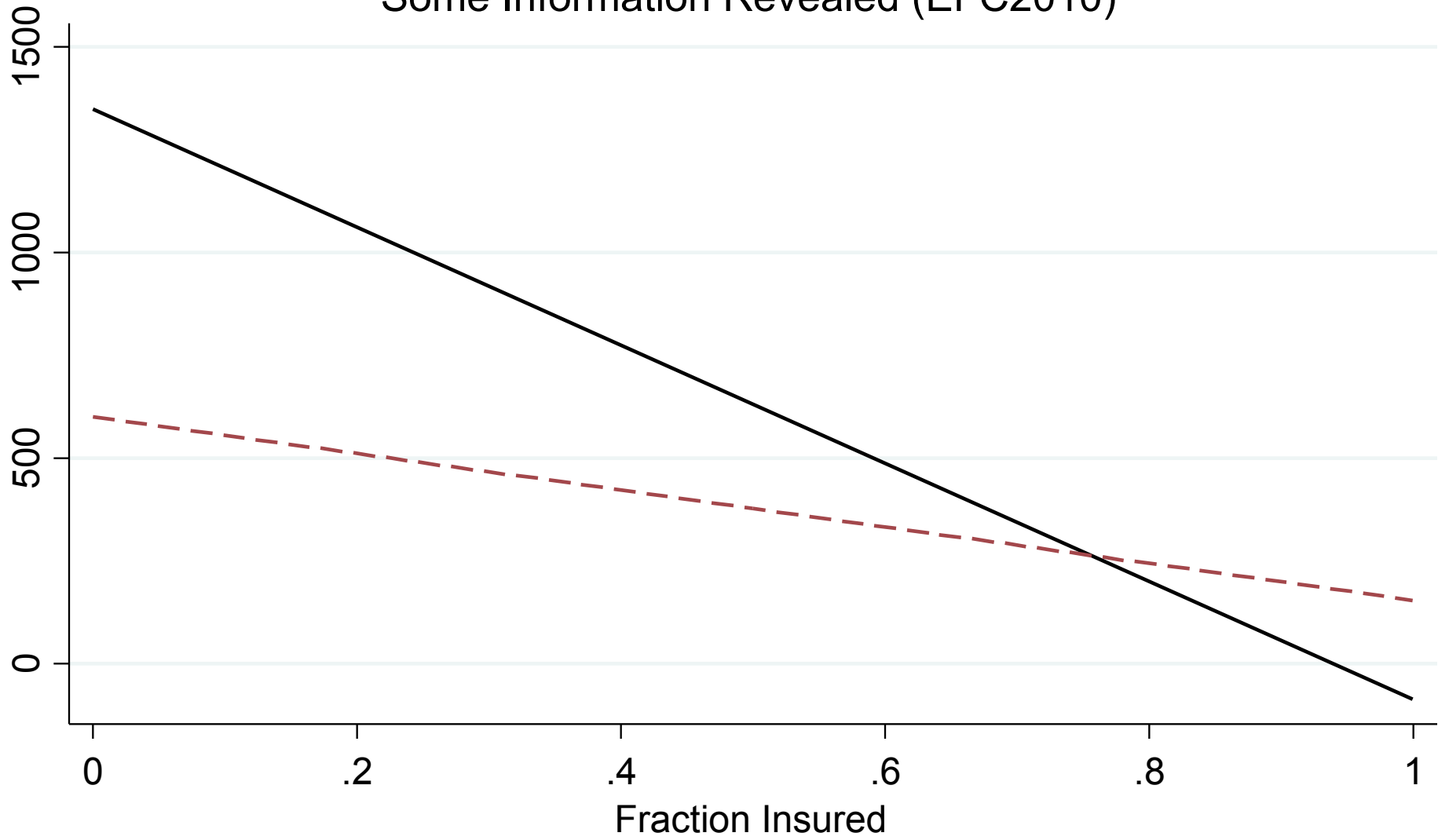
No Information Revealed



— Demand - - - Marginal Cost

Optimal Open Enrollment Period

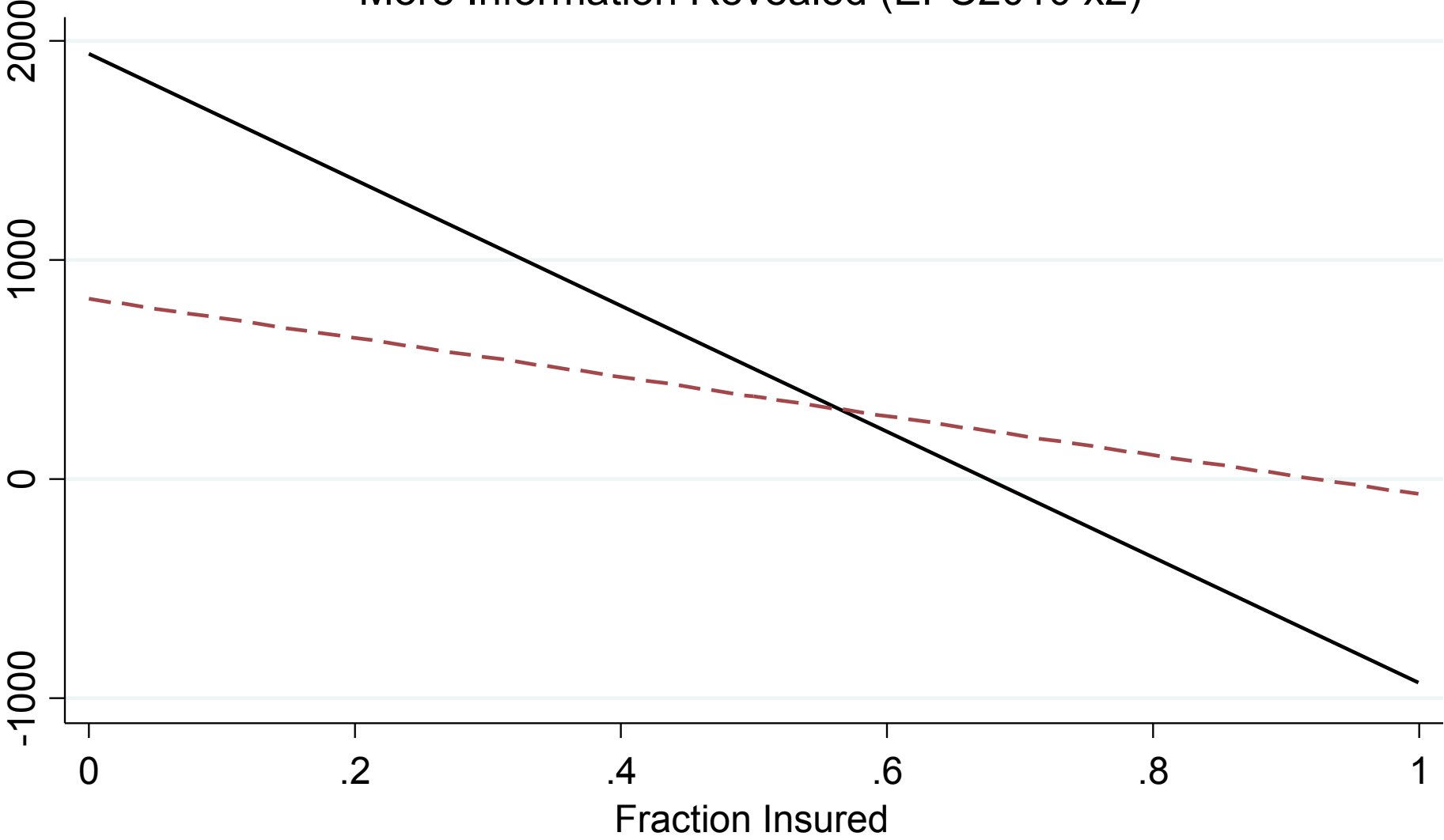
Some Information Revealed (EFC2010)



— Demand
— 'Ex-ante' Demand
- - - Marginal Cost

Optimal Open Enrollment Period

More Information Revealed (EFC2010 x2)



— Demand
— 'Ex-ante' Demand

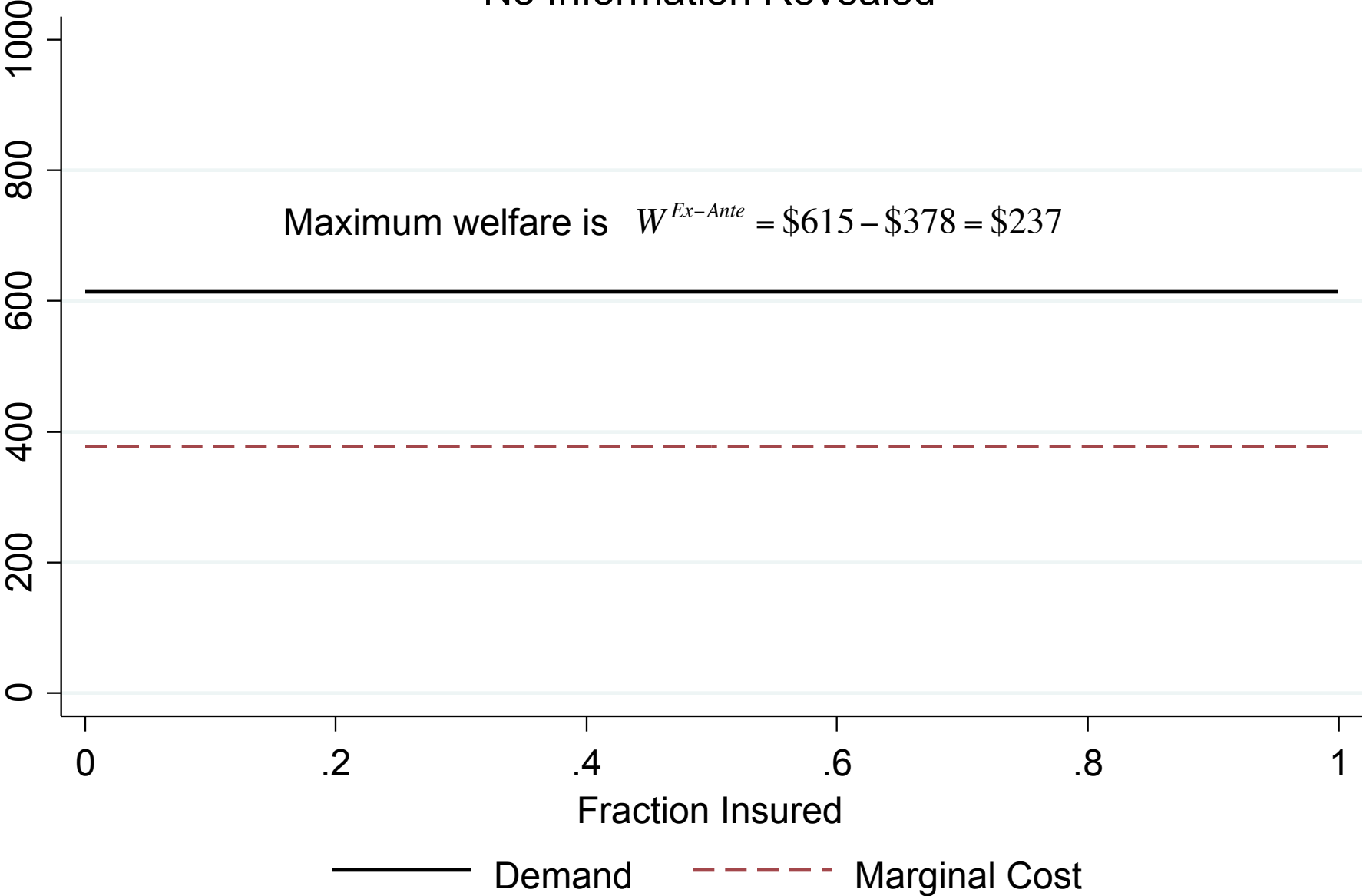
- - - Marginal Cost

Optimal Open Enrollment Periods

- Choice of optimal open enrollment period is a choice of which demand curve to face
 - Combined with choices of prices/subsidies for insurance
- Key: Average value of ex-ante demand curve is stable

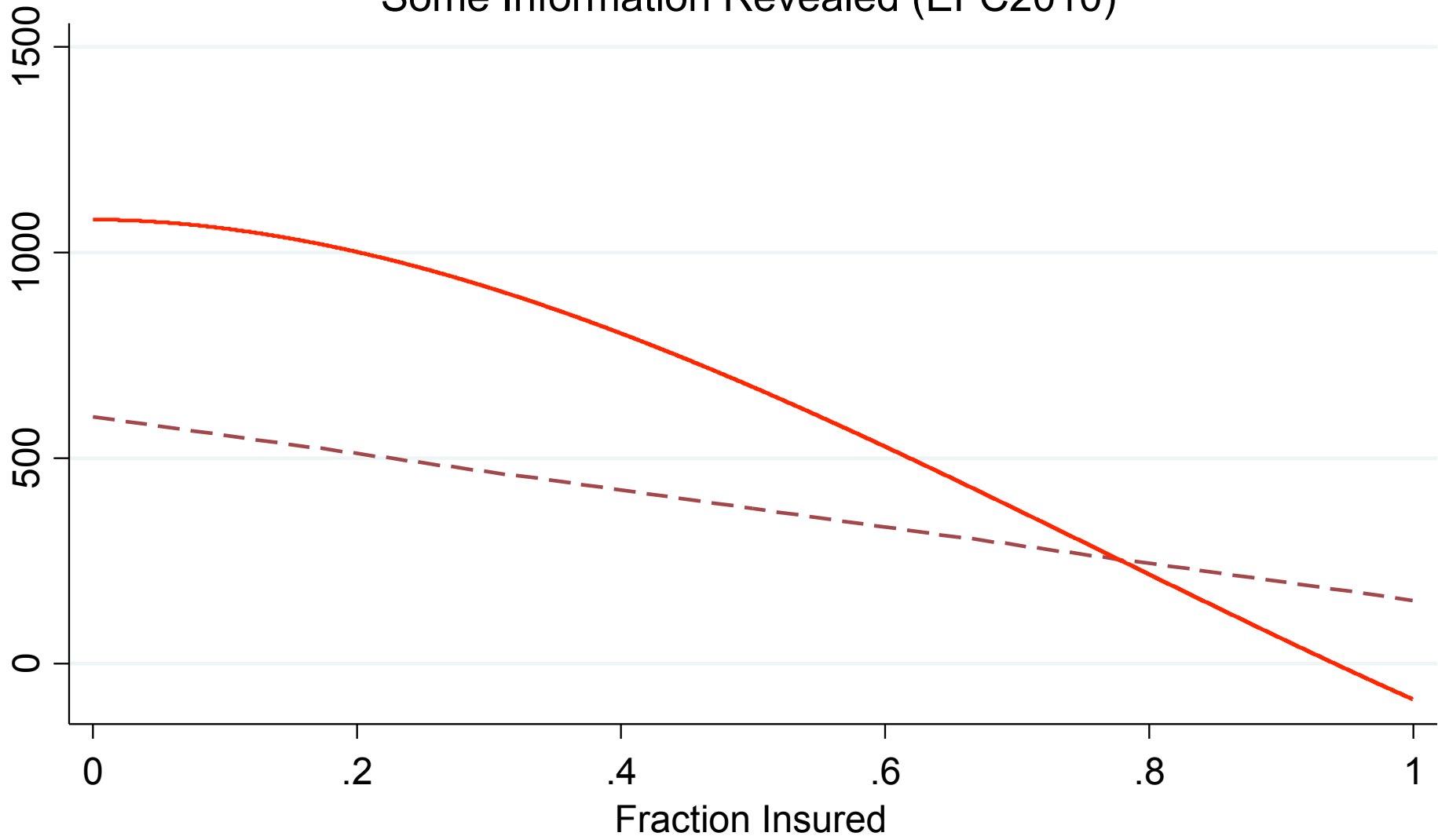
Optimal Open Enrollment Period

No Information Revealed



Optimal Open Enrollment Period

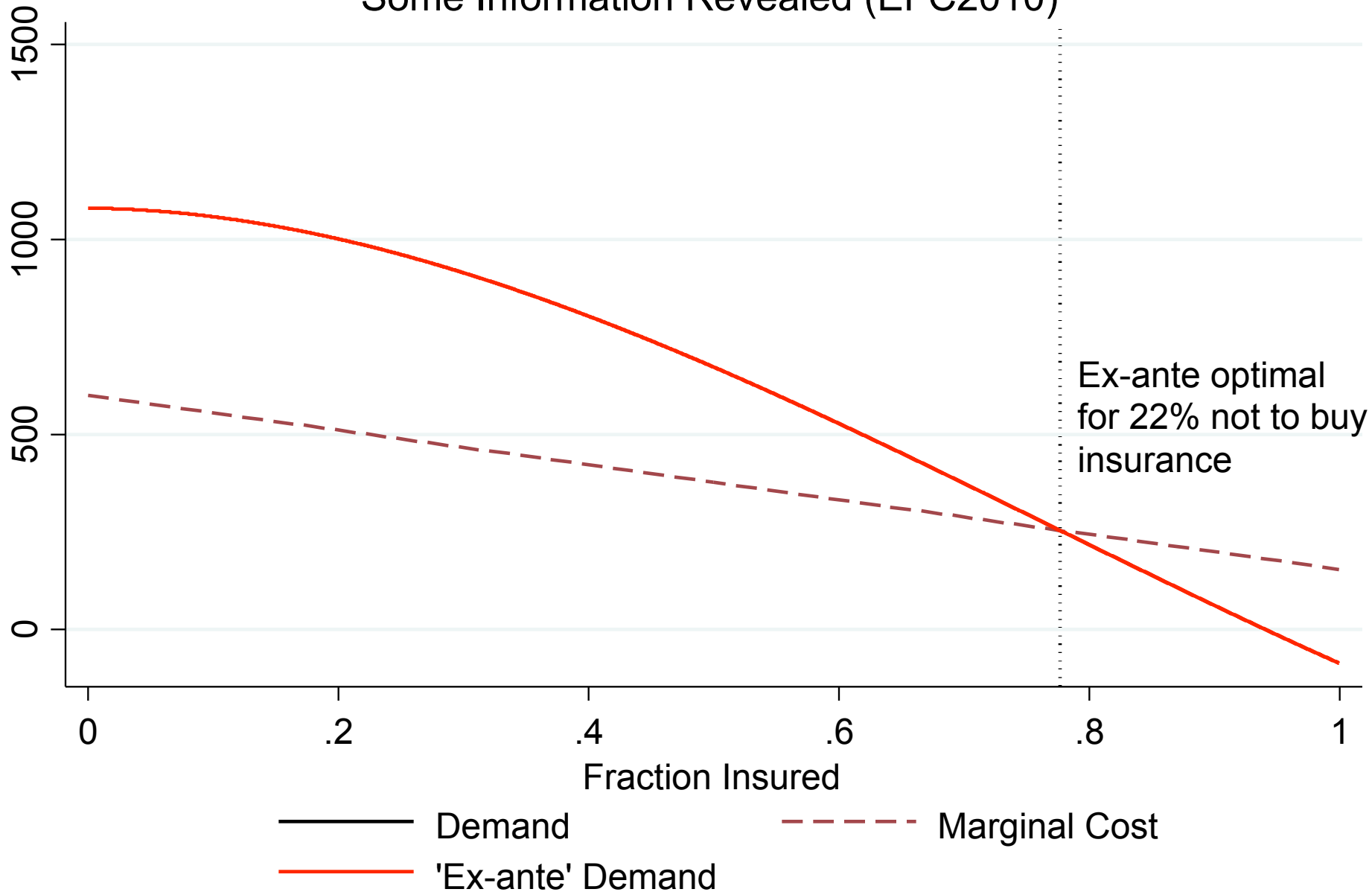
Some Information Revealed (EFC2010)



— Demand
— 'Ex-ante' Demand
- - - Marginal Cost

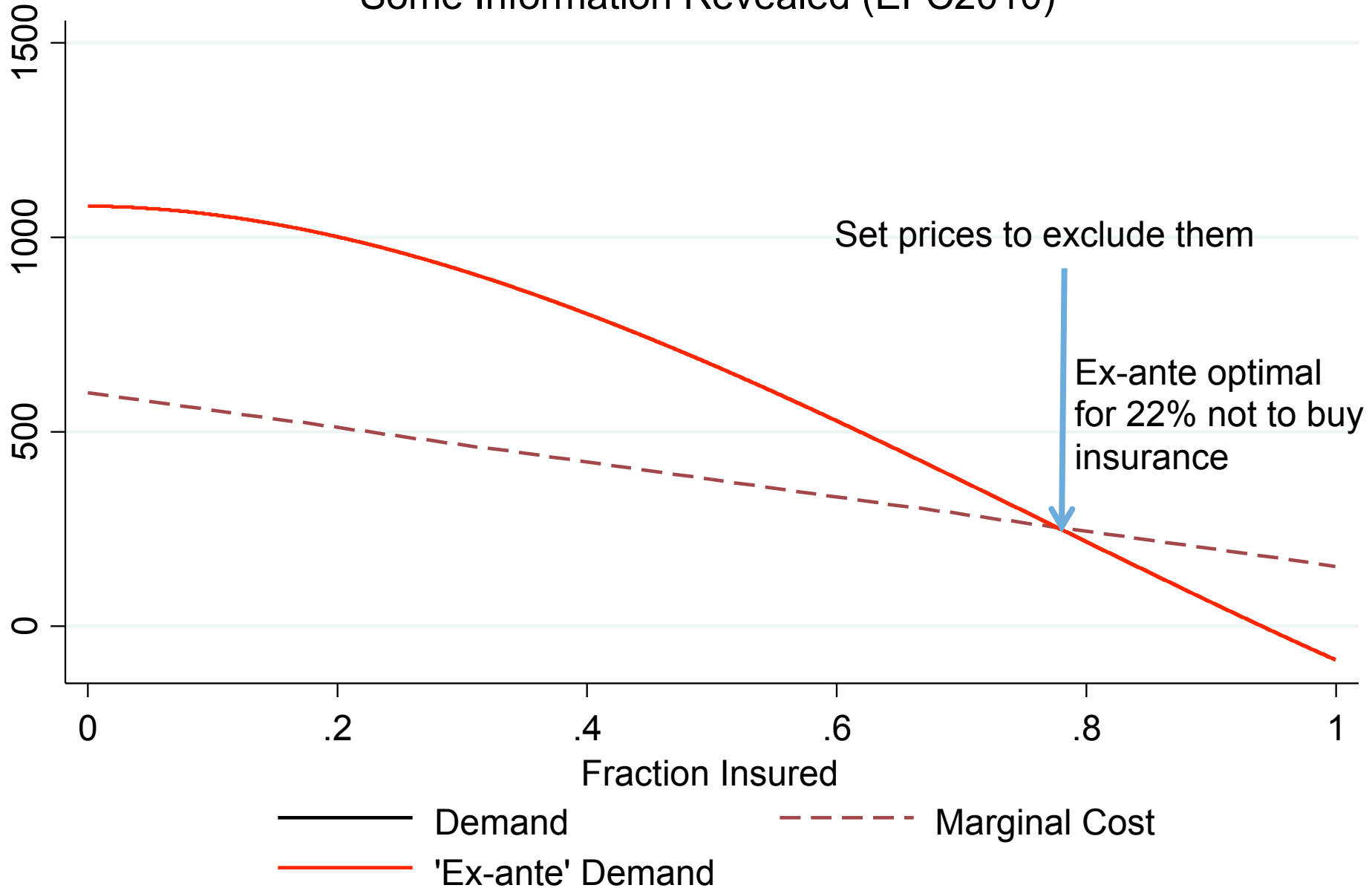
Optimal Open Enrollment Period

Some Information Revealed (EFC2010)



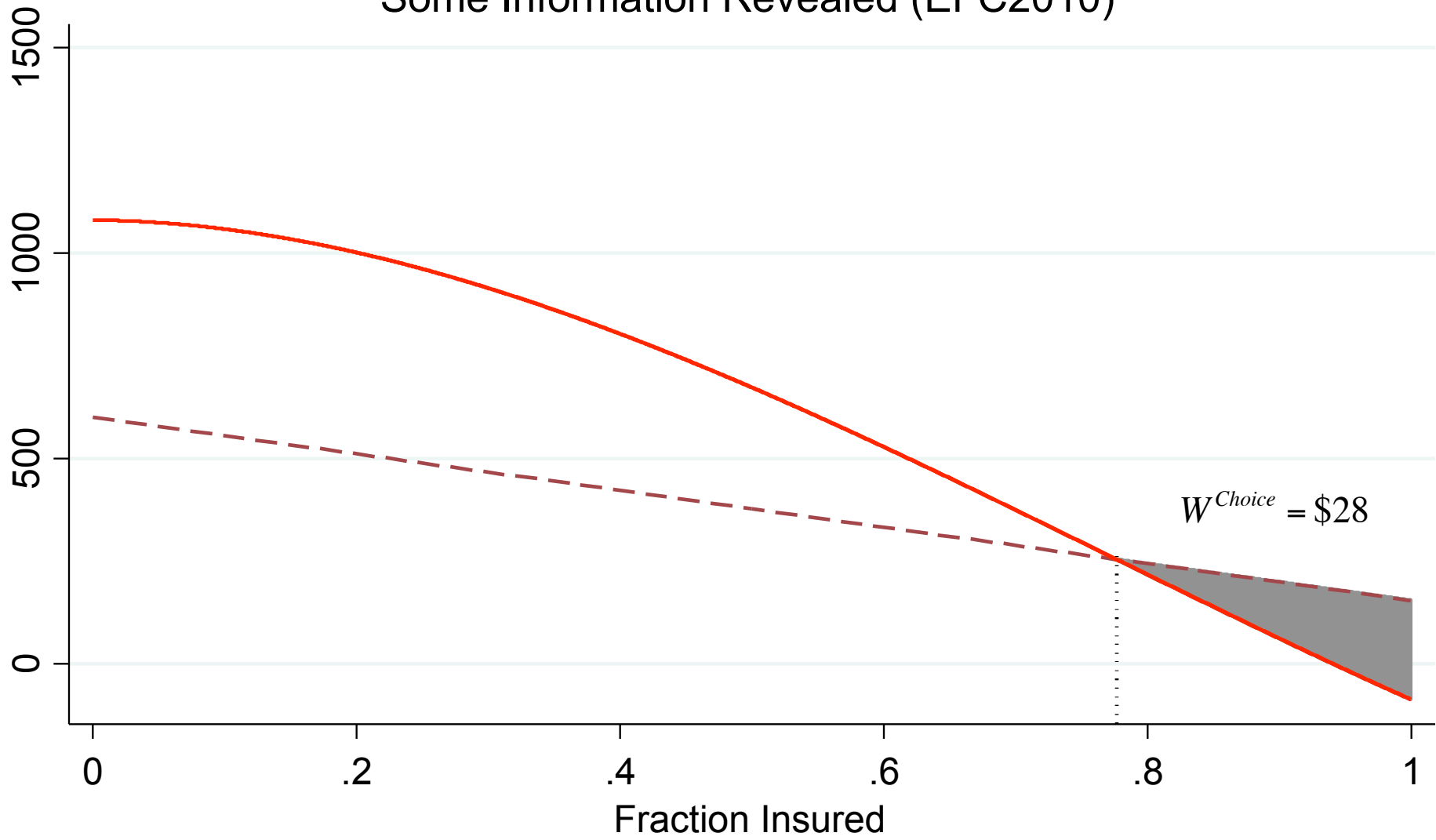
Optimal Open Enrollment Period

Some Information Revealed (EFC2010)



Optimal Open Enrollment Period

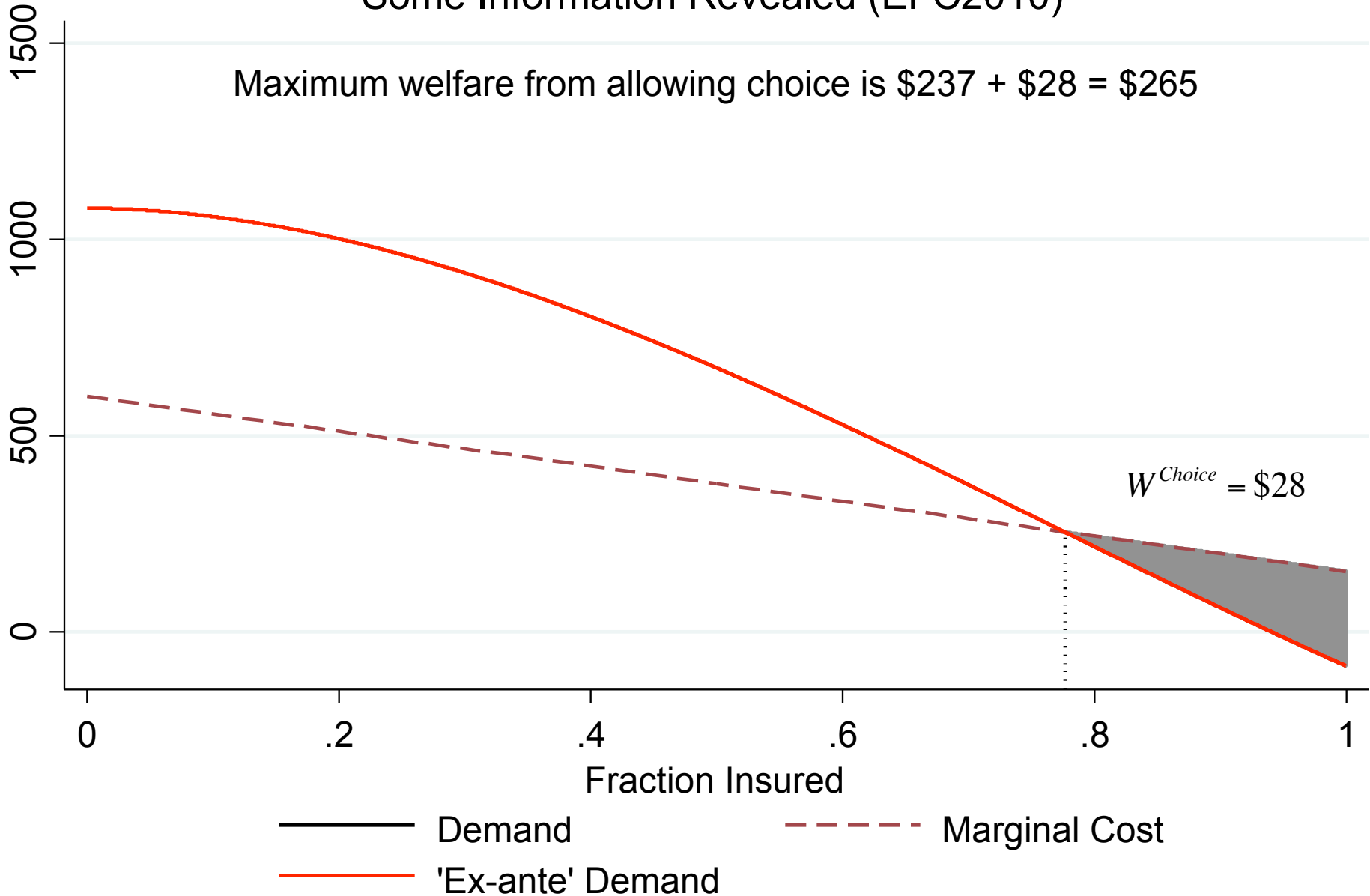
Some Information Revealed (EFC2010)



— Demand
— 'Ex-ante' Demand
- - - Marginal Cost

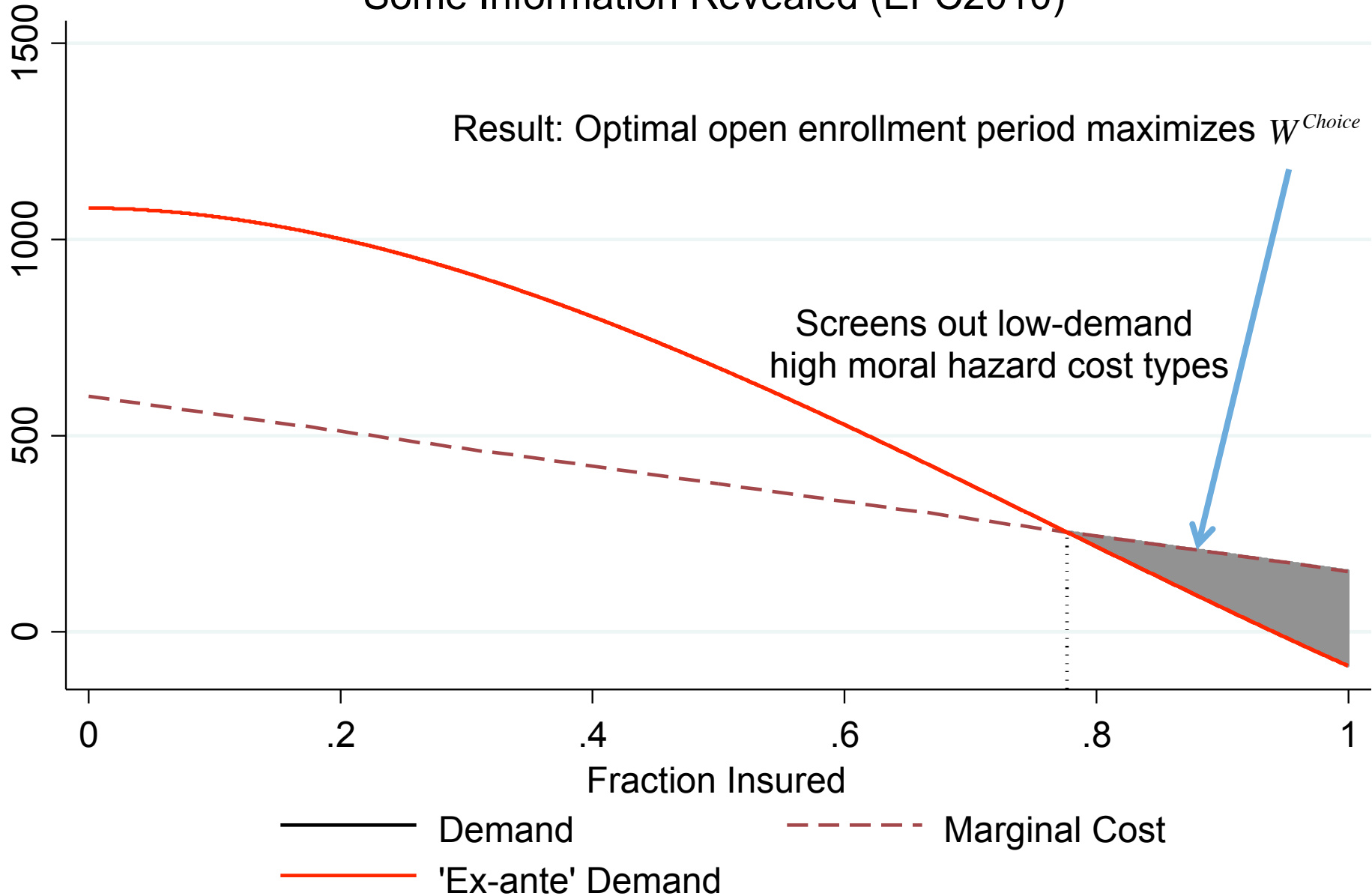
Optimal Open Enrollment Period

Some Information Revealed (EFC2010)



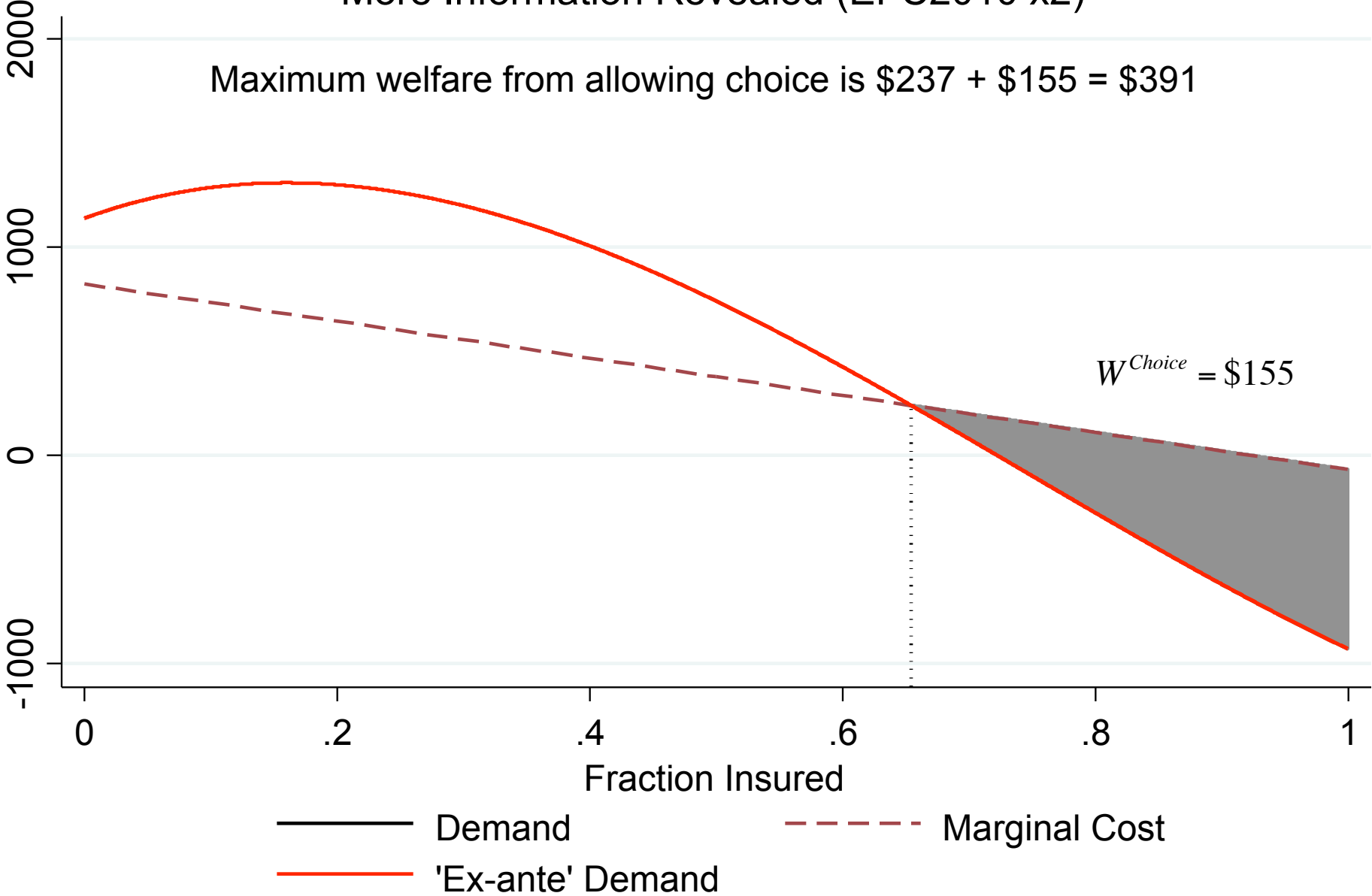
Optimal Open Enrollment Period

Some Information Revealed (EFC2010)



Optimal Open Enrollment Period

More Information Revealed (EFC2010 x2)

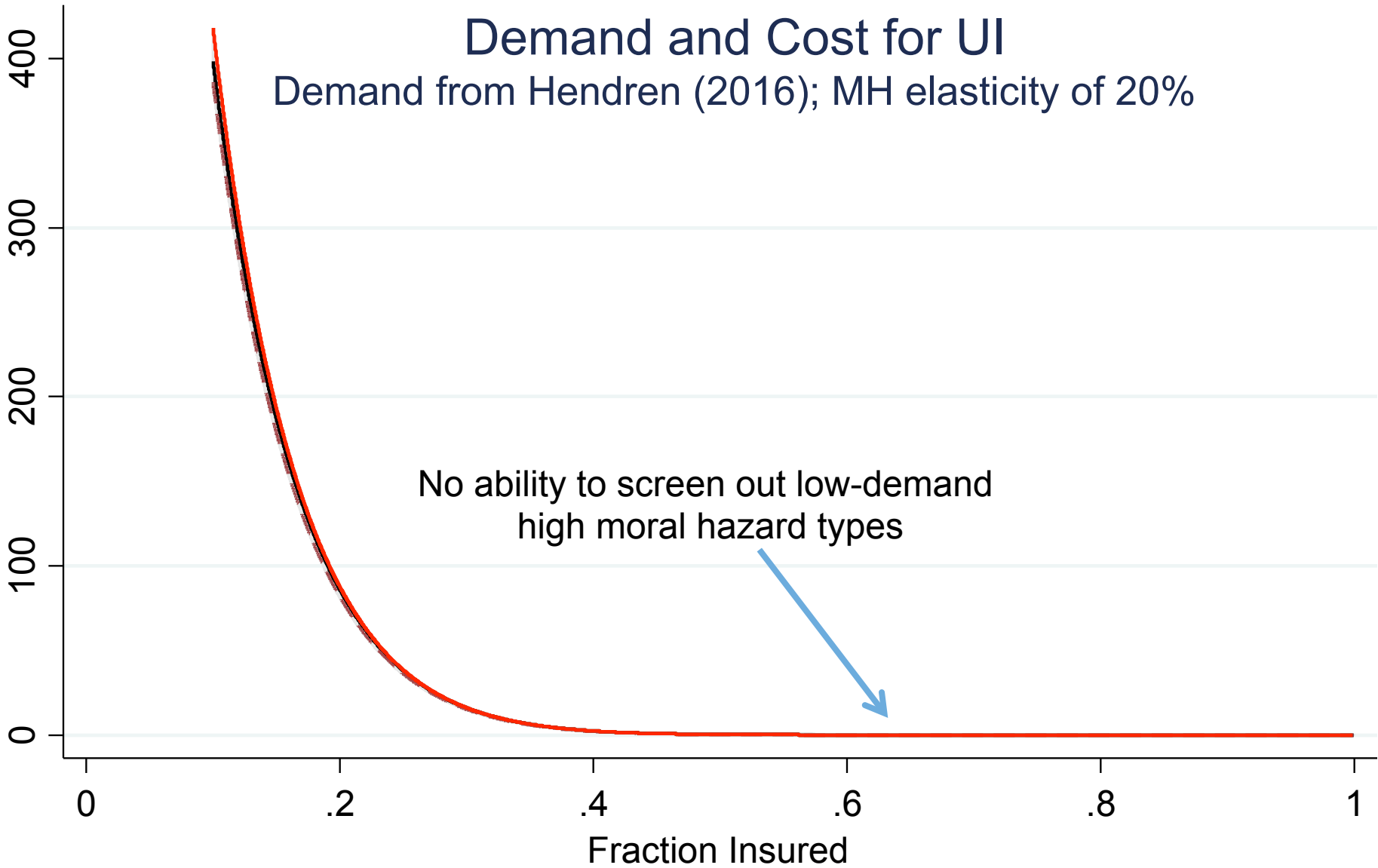


Optimal Open Enrollment Periods

- Optimal open enrollment periods maximize quantity of low-demand high moral hazard types
 - Maximize area between marginal cost curve and ex-ante demand curve
 - May be optimal / preferred to allow contracting in presence of adverse selection
- But low-demand high moral hazard types not always present

Demand and Cost for UI

Demand from Hendren (2016); MH elasticity of 20%



- Demand, $D(s)$
- - - Marginal cost, $MC(s)$
- Ex-Ante Demand, $EA(s)+D(s)$

Mandates versus Subsidized Choice

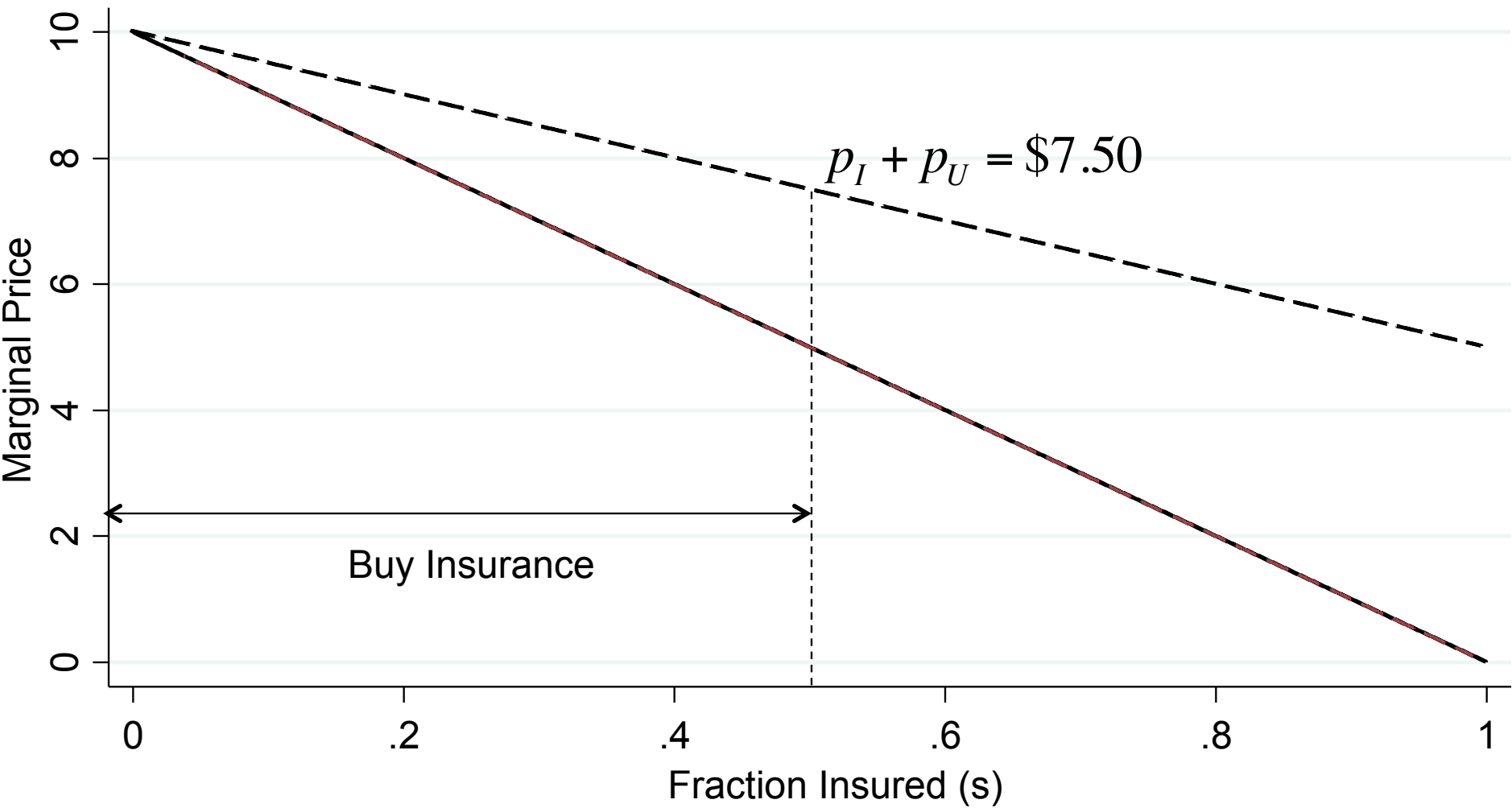
- Rationale for mandated UI but choice in health insurance?
- Are there no “low demand high moral hazard types” in UI?

Conclusion

- Insurance insures against the realization of risk
 - Adverse selection implies a divergence between DWL and Ex-ante welfare
- Exploit Baily-Chetty logic to create ex-ante demand curve
 - Conduct utilitarian/ex-ante welfare analysis
- DWL and Ex-ante welfare can differ in conclusions about:
 - Optimal size of insurance market
 - Welfare cost of adverse selection
 - Competitive markets vs. mandates
 - Difference between DWL and Ex-ante welfare increasing in size of risk
- Opens new questions like optimal open-enrollment periods
 - Screen out low-demand high moral hazard types

Appendix

From Observed Demand to Ex-Ante Demand

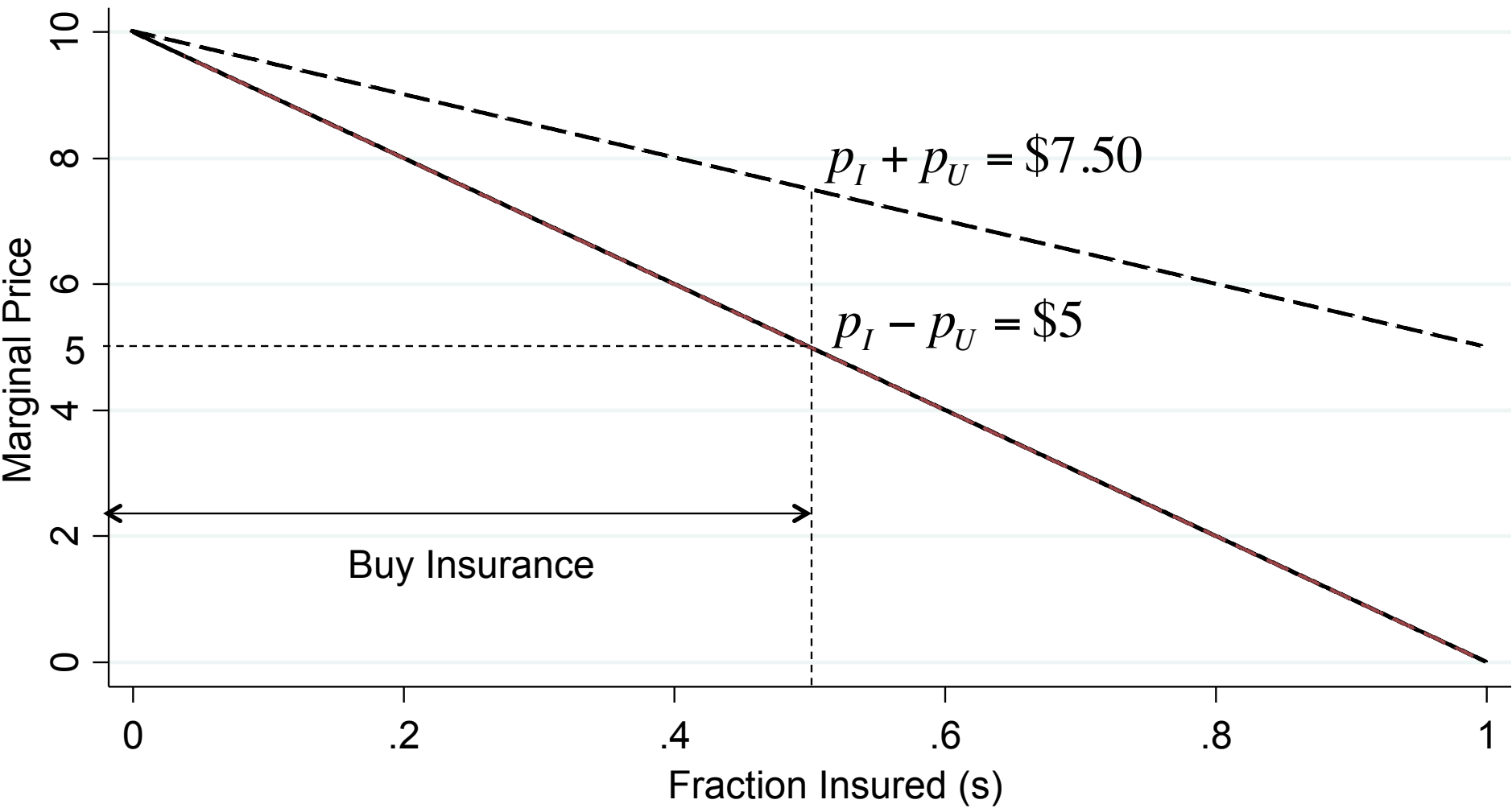


— Demand

- - - Marginal Cost

- - - Average Cost

From Observed Demand to Ex-Ante Demand

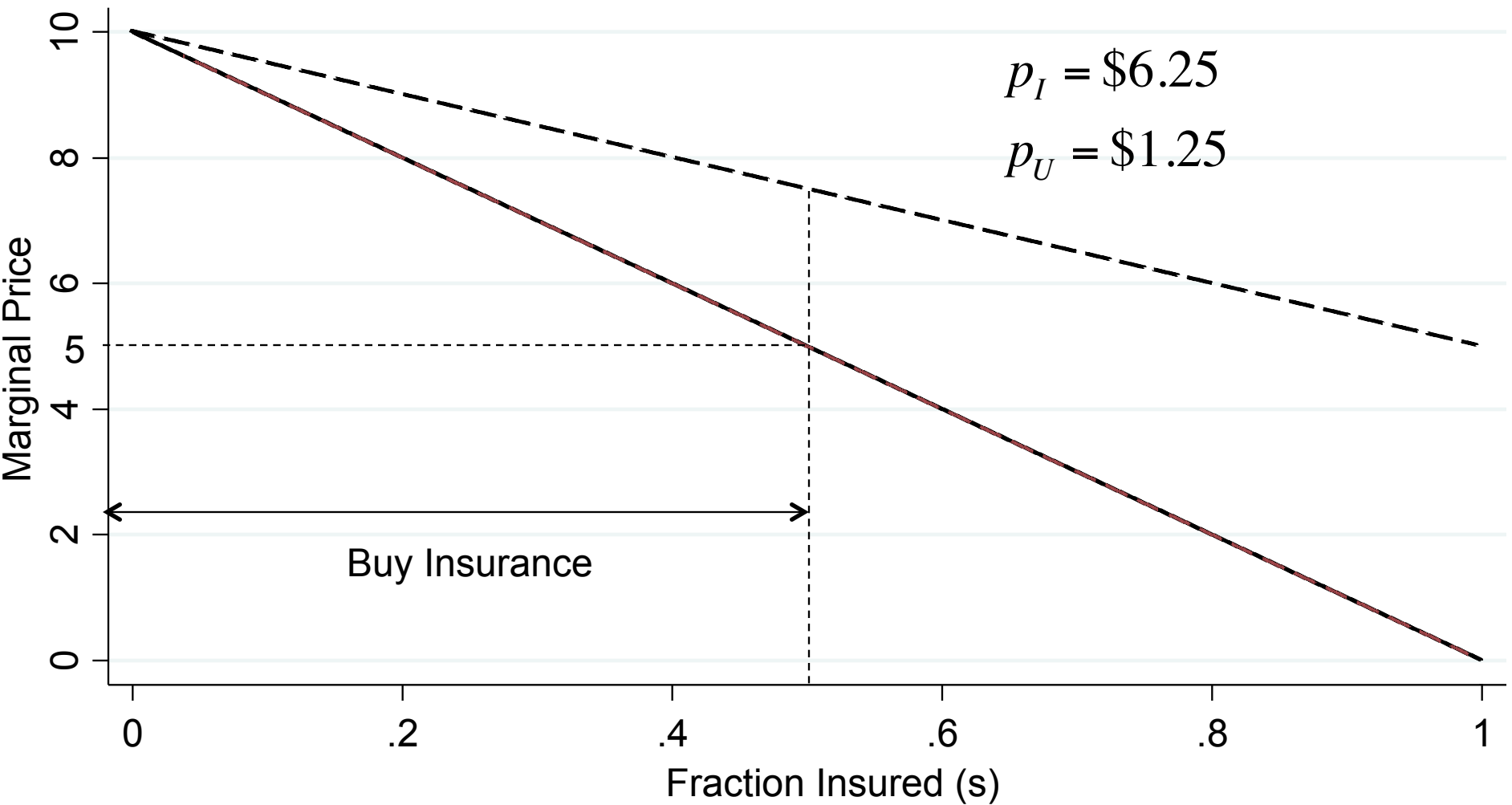


— Demand

- - - Marginal Cost

- - - Average Cost

From Observed Demand to Ex-Ante Demand



— Demand

- - - Marginal Cost

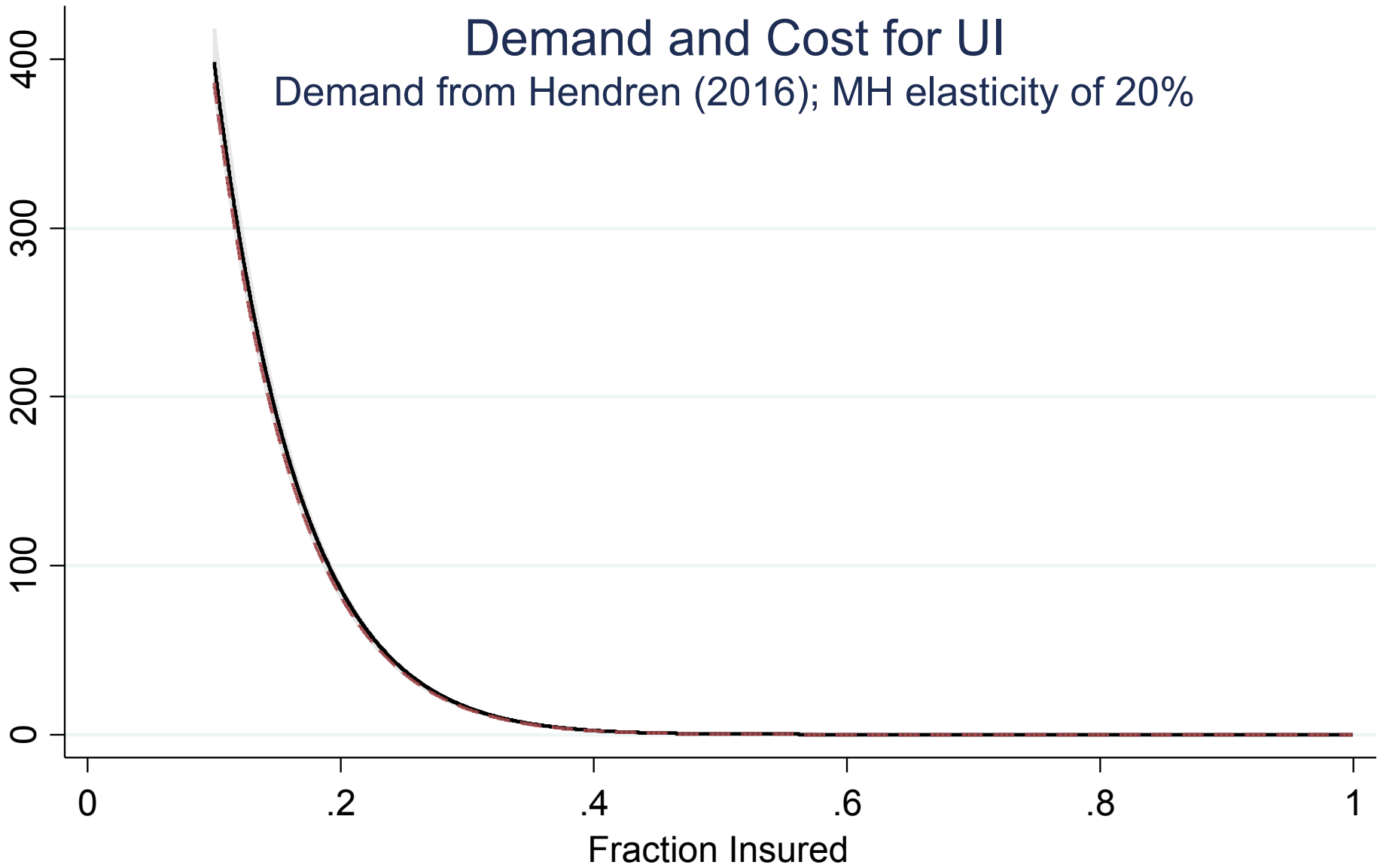
- - - Average Cost

Unemployment Insurance

- Ex-ante and observed demand also differ for UI
- Consider hypothetical annual contract to replace \$2,700 consumption drop if lose job in subsequent 12 months
 - Take demand parameters from Hendren (2016) + 20% moral hazard elasticity
 - Private market would unravel
 - Small fraction of market has high risk of losing job

Demand and Cost for UI

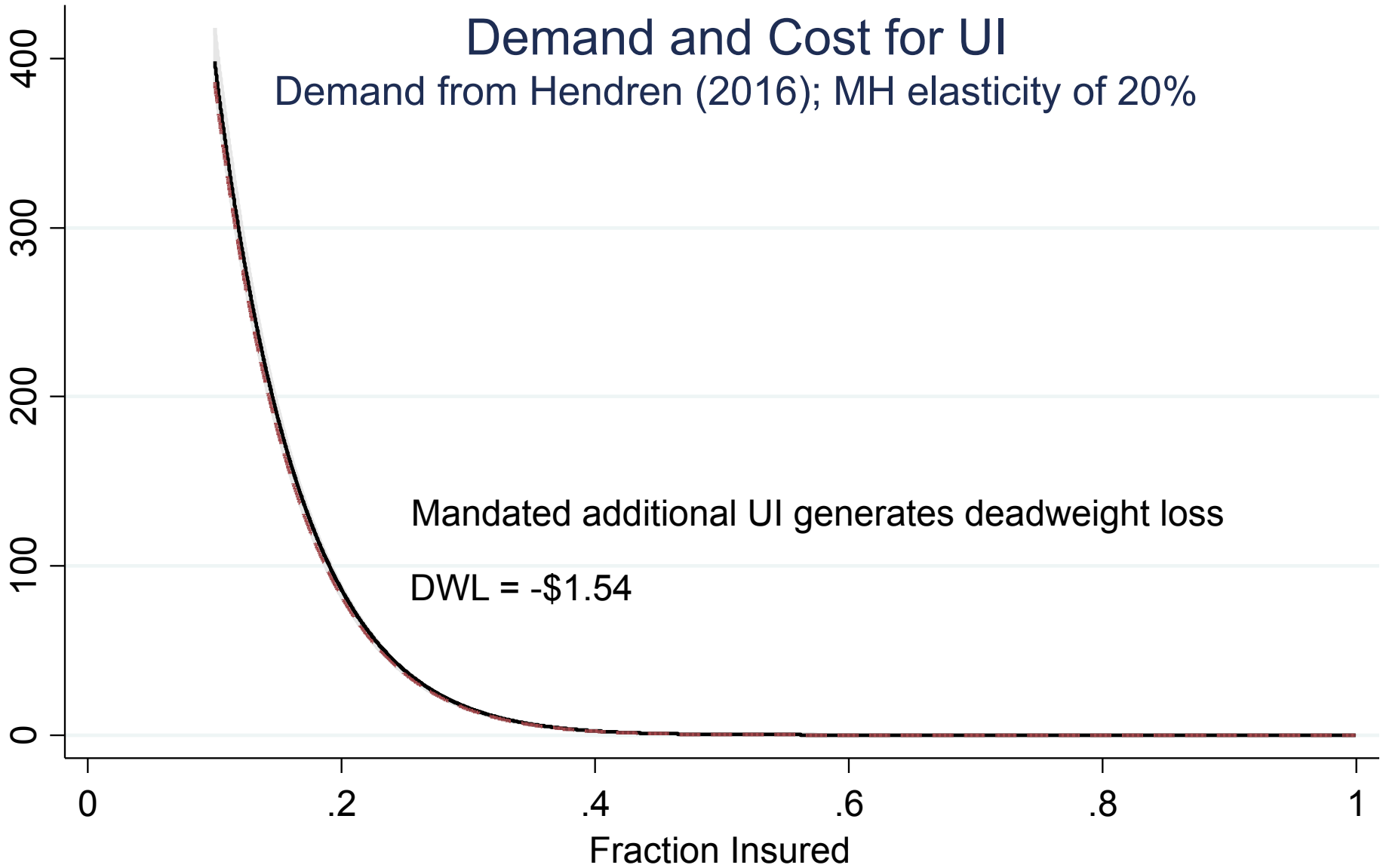
Demand from Hendren (2016); MH elasticity of 20%



- Demand, $D(s)$
- - - Marginal cost, $MC(s)$
- Ex-Ante Demand, $EA(s)+D(s)$

Demand and Cost for UI

Demand from Hendren (2016); MH elasticity of 20%



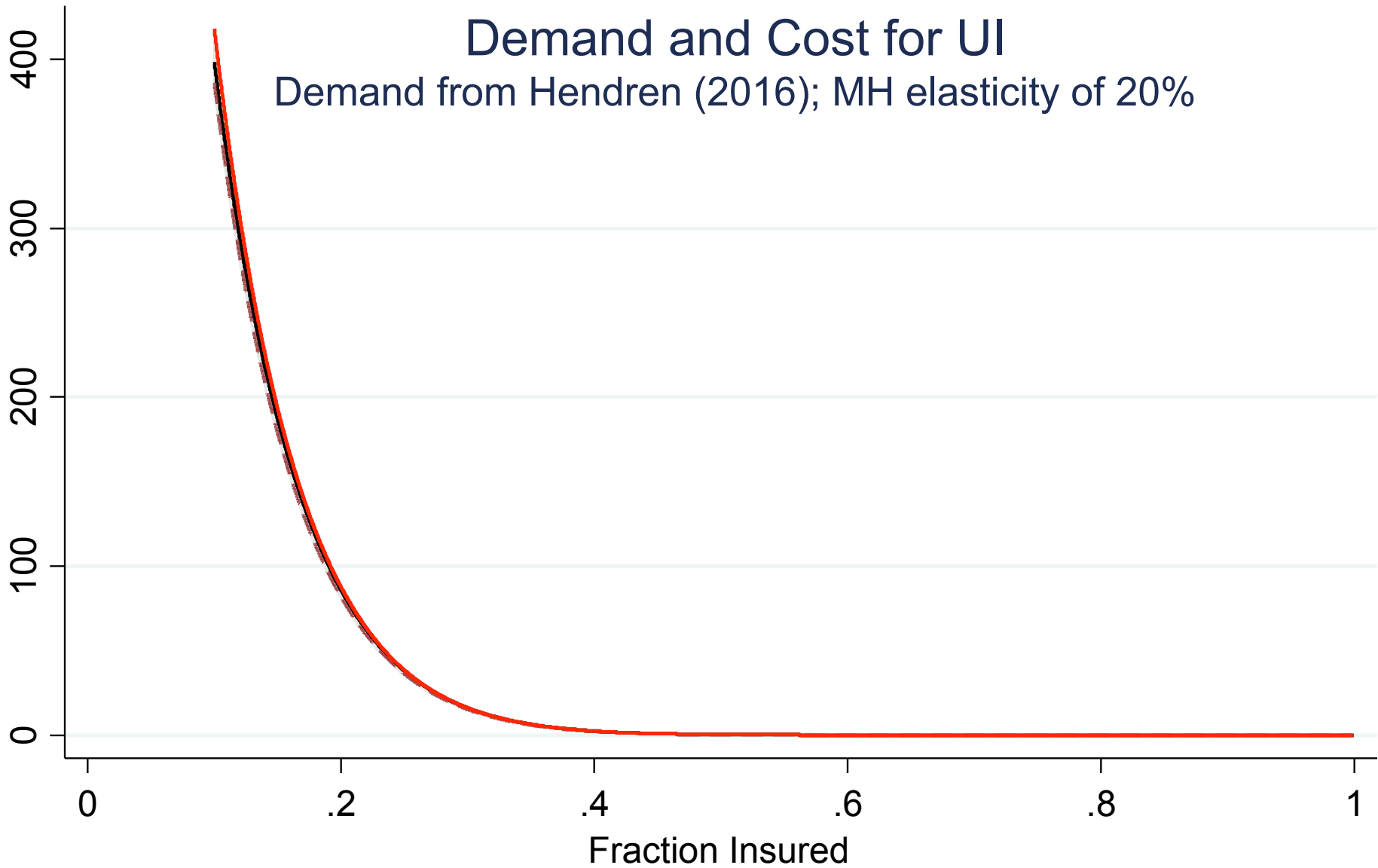
Mandated additional UI generates deadweight loss

DWL = -\$1.54

- Demand, D(s)
- - - Marginal cost, MC(s)
- Ex-Ante Demand, EA(s)+D(s)

Demand and Cost for UI

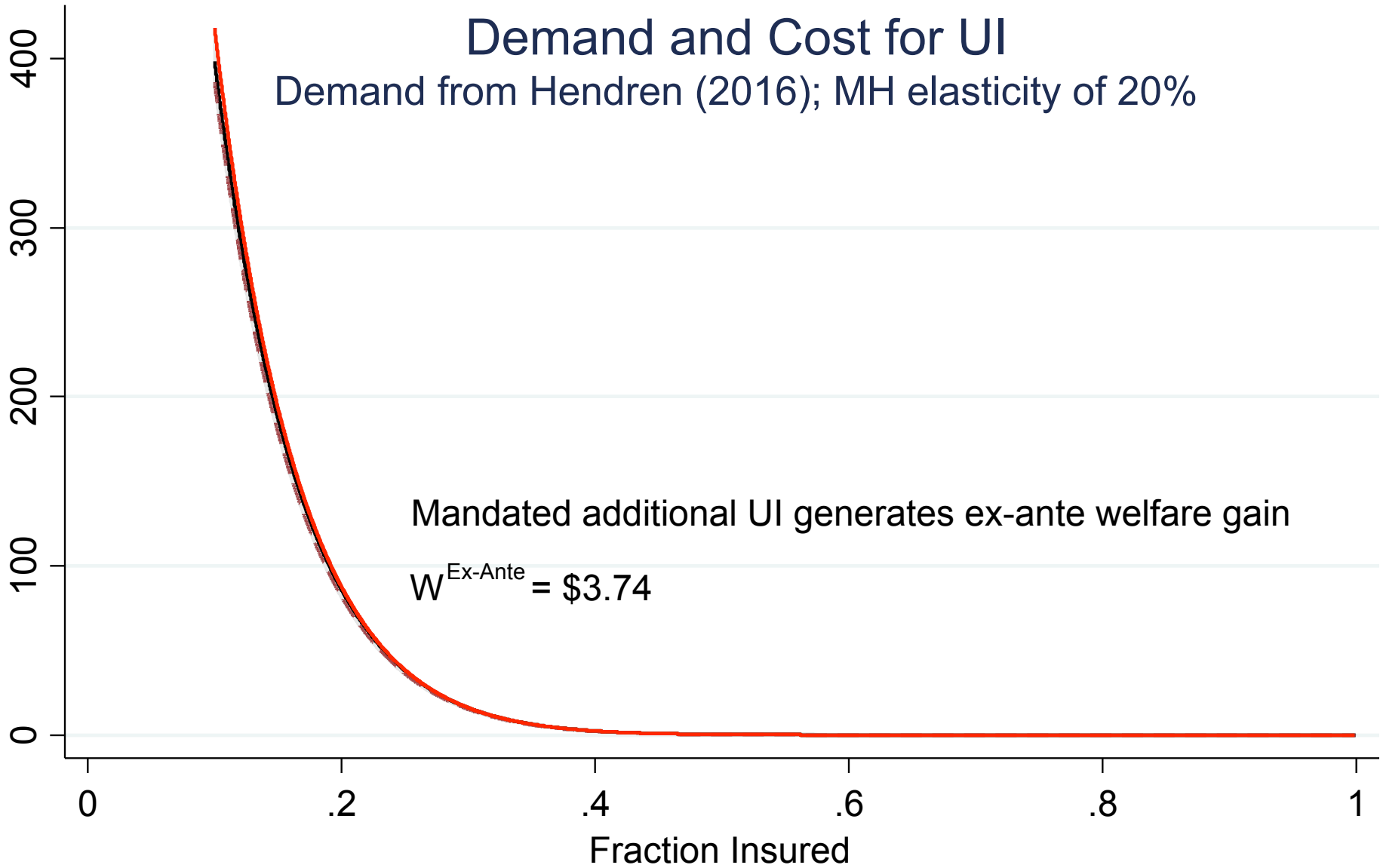
Demand from Hendren (2016); MH elasticity of 20%



— Demand, $D(s)$ - - - Marginal cost, $MC(s)$
— Ex-Ante Demand, $EA(s)+D(s)$

Demand and Cost for UI

Demand from Hendren (2016); MH elasticity of 20%



- Demand, D(s)
- - - Marginal cost, MC(s)
- Ex-Ante Demand, EA(s)+D(s)